

Physics at the LHC - WS 2021-2022

Rare B decays and Lepton Universality

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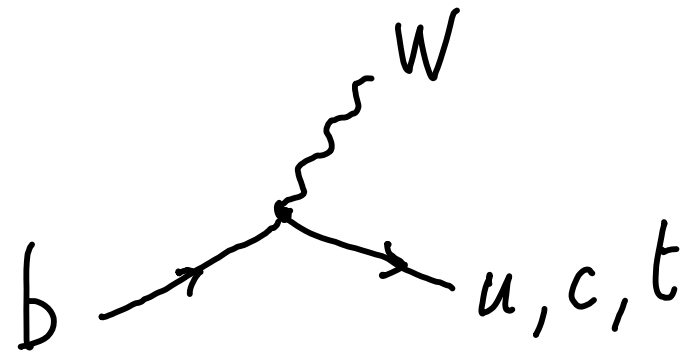
Credits/references

- P.Owen lecture at HCPSS2021
- M.Williams LHCb StarterTalk
- LHCb detector performance [paper](#)

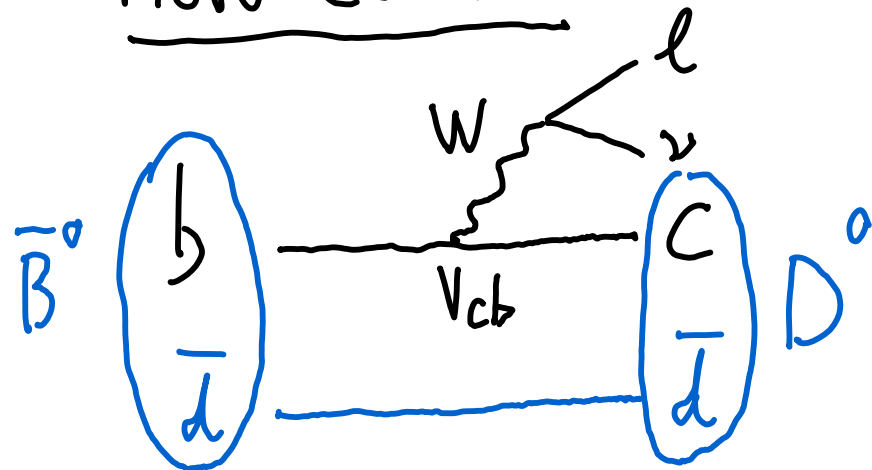
Lecture 2/4 - Monday Jan 17th 2022

Rare B decays

- B decays weakly



Most common



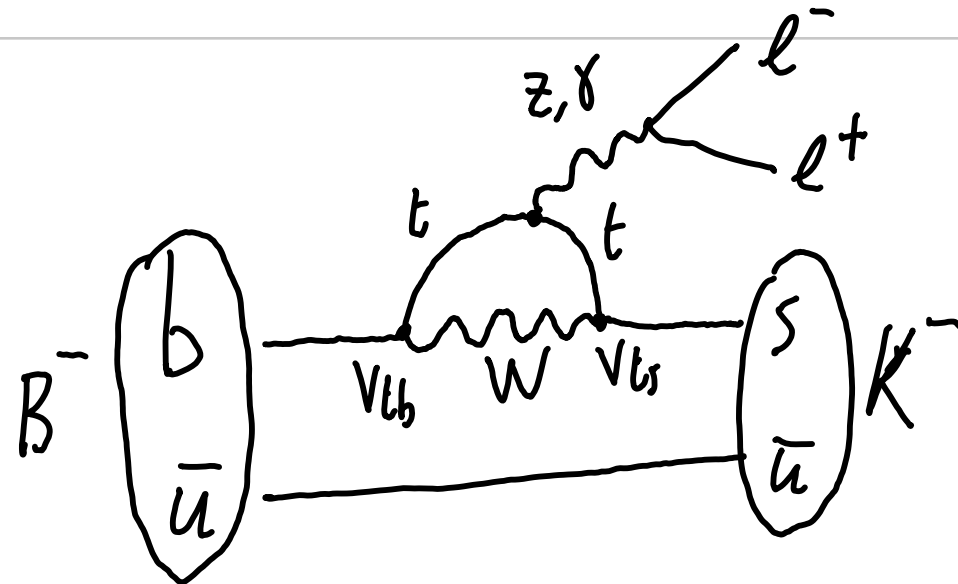
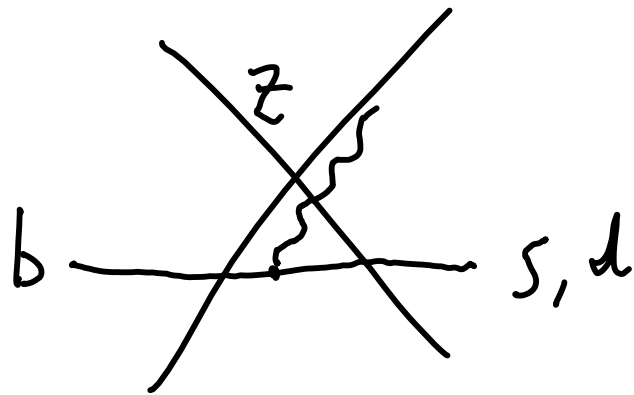
$$BR(\bar{B}^0 \rightarrow D^0 l \nu) \sim 2\%$$

$$\propto V_{CKM} = \begin{bmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & \boxed{V_{cb}} \\ V_{td} & V_{ts} & \cancel{V_{tb}} \end{bmatrix}$$

$$= \begin{bmatrix} 1 & 0.1 & 0.001 \\ 0.1 & 1 & 0.01 \\ 0.001 & 0.01 & 1 \end{bmatrix}$$

$$\Rightarrow \text{Rare B decay} < 10^{-4}$$

Flavour-Changing Neutral Currents

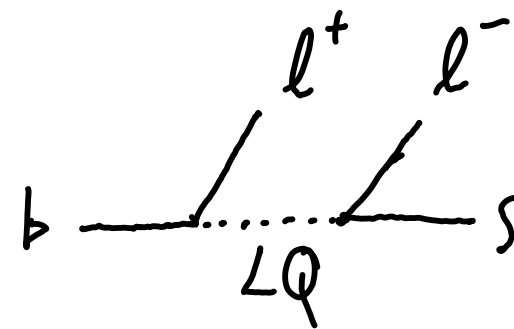
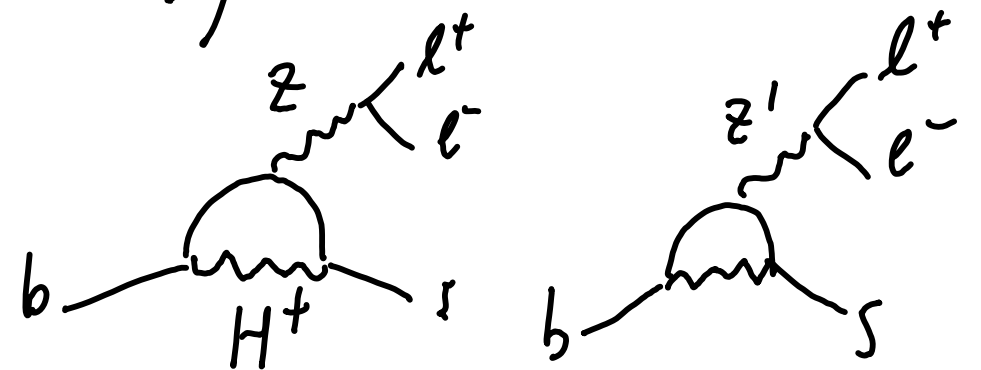


$10^{-5} \div 10^{-10}$

SUPPRESSED : 1) CKM V_{ts} 2) LOOP 3) GIM

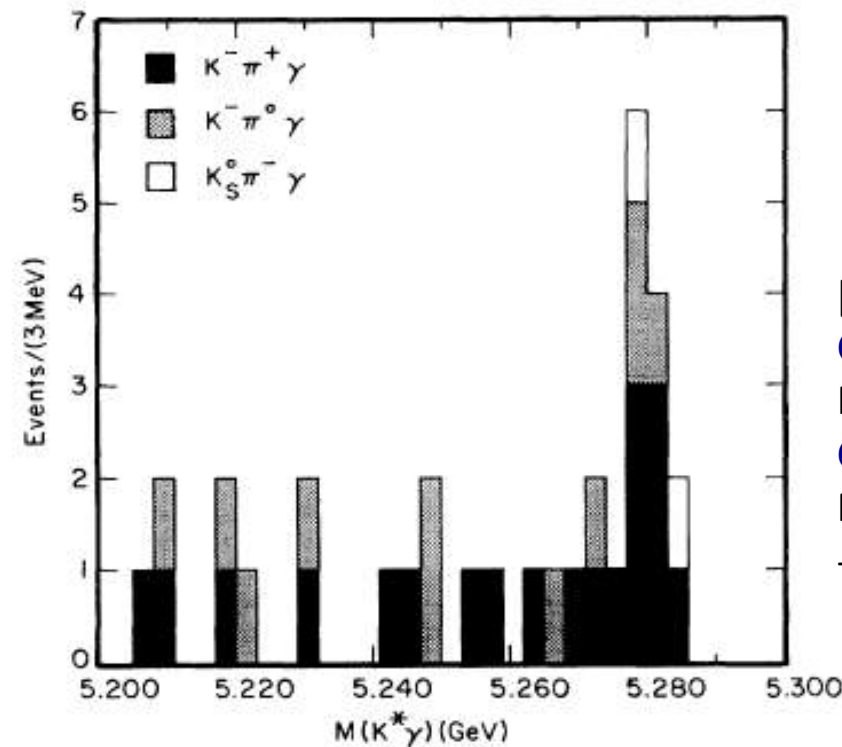
WHY INTERESTING?

- TEST the flav. structure of the SM
- SEARCH FOR NEW PARTICLES
- WORKED IN THE PAST
 $K \rightarrow \mu\mu \Rightarrow$ charm



First $b \rightarrow s$ FCNC: $b \rightarrow s\gamma$

- Discovered in 1993 at CLEO
 - $\text{BR}(B \rightarrow K^*\gamma) \simeq 4 \times 10^{-5}$
 - Quark transition $b \rightarrow s\gamma$
- Nowadays $b \rightarrow s\gamma$ well known
 - Many decays studied \rightarrow
 - Measured CP violation, mixing, polarisation of the emitted γ
- All measurements agree with SM
 - Great constraints on e.g. SUSY
 - Still space for improvement
- $b \rightarrow s\gamma$ hard at LHCb (neutral γ)



