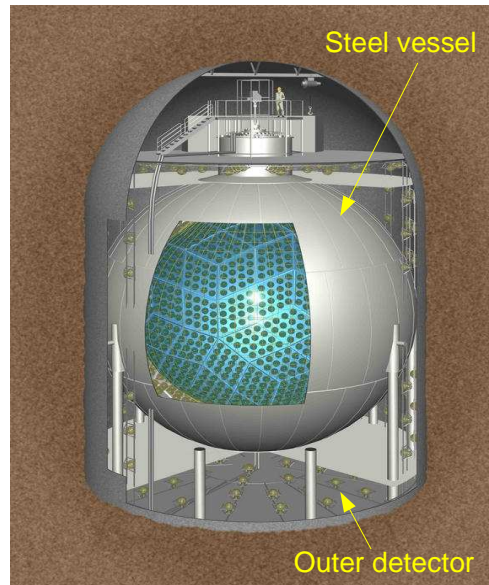


## 4. Reactor Experiments – Example KamLAND

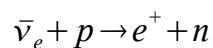
Kamioka Liquid scintillator Anti-Neutrino Detector located in the original KamiokaNDE cavity

- Site is surrounded by 53 Japanese commercial power reactors at an average distance  $L = 180$  km
- 9 m radius stainless steel vessel
- 1879 photomultipliers on the inner surface to measure scintillator light
- 6.5 m radius nylon balloon inside filled with 1000 t liquid scintillator (mineral oil, benzene and fluorescent chemicals)
- Balloon surrounded by non-scintillating oil shielding external radiation and supporting (nylon film is too thin to support 1000t)
- Steel vessel is surrounded by ultrapure water + Cerenkov counters – further shielding and veto against muons



Disappearance experiment:

$\bar{\nu}_e$  produced in reactors are detected via inverse  $\beta$ -decay with threshold  $E > 1.8$  MeV



Prompt scintillation light from  $e^+$  gives  $E_\nu$  – study  $E$  spectrum

$$E_\nu = E_{\text{prompt}} + \langle E_{n\text{recoil}} \rangle + 0.8 \text{ MeV}$$

$n$  capture by proton produces another 2.2 MeV  $\gamma$ -ray delayed by 200  $\mu\text{s}$   
- allows good background control

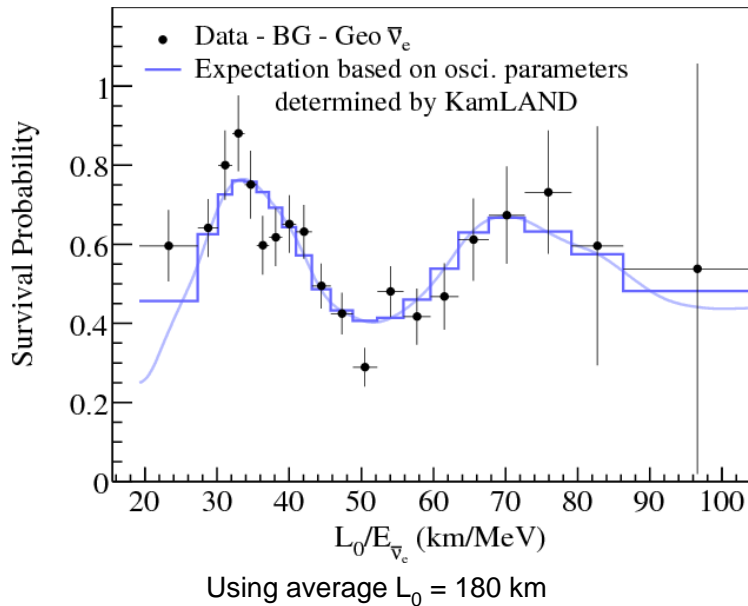
Very good sensitivity to  $\Delta m^2$  due to rather large  $L = 180$  km

$$P(\nu_\alpha \rightarrow \nu_\beta, t) = \sin^2 2\theta \sin^2 \left( \frac{\Delta m^2}{4E} L \right)$$

Note: solar neutrino are  $\nu_e$ , reactor neutrinos are  $\bar{\nu}_e$ . Different signature:  
for  $\nu_e$  there is no combination of prompt and delayed light.

## KamLAND Results

- Big deficit observed – in 1<sup>st</sup> study (2004) 258  $\nu_e$  w.  $E > 3.4$  MeV out of 365 expected
- Newest result for ratio (signal – geo bg) / expectation w/o oscillations



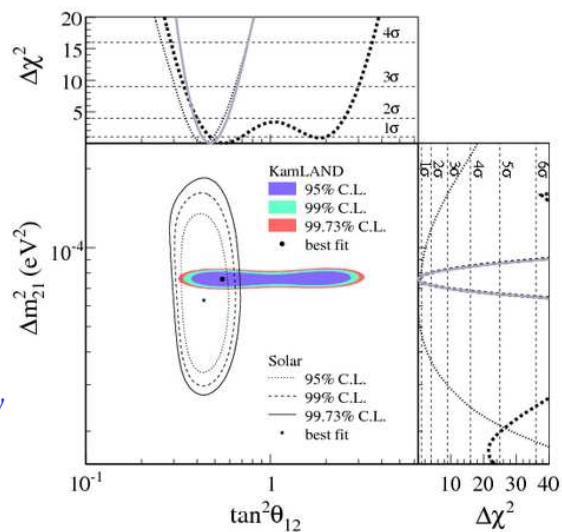
## KamLAND Results

Two-flavour analysis  $P(\nu_\alpha \rightarrow \nu_\beta, t) = \sin^2 2\theta \sin^2 \left( \frac{\Delta m^2}{4E} L \right)$