[Phys.Rev.Lett. 71 (1993) 674 -
Cited by 605 records
Phys.Rev.Lett. 74 (1995) 2885 -
Cited by 836 records
Phys.Rev.Lett. 87 (2001) 251807
- Cited by 565 records]

$$B^+ \rightarrow K^{*+} \gamma$$

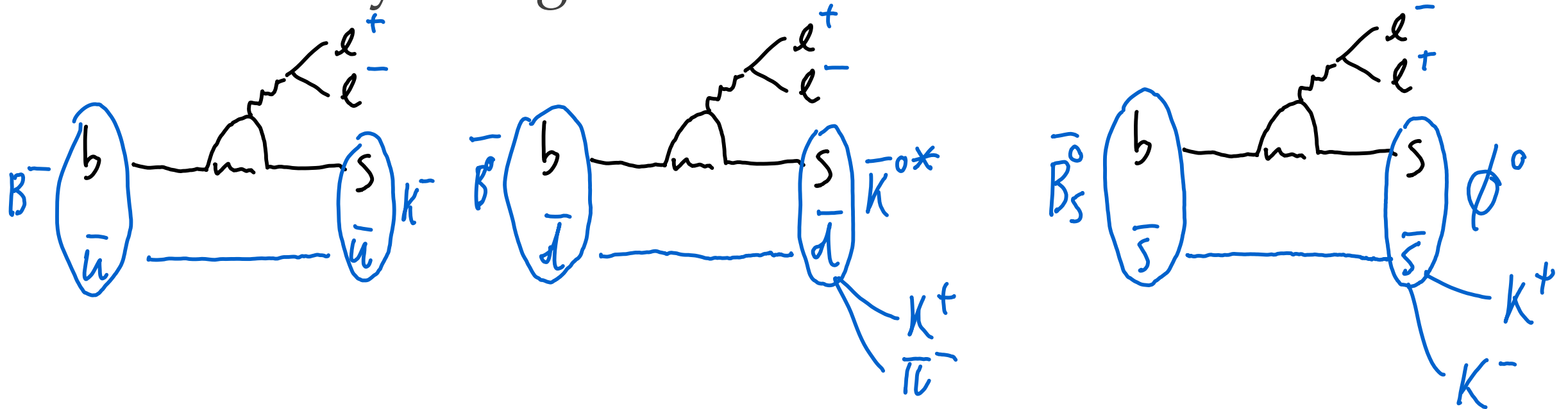
$$\hookrightarrow K^+ \pi^0, K^0 \pi^+$$

$$B^0 \rightarrow K^{*0} \gamma$$

$$\hookrightarrow K^+ \pi^-, \cancel{K^0 \pi^0}$$

$b \rightarrow s \ell^+ \ell^-$ at LHCb

- Several fully charged final states

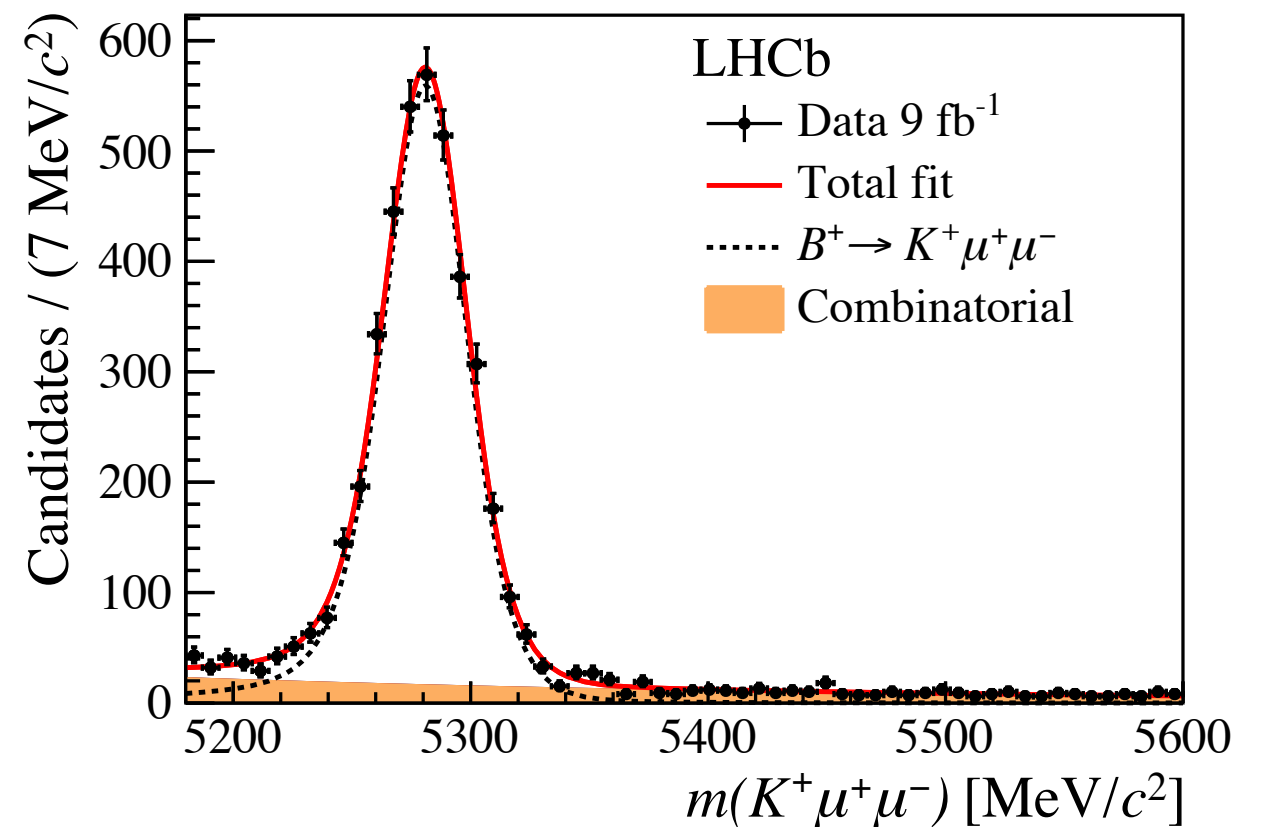


Selecting $b \rightarrow s\mu\mu$

- Hardware trigger: μ , $\mu\mu$
- Software trigger: displaced charged tracks forming vertex
- Muon and charged-hadron identification
- Machine Learning classifier to label events that are more likely to contain signal
- Fit to B invariant mass to subtract background
 - Mostly combinatorial combination of tracks



$\sim 4\text{k } B^+ \rightarrow K^+ \mu^+ \mu^-$
BR of about 1.2×10^{-7}



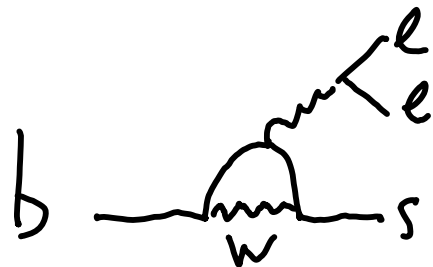
Measuring the BR

- Decay amplitude gets contribution from NP
→ Decay Branching Ratio can be different

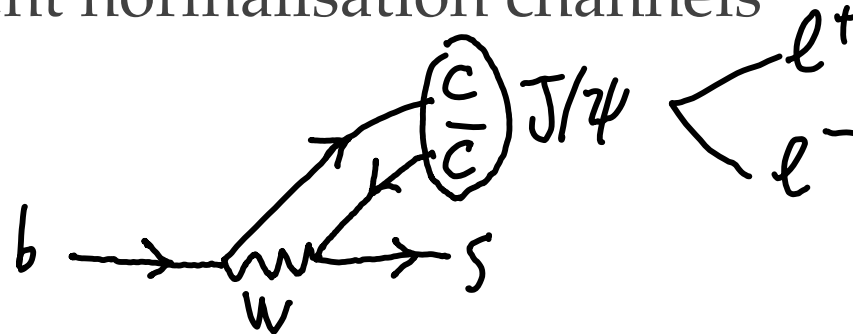
- Measuring BR at LHCb**

- Hard to know how many B are produced
- Always normalise to other decay channel

- $b \rightarrow s \ell^+ \ell^-$ have excellent normalisation channels



$$BR(B^+ \rightarrow K^+ \ell^+ \ell^-) \sim 10^{-7}$$



$$BR(B^+ \rightarrow J/\psi K^+) \sim 10^{-3}$$

$$BR(J/\psi \rightarrow \ell^+ \ell^-) \sim 6 \times 10^{-2}$$

$$BR(B^+ \rightarrow K^+ J/\psi \rightarrow \ell^+ \ell^-) \sim 6 \times 10^{-5}$$

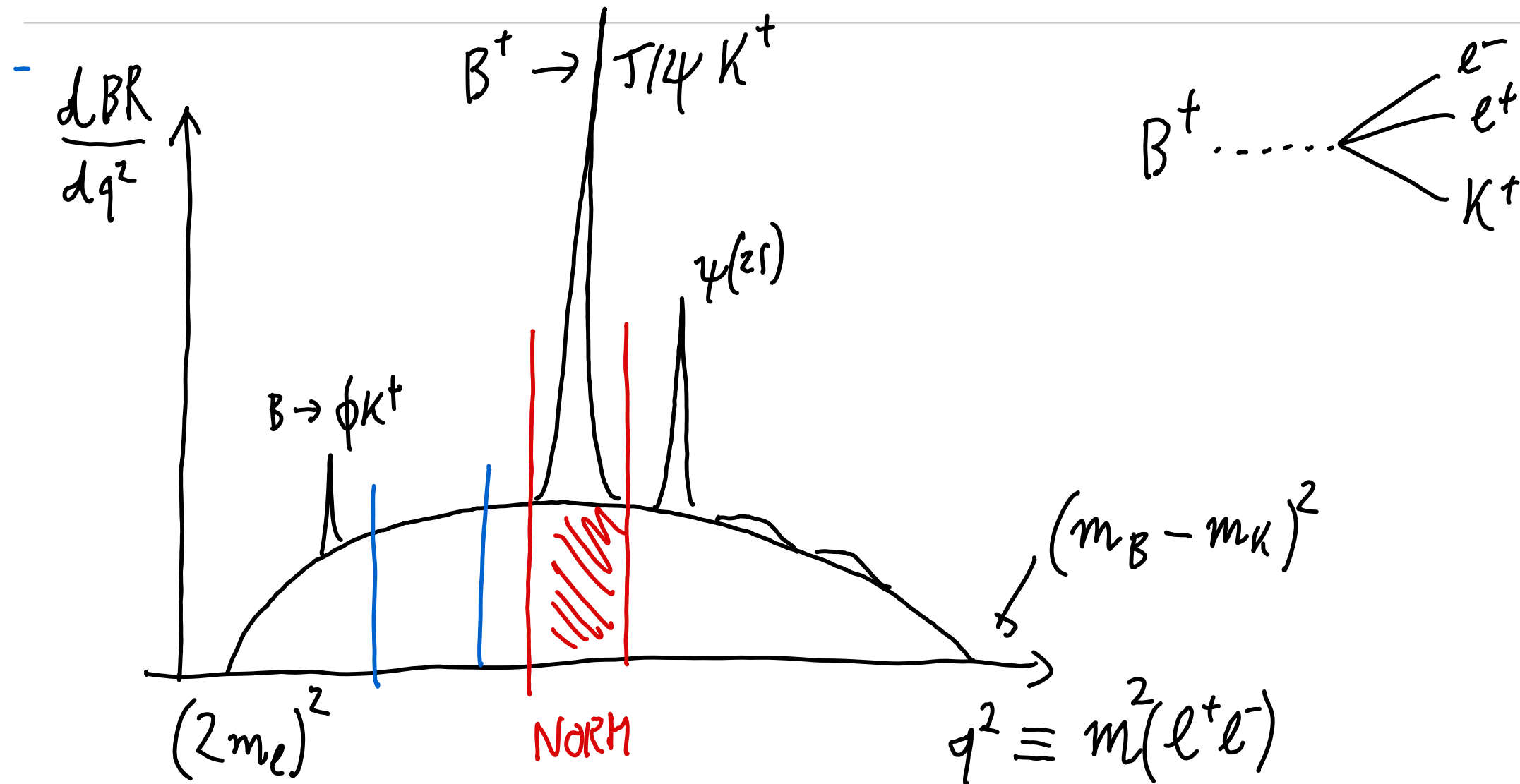
SIGNAL DECAY

B factories

$$BR(S) = \frac{N_S}{N_N} \underbrace{\left(\frac{\epsilon_N}{\epsilon_S} \right)}_{\sim 1} BR(N)$$