$$\Delta m^2 = (8.2 \pm 0.6) \times 10^{-5} \text{ eV}^2$$

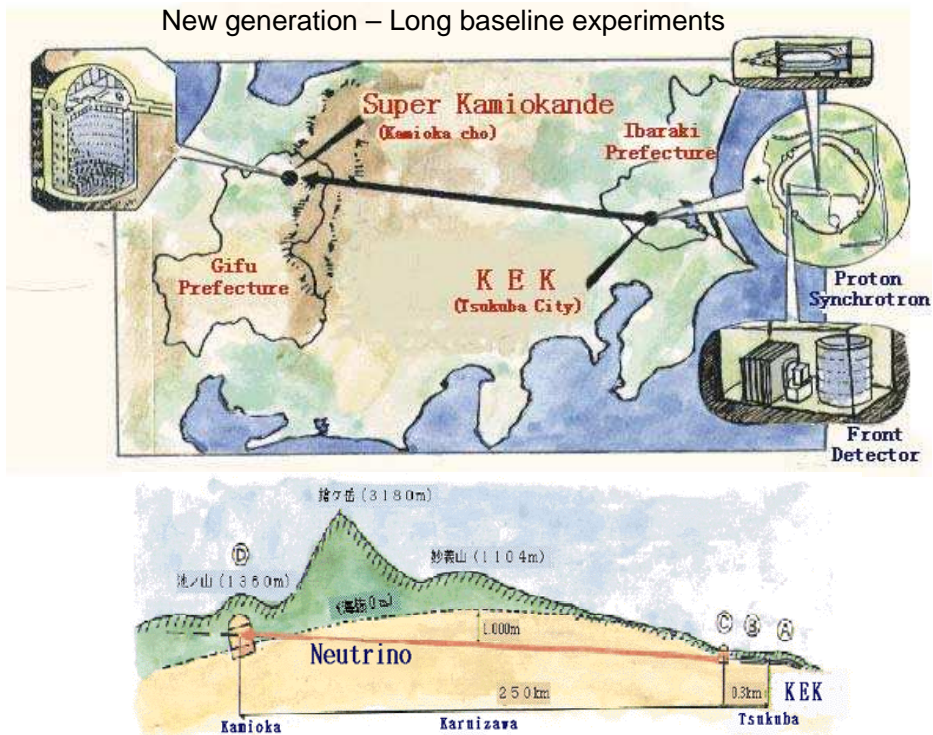
$$\sin^2 2\theta \approx 0.83$$

LMA = large mixing angle:  
MSW effect necessary for solar  $\nu$

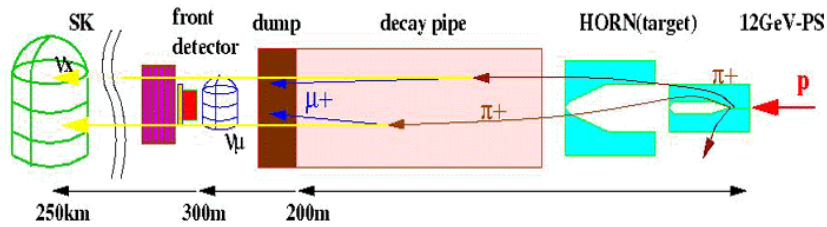


# 5. Accelerator Experiments – Example K2K

New generation – Long baseline experiments

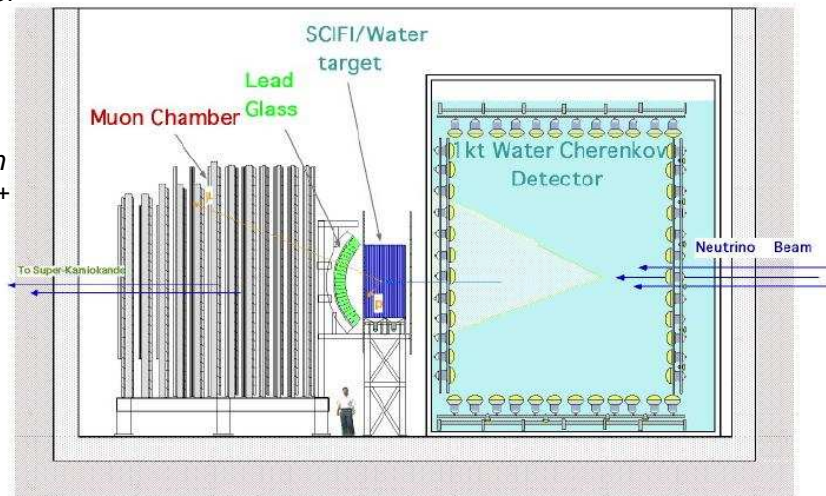


Scheme of the experiment



Front detector

measure CC  
 $\nu_\mu + n \rightarrow \mu^- + p$   
 and pion production  
 $\nu_\mu + p \rightarrow \mu^- + p + \pi^+$



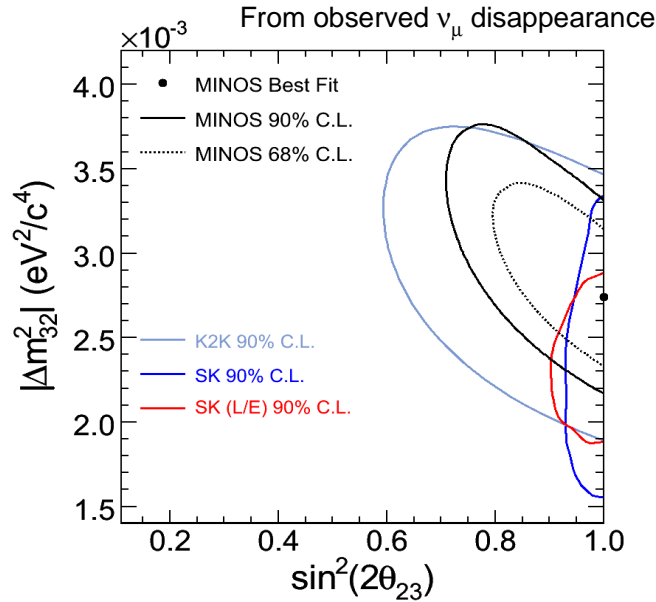
Similar experiment in the USA:

NuMI (Neutrinos at the Main Injector) at Fermilab + MINOS (Main Injector Neutrino Oscillation Search) in Soudan mine

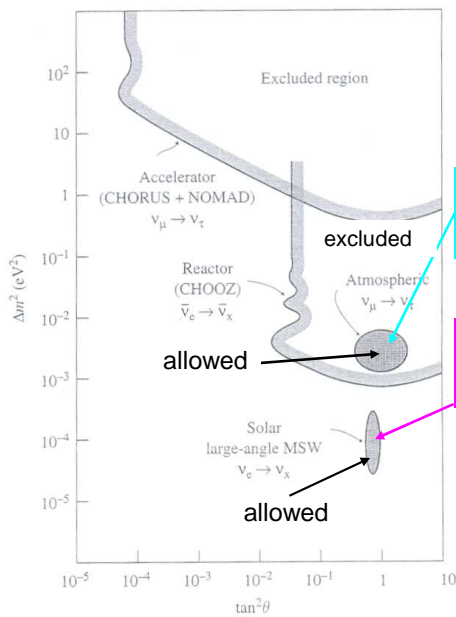
Distance: 735 km, 120 GeV protons

In Europe: CERN beam to Gran Sasso ICARUS and OPERA experiments

Distance: 730 km

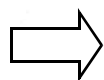


## Status of oscillation measurements



**Atmos**  $\Delta m^2 = (2.4 \pm 0.4) \times 10^{-3} \text{ eV}^2$   
 $\nu_\mu \rightarrow \nu_x$   $\sin^2 2\theta > 0.92$  @ 90 C.L.  
 + accelerator (not on this plot)

**Solar+KamLAND**  $\Delta m^2 = (8.2 \pm 0.6) \times 10^{-5} \text{ eV}^2$   
 $\nu_e \rightarrow \nu_x$   $\sin^2 2\theta \approx 0.83$

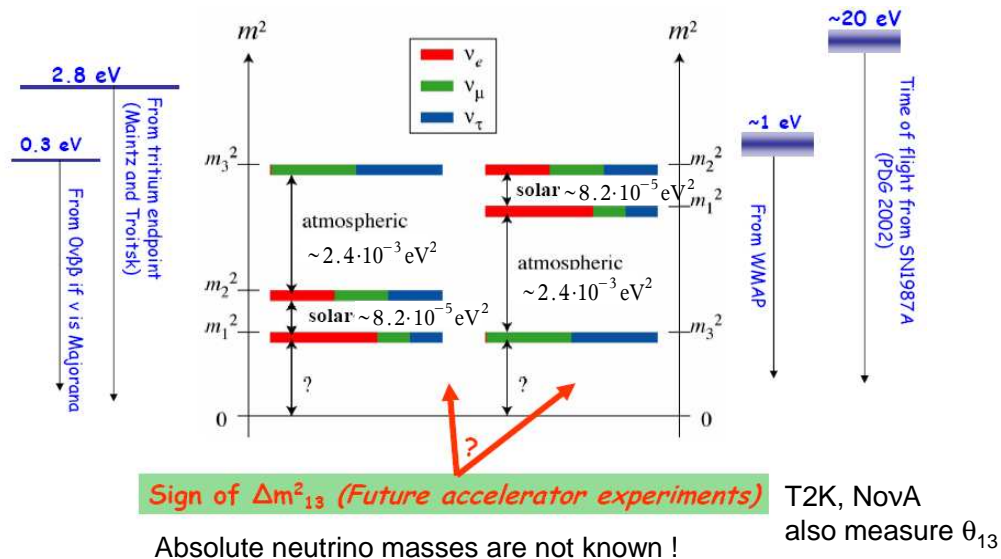


Different oscillation pattern for different neutrinos – what can we learn about the masses ??