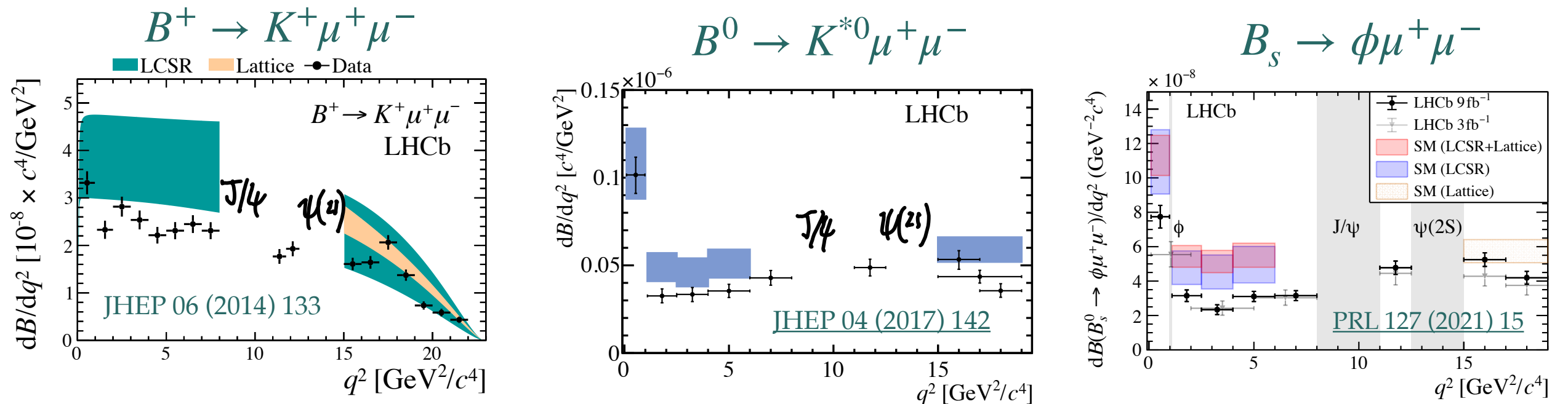
NORMALISATION DECAY

A function of q^2



$$\frac{dBR(B \rightarrow K l l)}{dq^2} = \frac{N_S^{q^2_{avg}}}{N_N} \frac{\sum_N}{\sum_S} \frac{BR(N)}{\Delta q^2} \leftarrow \text{bin width}$$

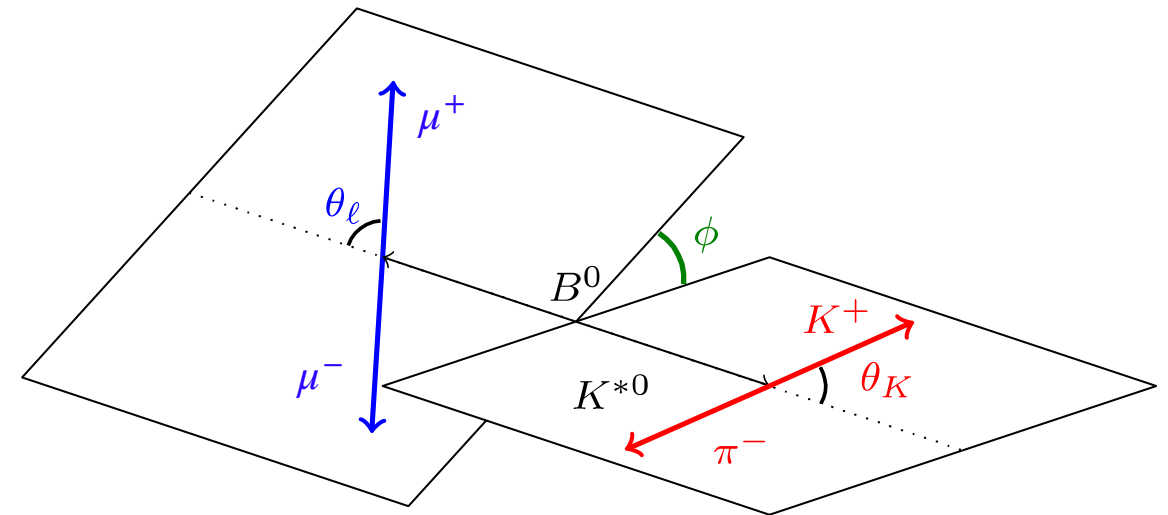
BR results



- Measured dBR/dq^2 in various decay modes
- Predictions have large uncertainties (10-20%)
- All rates lower than SM predictions
 - Is this a sign of NP contributions (negative interference with SM)
 - Or is this just a sign that these SM predictions are hard to do?

Angular analyses

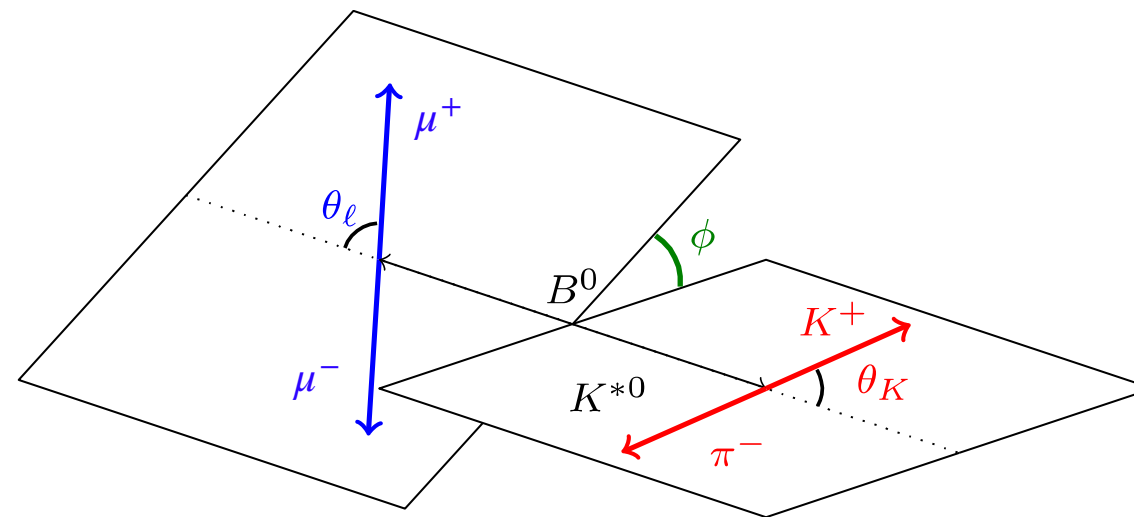
- Can study other properties of the B decay
 - e.g. $B^0 \rightarrow K^{*0} \ell^+ \ell^-$ has rich structure
- Full decay kinematic described as function of q^2 and three angles



$$\frac{1}{d(\Gamma + \bar{\Gamma})/dq^2} \frac{d^4(\Gamma + \bar{\Gamma})}{dq^2 d\vec{\Omega}} = \frac{9}{32\pi} \left[\frac{3}{4}(1 - F_L) \sin^2 \theta_K + F_L \cos^2 \theta_K \right. \\ \left. + \frac{1}{4}(1 - F_L) \sin^2 \theta_K \cos 2\theta_l - F_L \cos^2 \theta_K \cos 2\theta_l + S_3 \sin^2 \theta_K \sin^2 \theta_l \cos 2\phi \right. \\ \left. + S_4 \sin 2\theta_K \sin 2\theta_l \cos \phi + S_5 \sin 2\theta_K \sin \theta_l \cos \phi \right. \\ \left. + \frac{4}{3} A_{FB} \sin^2 \theta_K \cos \theta_l + S_7 \sin 2\theta_K \sin \theta_l \sin \phi \right. \\ \left. + S_8 \sin 2\theta_K \sin 2\theta_l \sin \phi + S_9 \sin^2 \theta_K \sin^2 \theta_l \sin 2\phi \right]$$

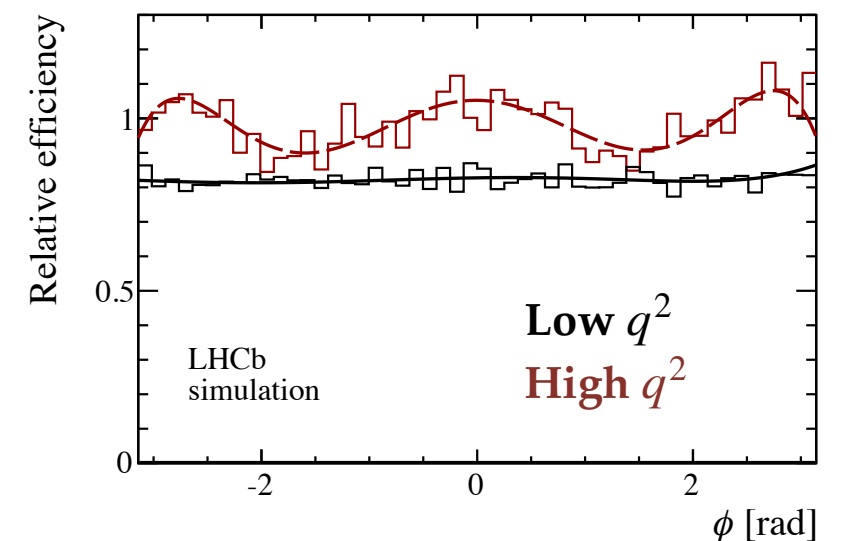
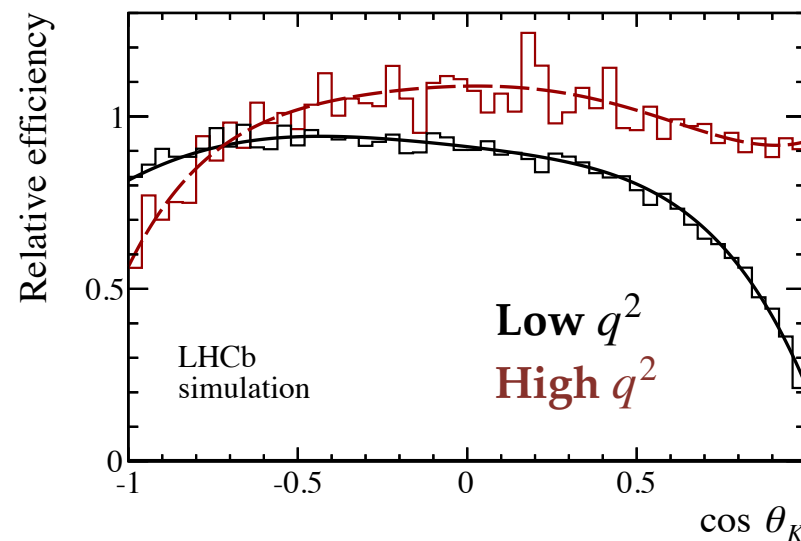
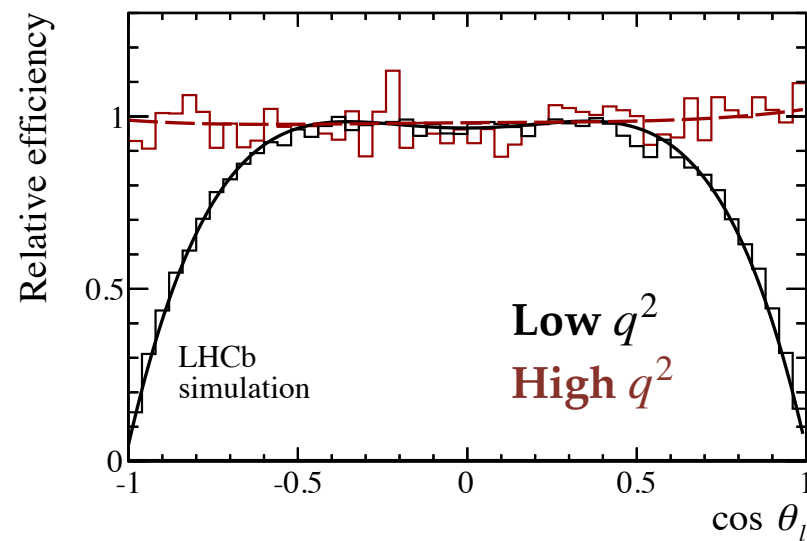
$d\cos\theta_l d\cos\theta_K d\phi$

Correcting acceptance effects



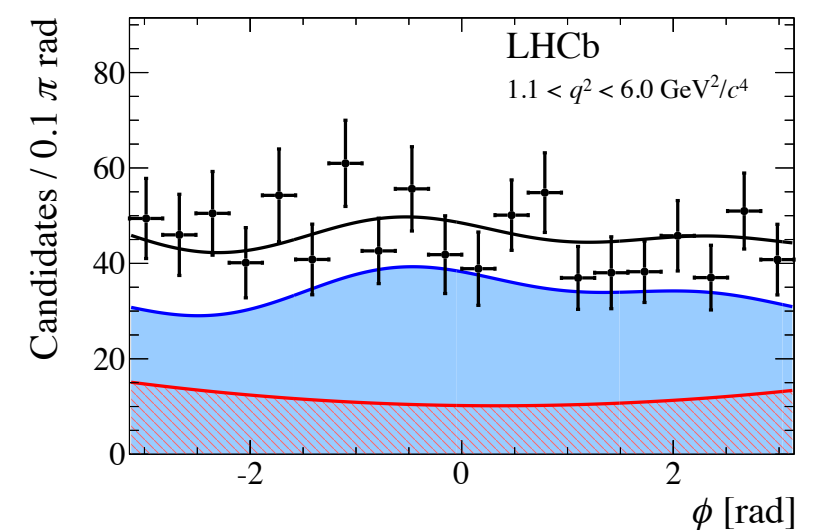
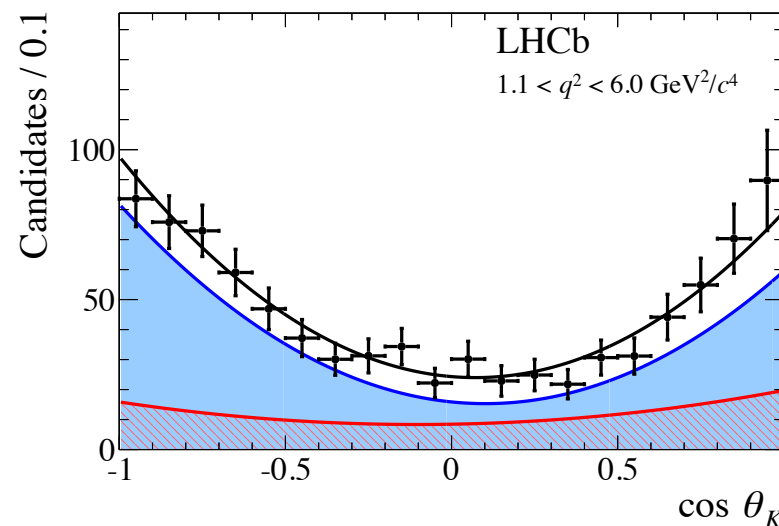
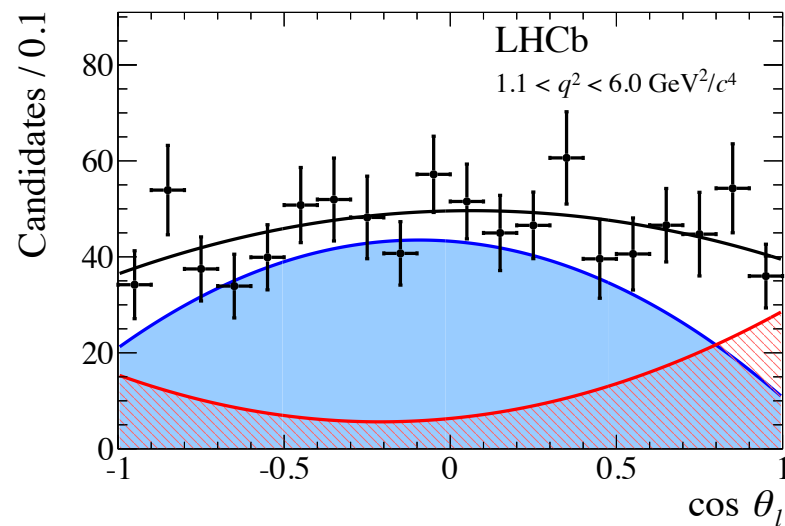
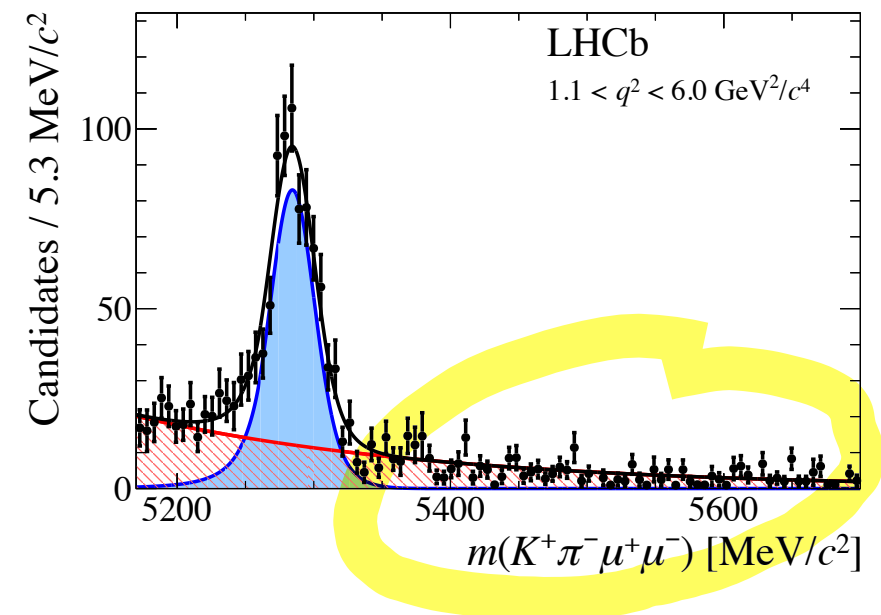
$$\cos \theta_\ell \sim \frac{E_{e^+} - E_{e^-}}{E_{e^+} + E_{e^-}}$$

$$\cos \theta_K \sim \frac{E_{K^+} - E_{\pi^-}}{E_{K^+} + E_{\pi^-}}$$

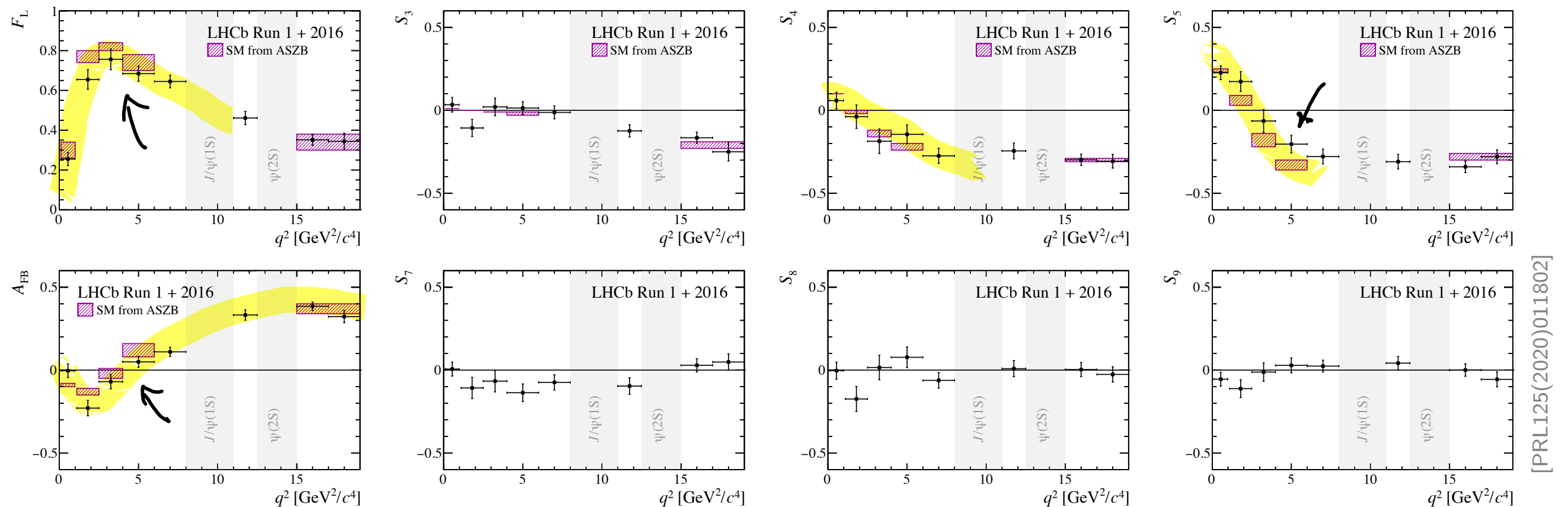


Multidimensional fit

- Fit physical probability density function (PDF) to acceptance-corrected data
- Use B mass fit to subtract background and to model it in the angular dimensions
- Fit three angles simultaneously and extract **angular observables** in bins of q^2



Results angular analysis



- Measure 8 angular observables in 8 q^2 bins (64 numbers!)
- Deviations at 1-2 sigma level observed in some observables
→ is it simply look-elsewhere effect?

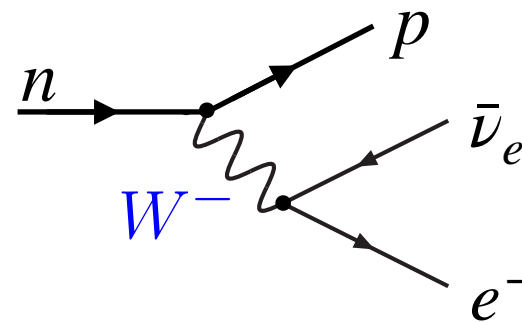
Interpretation

- Integrate out $> m_W$
- four-fermion interaction described by effective couplings

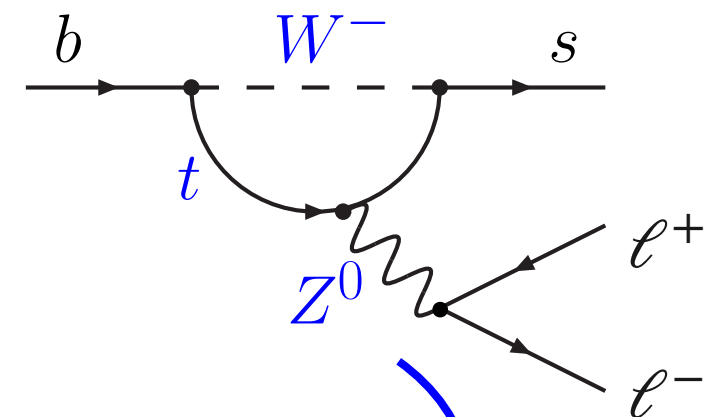
$$C_i = C_i^{\text{SM}} + C_i^{\text{NP}}$$

- Main SM contributions:
 - Vector** (C_9) and **Axial-vector** (C_{10}) leptonic currents
 - $b \rightarrow s\gamma^*$ contribution in (C_7)
 \rightarrow very well constrained by radiative decays

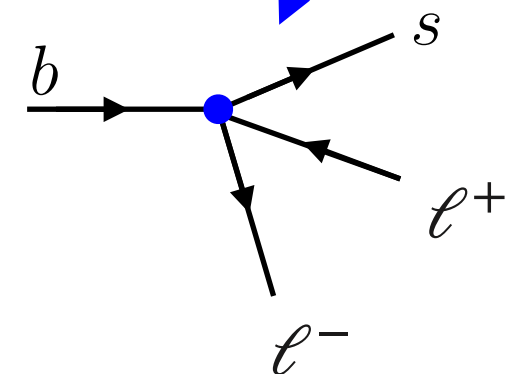
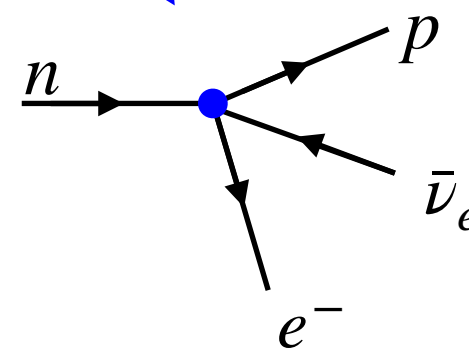
β decay