## 6. Neutrino masses

$$U = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13} & c_{12}c_{23} - s_{12}s_{23}s_{13} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13} & -c_{12}s_{23} - s_{12}c_{23}s_{13} & c_{23}c_{13} \end{pmatrix} \quad \text{where } c_{ij} = \cos \theta_{ij}, \quad s_{ij} = \sin \theta_{ij}$$

$$\theta_{12} \equiv \theta_{sol} \quad \theta_{23} \equiv \theta_{atm} \quad \theta_{13} \approx 0$$



## Neutrino masses added to the Standard Model

- Mass term in the Lagrangian of a free massive Dirac field

$$L(\vec{x}, t) = i\bar{\psi}(\vec{x}, t)\gamma^\mu\partial_\mu\psi(\vec{x}, t) - m\bar{\psi}(\vec{x}, t)\psi(\vec{x}, t)$$

(Using Euler-Lagrange formalism  $L$  leads to the Dirac equation)

- Using chirality projection operators:
 
$$\bar{\psi}_L = \bar{\psi} \frac{1}{2}(1 + \gamma^5) \quad \psi_L = \frac{1}{2}(1 - \gamma^5)\psi$$

$$\bar{\psi}_R = \bar{\psi} \frac{1}{2}(1 - \gamma^5) \quad \psi_R = \frac{1}{2}(1 + \gamma^5)\psi$$

we get

$$m\bar{\psi}\psi = m\bar{\psi}\left[\frac{1}{2}(1 - \gamma^5) + \frac{1}{2}(1 + \gamma^5)\right]\psi =$$

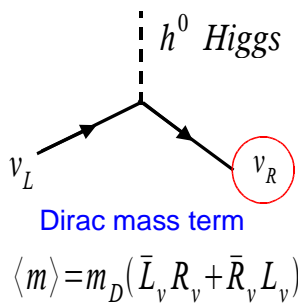
$$= m\bar{\psi}\left[\frac{1}{2}(1 - \gamma^5) + \frac{1}{2}(1 + \gamma^5)\right]\left[\frac{1}{2}(1 - \gamma^5) + \frac{1}{2}(1 + \gamma^5)\right]\psi =$$

$$= m\bar{\psi}_R\psi_L + m\bar{\psi}_L\psi_R$$

because  $\gamma^5\gamma^5 = 1 \longrightarrow (1 - \gamma^5)(1 + \gamma^5) = 1 - \gamma^5\gamma^5 = 0$

# Neutrino masses added to the Standard Model

- Neutrino Mass term: the same as for charged leptons:  $\sim m \bar{\psi}_R \psi_L$



Masses of neutrinos through Yukawa coupling to Higgs:

$$m_\nu = \frac{\lambda_\nu v}{\sqrt{2}}$$

From the vacuum expectation value of the Higgs,  $v \approx 246$  GeV, follows that the Yukawa coupling must be extremely small ( $< 10^{-11}$ ) to generate the small neutrino masses.

→ unnatural

- Dirac mass terms imply existence of right (left) -handed (anti) neutrinos.

Minimal extension of the Standard Model:

Introduce singlets of right (left)-handed (anti)neutrinos which do not couple to charged and neutral currents.

- Lepton numbers:  $L_e$ ,  $L_\mu$  and  $L_\tau$  are not conserved.  $L$  is conserved !!
- But why are the neutrino masses so small ?

# Majorana Neutrinos

- Unlike the charged leptons, neutrinos could be their own anti-particles:
- Majorana-mass terms in addition to Dirac mass terms possible:

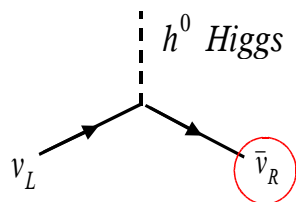
## Majorana Neutrinos

$$\nu = \bar{\nu} \begin{cases} \bar{\nu}_L = \nu_L \\ \nu_R = \bar{\nu}_R \end{cases}$$

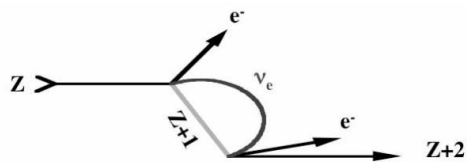
Majorana mass term

$$\langle m \rangle = (\bar{L}_\nu, \bar{L}_{\bar{\nu}}) \begin{pmatrix} m_{M,L} & 0 \\ 0 & m_{M,R} \end{pmatrix} \begin{pmatrix} R_{\bar{\nu}} \\ R_\nu \end{pmatrix} + c.c.$$