$b \rightarrow s\ell\ell$



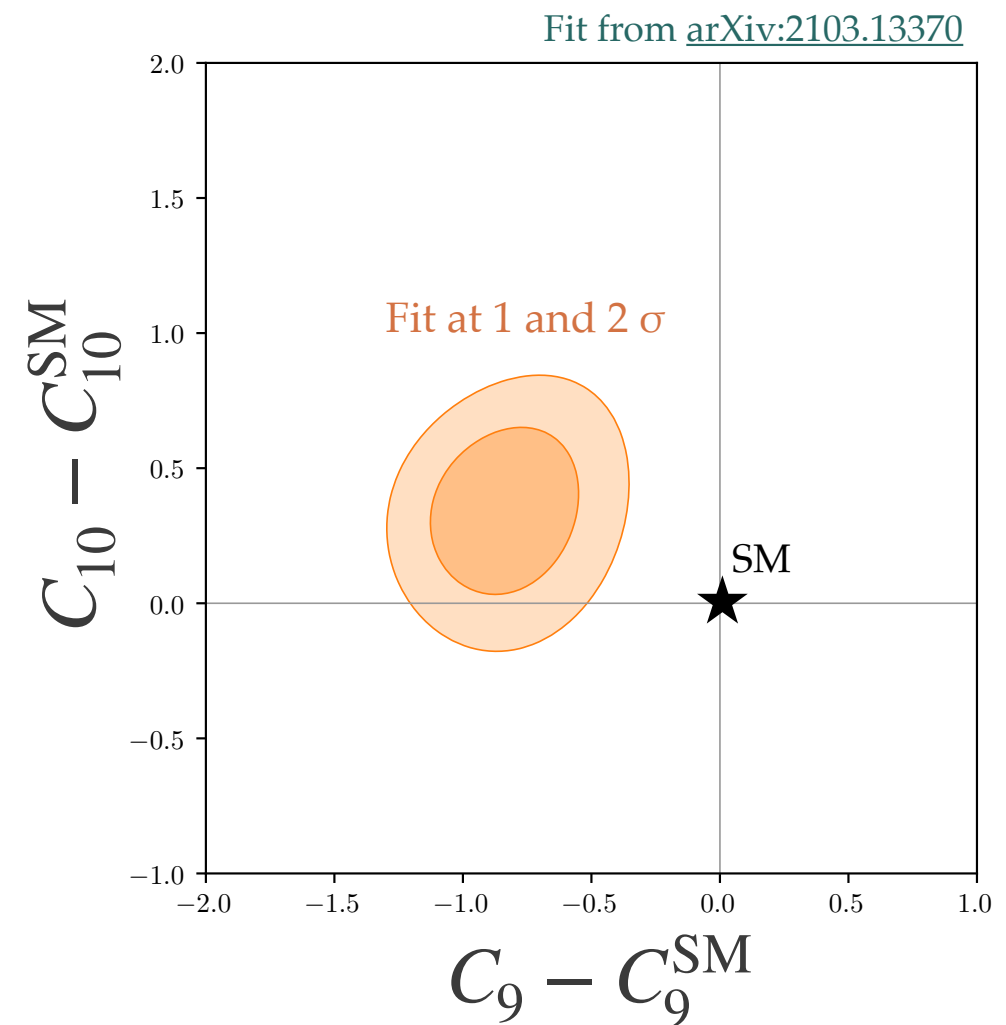
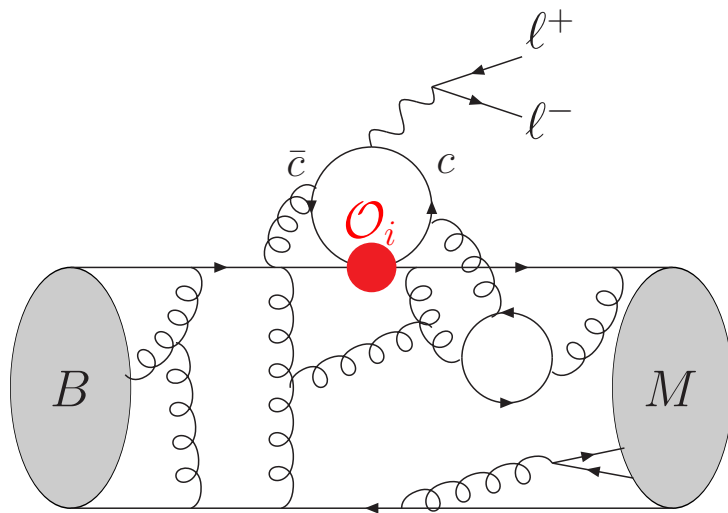
integrate out $> m_W$



$$\mathcal{H}_{\text{eff}} = \frac{G_F}{\sqrt{2}} V_{tb} V_{ts}^* \sum_i C_i \mathcal{O}_i$$

Interpretation

- Fit most relevant effective couplings C_9 and C_{10} to data
- Use all $b \rightarrow s\mu\mu$ measurements
 - Branching ratios
 - Angular analyses
- Fitted couplings do not match SM expectation (**anomaly!**)
 - Coherent picture from BR and angular analyses
 - SM predictions still under scrutiny

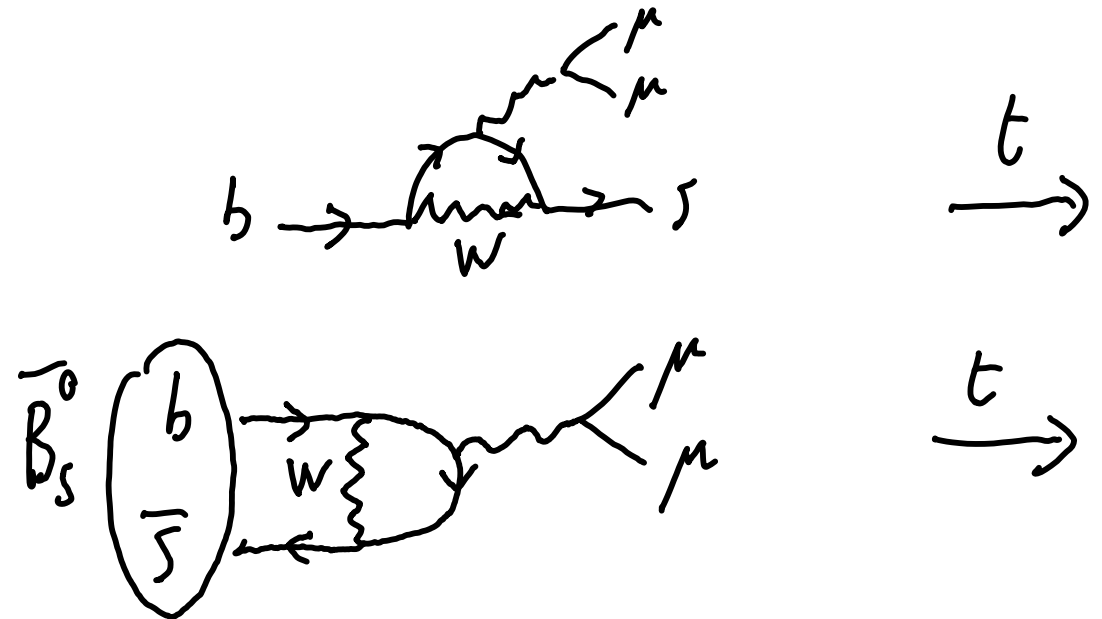


Similar fits from other groups:
Algueró et al., [arXiv:1903.09578](https://arxiv.org/abs/1903.09578)
Kowalska et al., [arXiv:1903.10932](https://arxiv.org/abs/1903.10932)
Ciuchini et al., [arXiv:2011.01212](https://arxiv.org/abs/2011.01212)
Datta et al., [arXiv:1903.10086](https://arxiv.org/abs/1903.10086)
Arbey et al., [arXiv:1904.08399](https://arxiv.org/abs/1904.08399)
Geng et al., [arXiv:2103.12738](https://arxiv.org/abs/2103.12738)

The very rare $B_s \rightarrow \mu\mu$

- Purely leptonic $B_{(s)} \rightarrow \mu^+\mu^-$ decay

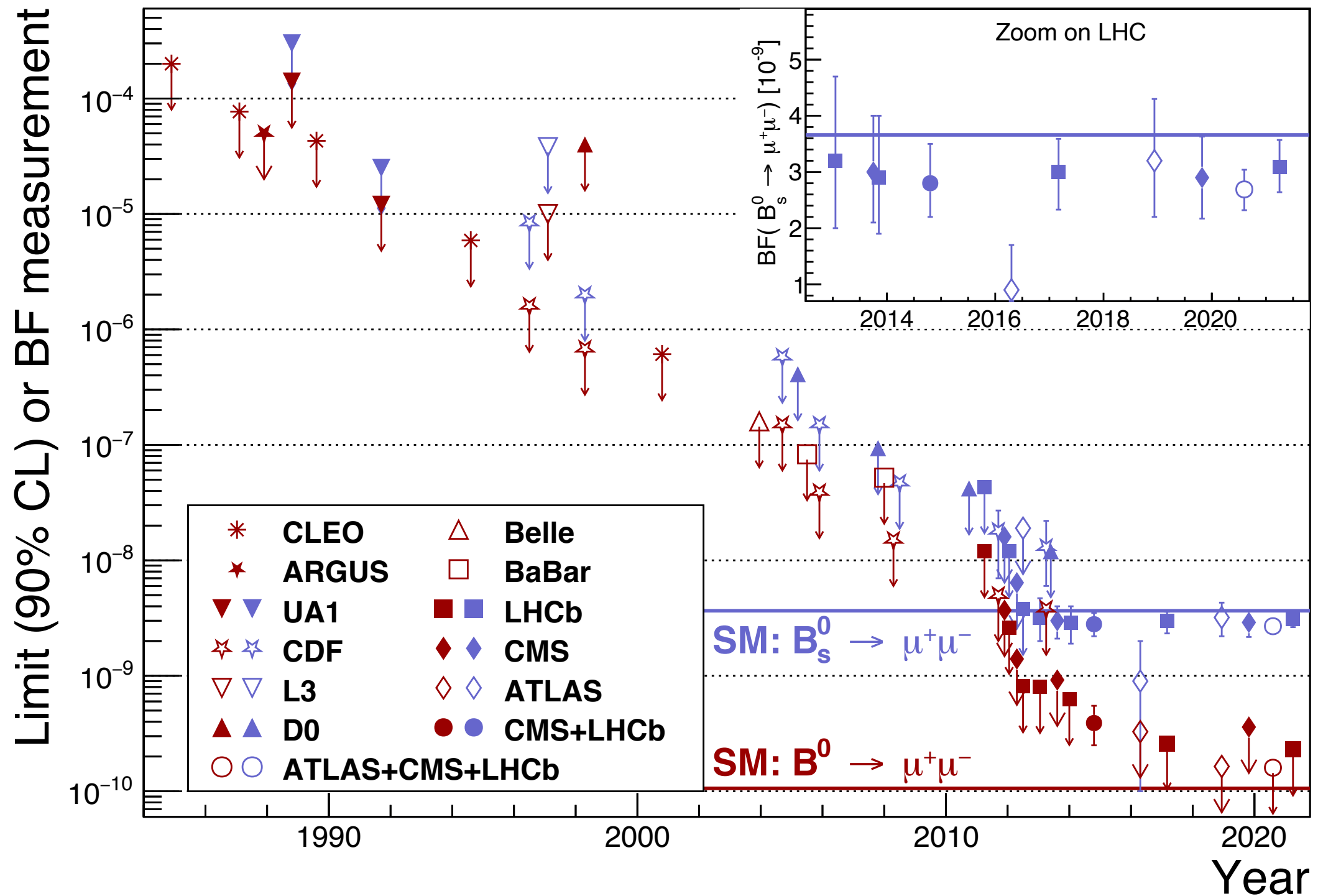
- Same diagrams as $b \rightarrow s\mu\mu$ (spectator quark in initial state)
- More precise predictions because of leptonic final state
- Much smaller BR because of helicity suppression ($B_{(s)}$ pseudoscalar)



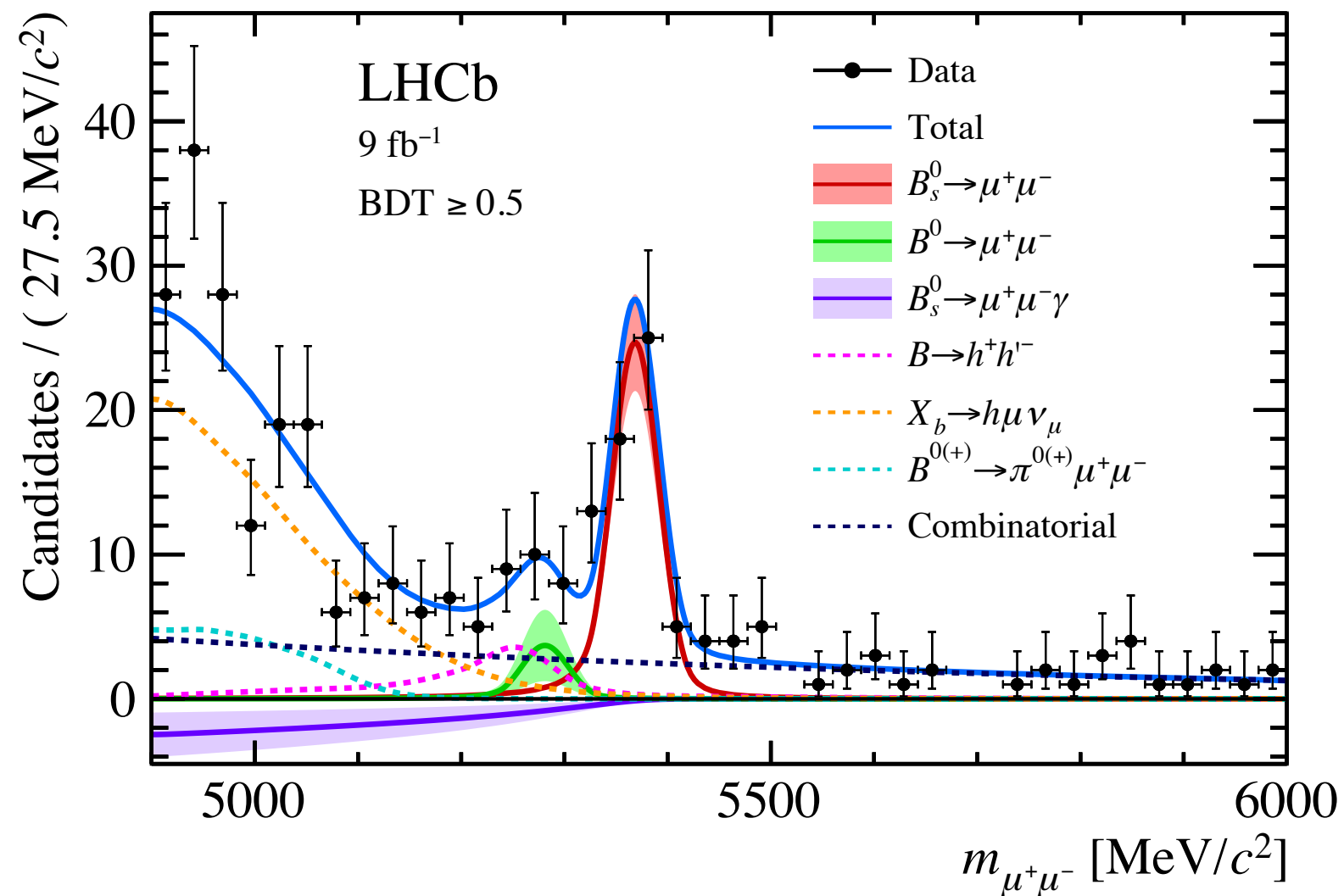
- SM branching fractions prediction:
 $\mathcal{B}(B_s^0 \rightarrow \mu^+\mu^-) = (3.66 \pm 0.14) \times 10^{-9}$
with only 4% uncertainty

The very rare $B_s \rightarrow \mu\mu$

LHCB-PAPER-2021-007



The very rare $B_s \rightarrow \mu\mu$



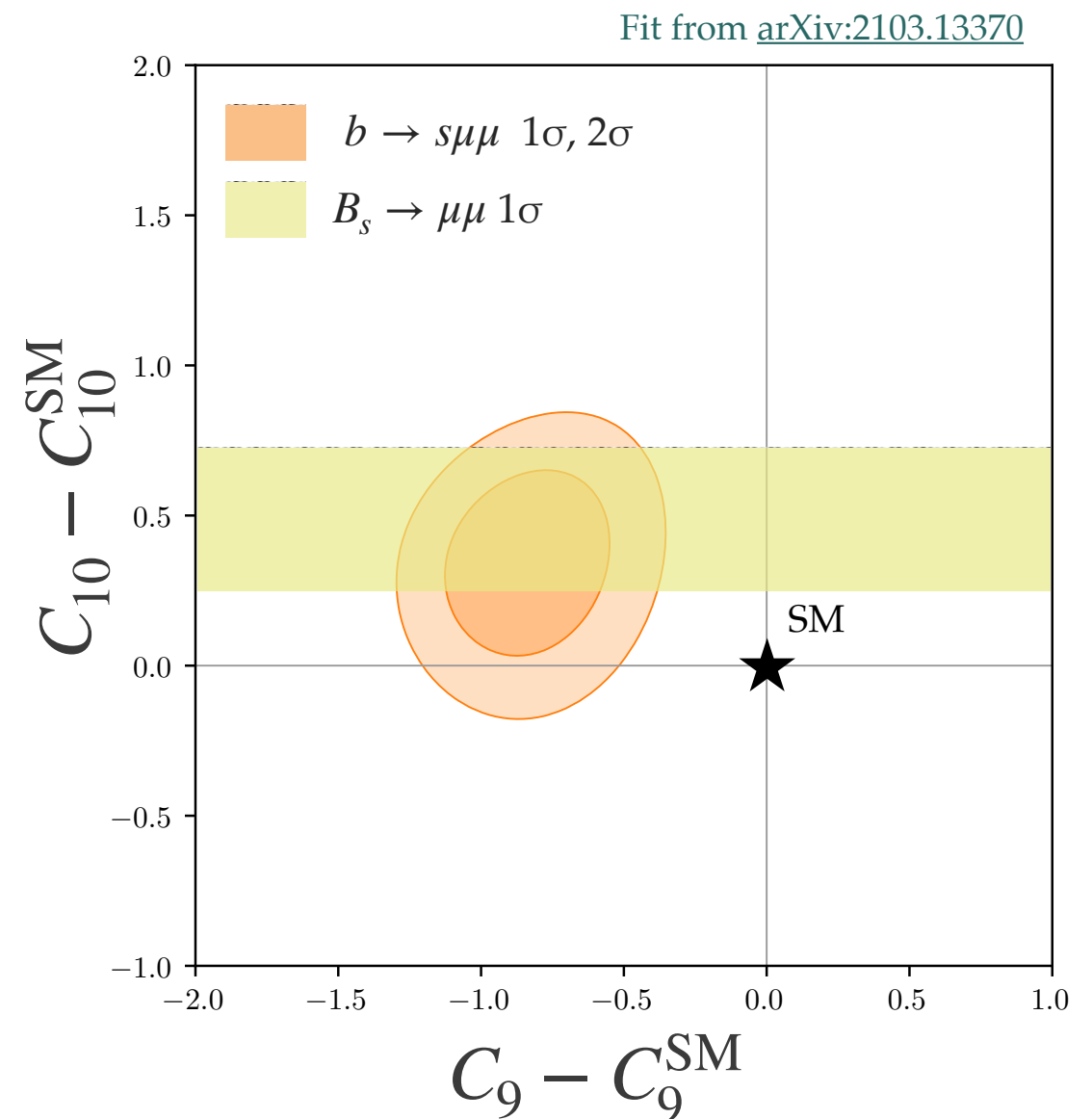
Latest LHCb result

$$BR(B_s^0 \rightarrow \mu^+\mu^-) = (3.09^{+0.46+0.15}_{-0.43-0.11}) \times 10^{-9}$$

16% uncertainty!

Interpretation

- Combining results $B_{(s)} \rightarrow \mu\mu$ results from ATLAS, CMS and LHCb
- Uncertainty on $BR(B_s \rightarrow \mu\mu)$ reduced to about 12%
- Measurement below SM by about 2σ \rightarrow Compatible with C_{10} shift that could explain $b \rightarrow s\mu\mu$!



Tests of Lepton Universality

$b \rightarrow s \ell^+ \ell^-$ tests of LU

- $b \rightarrow s \ell^+ \ell^-$ is lepton universal in the SM
→ can identify LU violating NP contribution

Hiller & Kruger [arXiv:hep-ph/0310219](https://arxiv.org/abs/hep-ph/0310219)

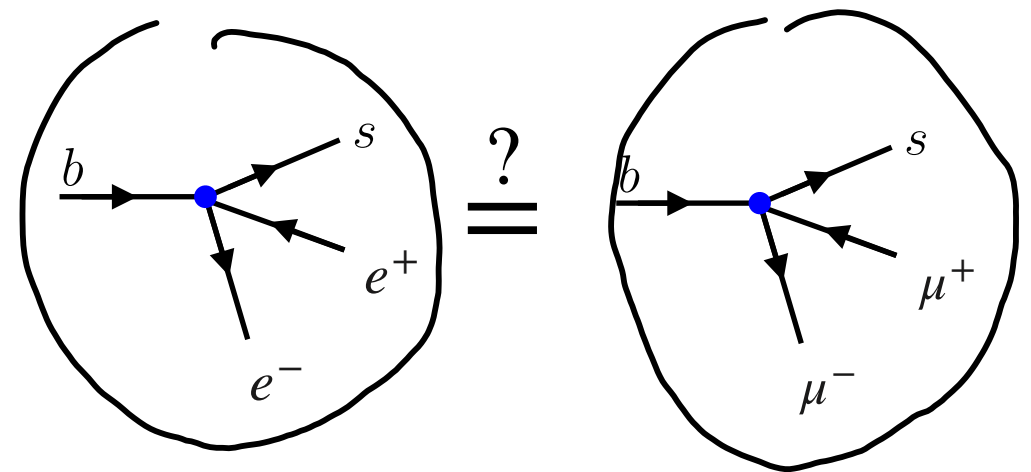
- $b \rightarrow s \tau \tau$ not observed yet → compare μ and e

- Predictions are extremely precise

- QCD uncertainty cancels to 10^{-4}
- Up to $\sim 1\%$ QED corrections

Bordone et al [arXiv:1605.07633](https://arxiv.org/abs/1605.07633)

- Main challenge at LHCb is e/μ differences in the detector response



$$R_H = \frac{\int_{q_{\min}^2}^{q_{\max}^2} \frac{d\mathcal{B}(B \rightarrow H\mu^+\mu^-)}{dq^2} dq^2}{\int_{q_{\min}^2}^{q_{\max}^2} \frac{d\mathcal{B}(B \rightarrow He^+e^-)}{dq^2} dq^2} \stackrel{\text{SM}}{\approx} 1$$

e^+e^- at LHCb: Selection

● Electrons at LHCb:

- Being light, they are produced in a plethora of decay channels
- **Trigger** on large e^\pm/h^\pm energy deposit on calorimeters
- **Electron ID** relies on calorimeter for suppression of π mis-ID
- Large **combinatorial background**: machine-learning based classification using kinematics info and isolation