Mass term violates Lepton flavor conservation:  $\Delta L = \pm 2$



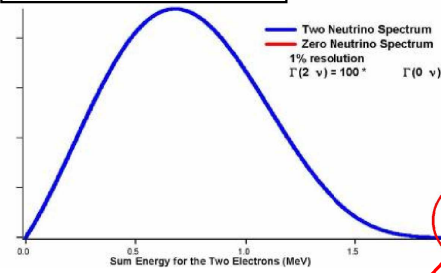
- Majorana character can be checked in neutrinoless double beta decay ( $0\nu 2\beta$ ):



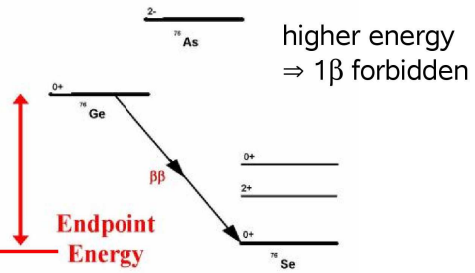
- Can we prove that neutrino is a Dirac particle

# Search for $0\nu 2\beta$

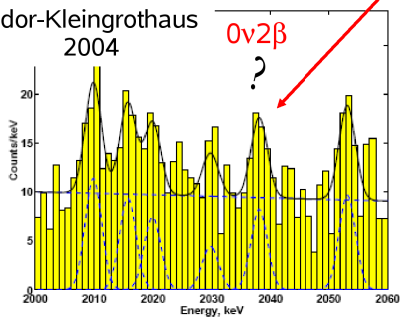
$2\beta$  energy spectrum



Germanium decay (example)



Klapdor-Kleingrothaus 2004



Isotope	Half-life (years)	$m_{\beta\beta}$ (meV)	Reference
$^{48}\text{Ca}$	$>1.4 \times 10^{22}$	$<7200-44700$	[7]
$^{76}\text{Ge}$	$>1.9 \times 10^{25}$	$<350$	[8]
$^{76}\text{Ge}$	$>1.6 \times 10^{25}$	$<330-1350$	[9]
$^{76}\text{Ge}$	$=1.2 \times 10^{25}$	$=440$	[10]
$^{82}\text{Se}$	$>2.7 \times 10^{22}$ (68%)	$<5000$	[11]
$^{100}\text{Mo}$	$>5.5 \times 10^{22}$	$<2100$	[12]
$^{116}\text{Cd}$	$>1.7 \times 10^{23}$	$<1700$	[13]
$^{126}\text{Te}$	$>7.7 \times 10^{24}$ (geochem)	$<1100-1500$	[14]
$^{130}\text{Te}$	$>5.5 \times 10^{25}$	$<370-1900$	[15]
$^{136}\text{Xe}$	$>4.4 \times 10^{23}$	$<1800-5200$	[16]
$^{150}\text{Nd}$	$>1.2 \times 10^{21}$	$<3000$	[17]

## Seesaw mechanism to generate light neutrinos

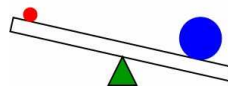
- If neutrinos are Majorana particles:

Introduce in addition to the Dirac mass term also a Majorana mass term for the right-handed neutrino singlet:

$$\langle m \rangle = (\bar{L}_\nu, \bar{L}_{\bar{\nu}}) \begin{pmatrix} m_{M,L} & m_D \\ m_D & m_{M,R} \end{pmatrix} \begin{pmatrix} R_{\bar{\nu}} \\ R_\nu \end{pmatrix} + c.c.$$

**Seesaw Model:** Assume Higgs mechanism gives Dirac masses at EW scale, and very high (GUT) Majorana mass  $M_R$  of the right-handed neutrino, and zero Majorana mass  $M_L$  of left handed neutrino = 0. The eigenstates for weak interaction are eigenstates of this matrix. Diagonalising gives:

$$m_\nu = \frac{m_D^2}{M_R}$$



- Small neutrino masses can be explained ... but how large is  $M_R$  ( $10^{10} \dots 10^{15}$  GeV) ?