● Muons trigger and ID is easier

- Selection more efficient

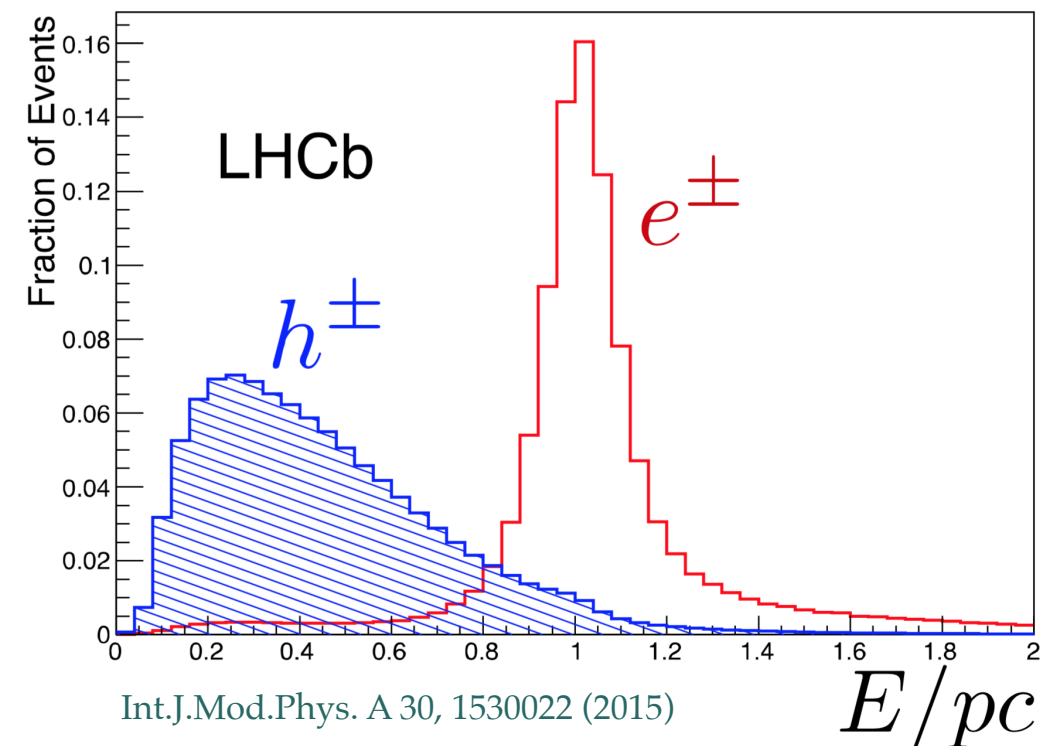
$$\frac{\epsilon(B^+ \rightarrow K^+ \mu^+ \mu^-)}{\epsilon(B^+ \rightarrow K^+ e^+ e^-)} \simeq 3$$

Phys. Rev. Lett. 122 (2019) 191801

Hardware trigger at LHCb:

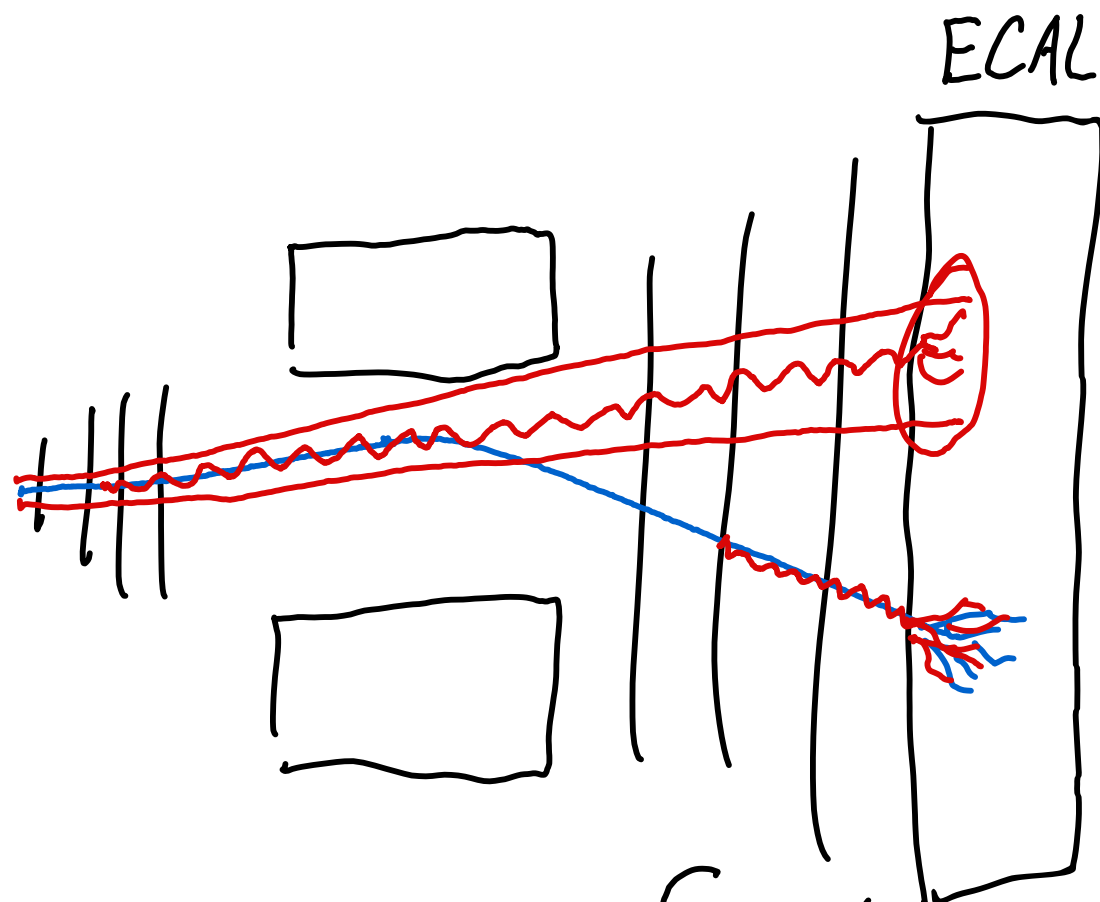
- $p_T(\mu^\pm) > 1.5 - 1.8$ GeV
- $E_T(e^\pm) > 2.5 - 3.0$ GeV

Electron ID at LHCb

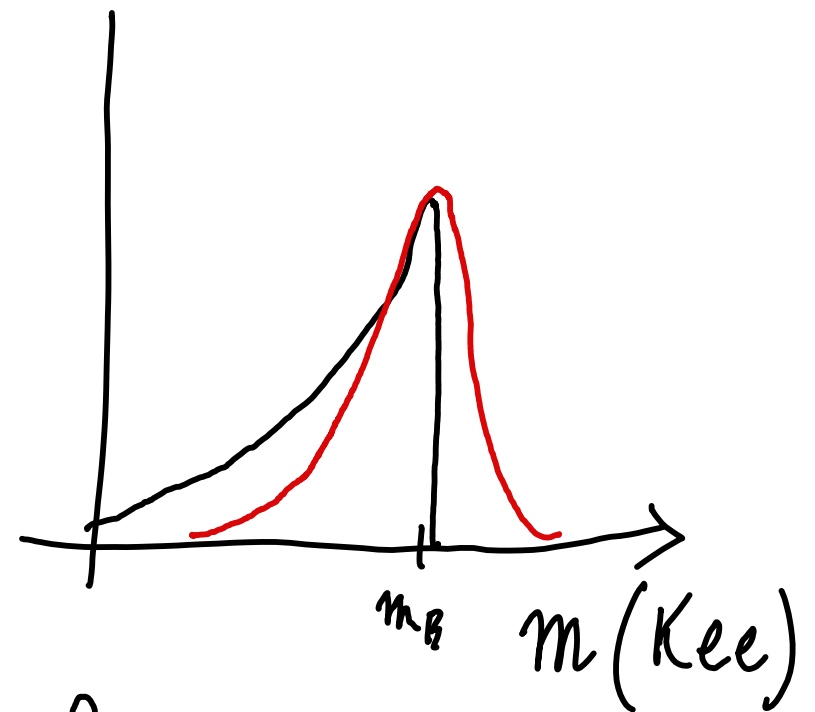


E/pc

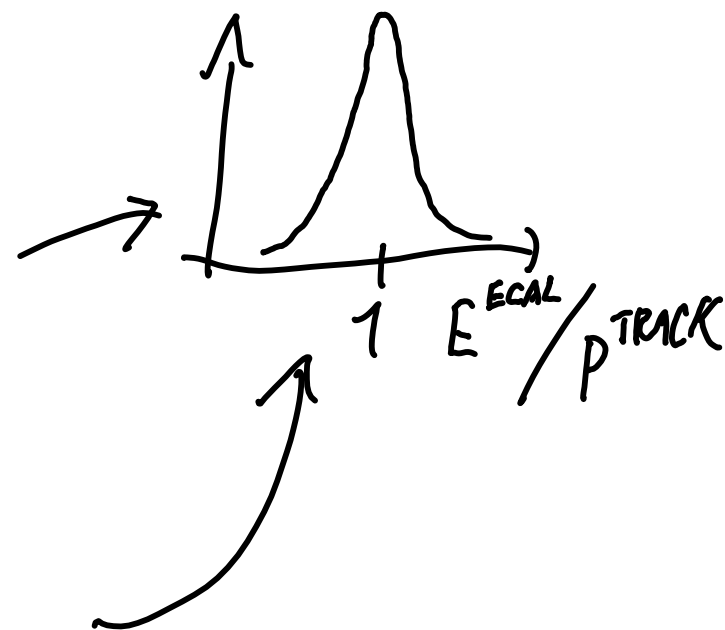
Bremsstrahlung



γ after MAGNET $\left\{ \begin{array}{l} p^{\text{TRACK}} = p^{\text{TRUE}} \\ E^{\text{ECAL}} = p^{\text{TRACK}} \end{array} \right.$
 γ before MAGNET $\left\{ \begin{array}{l} p^{\text{TRACK}} < p^{\text{TRUE}} \\ E^{\text{ECAL}} = p^{\text{TRACK}} \end{array} \right.$

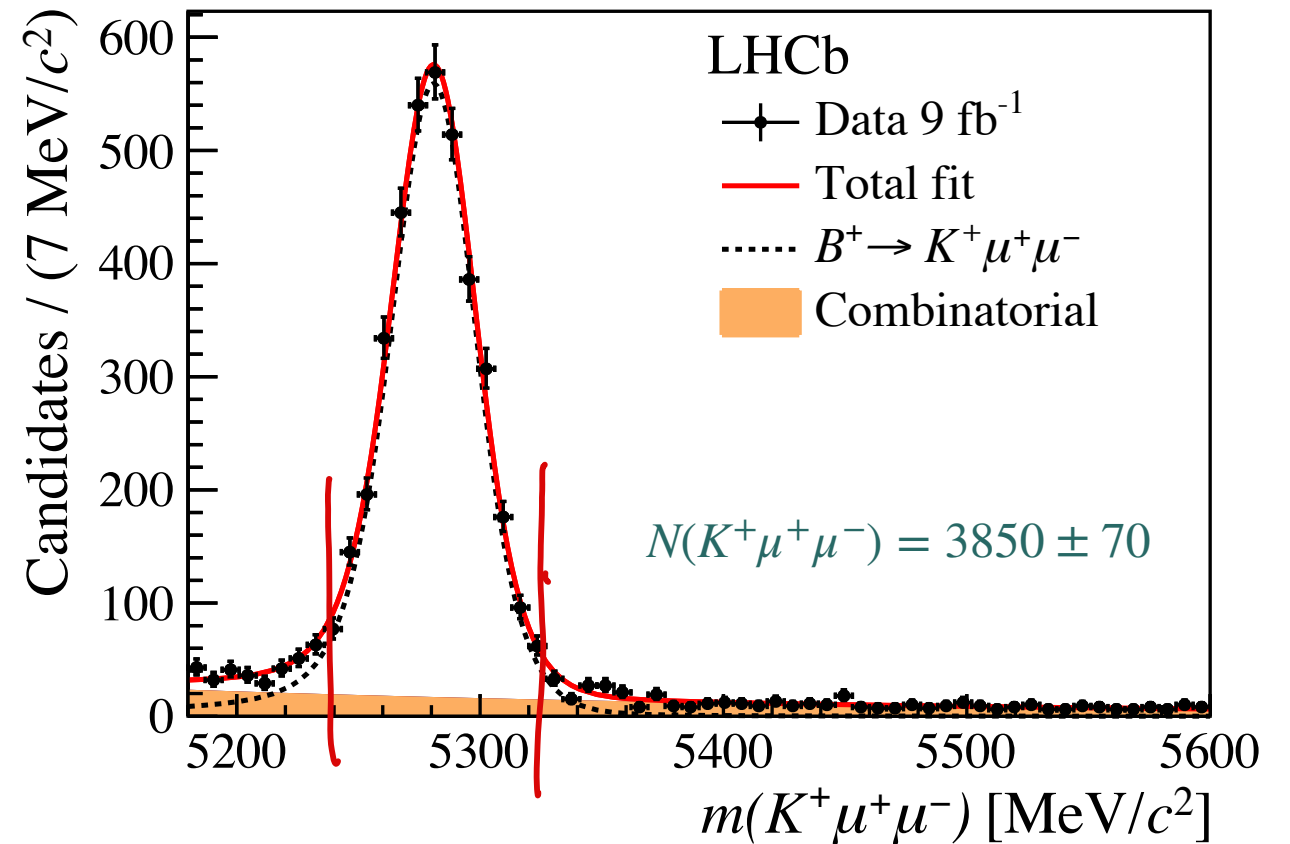
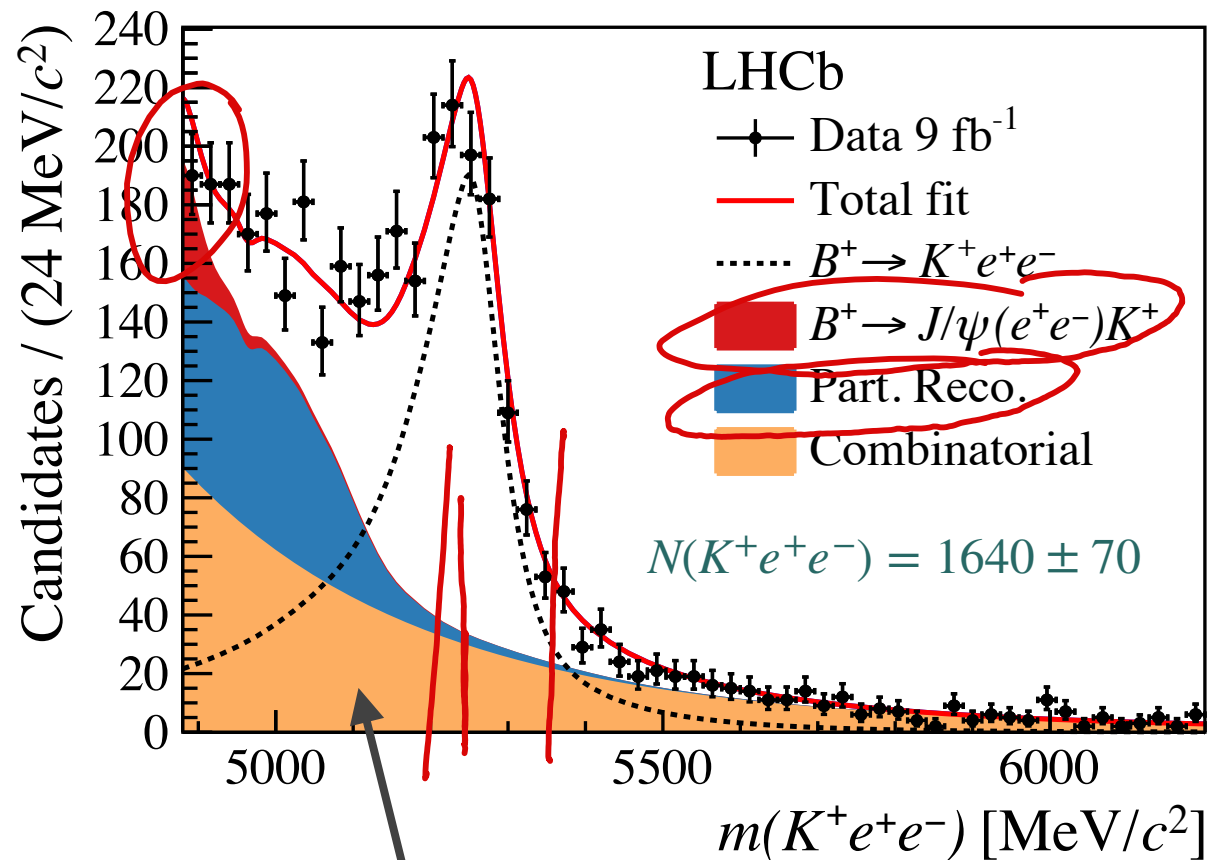


$B \rightarrow K e e$



Mass resolution

LHCb arXiv:2103.11769



- Background with missing pion (Part. Reco.) due to mass resolution
- Combinatorial background is much larger

Backgrounds in electrons

- Particle ID and mass vetoes to suppress peaking bkg

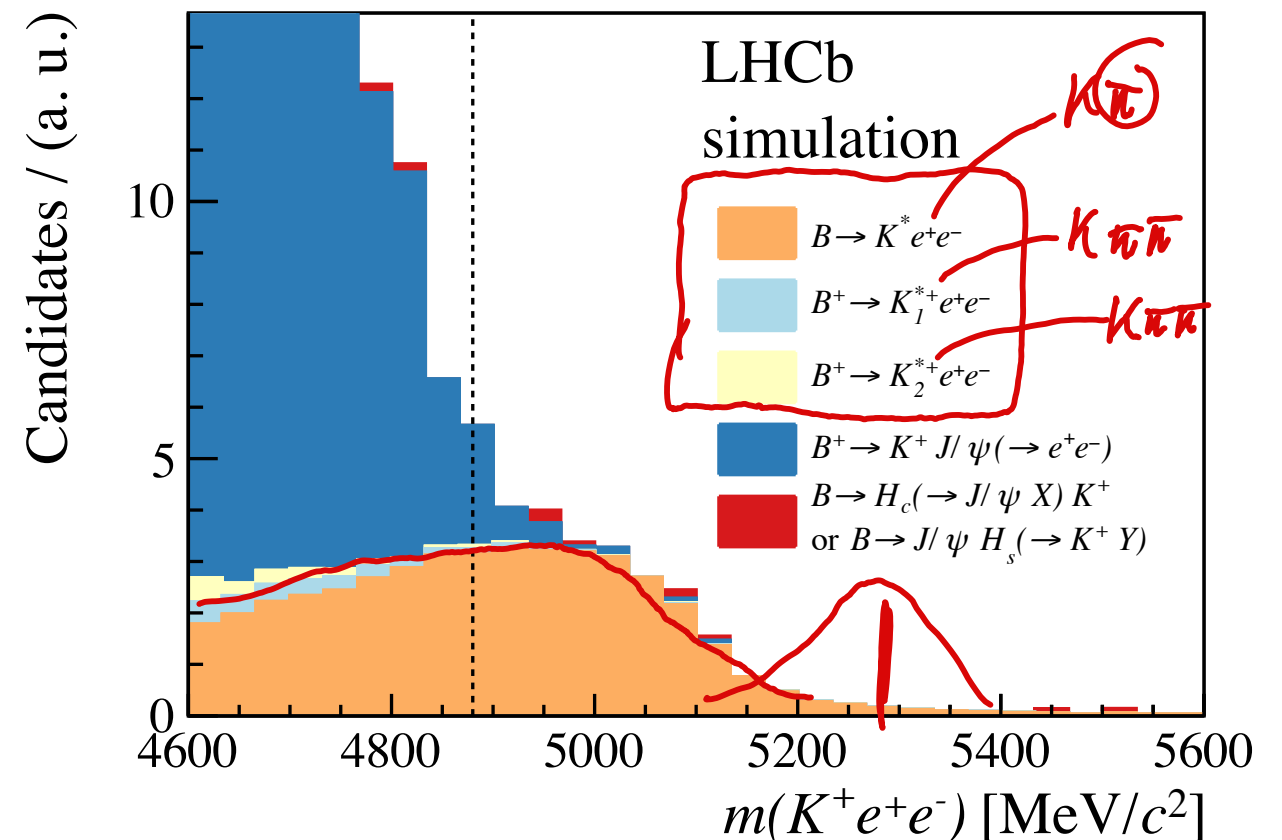
- Remove $B^+ \rightarrow \bar{D}^0(\rightarrow K^+ e^- \nu) e^+ \bar{\nu}$ by requiring $m(K^+ e^-) > m_{D^0}$
- Remove $B^+ \rightarrow K^+ \pi^+ \pi^-$ with electron ID

$P(\pi \rightarrow e) \sim 1\%$
 $P(K\pi\pi \rightarrow Ke\bar{e}) \sim 10^{-4}$

- Reduce combinatorial background with multivariate analysis (Boosted Decision Tree)

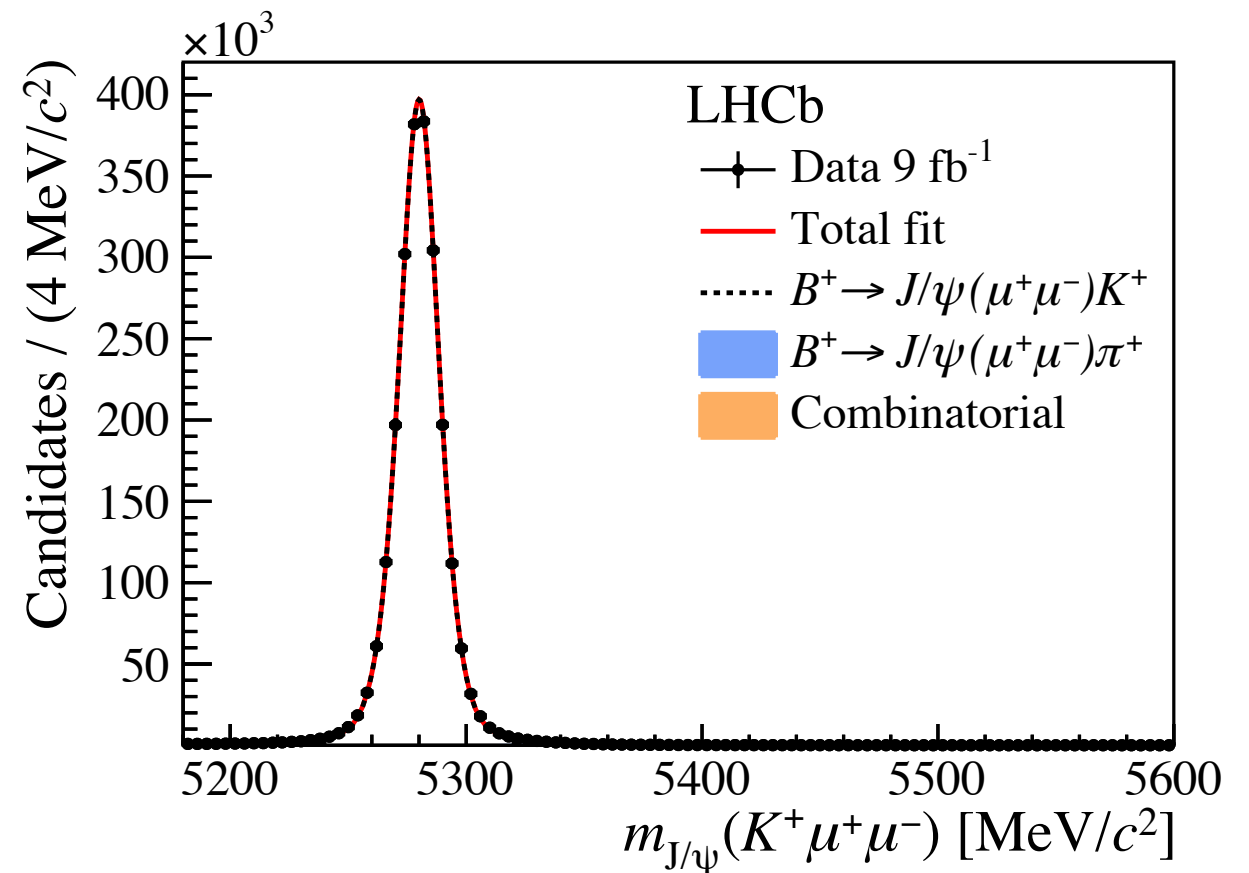
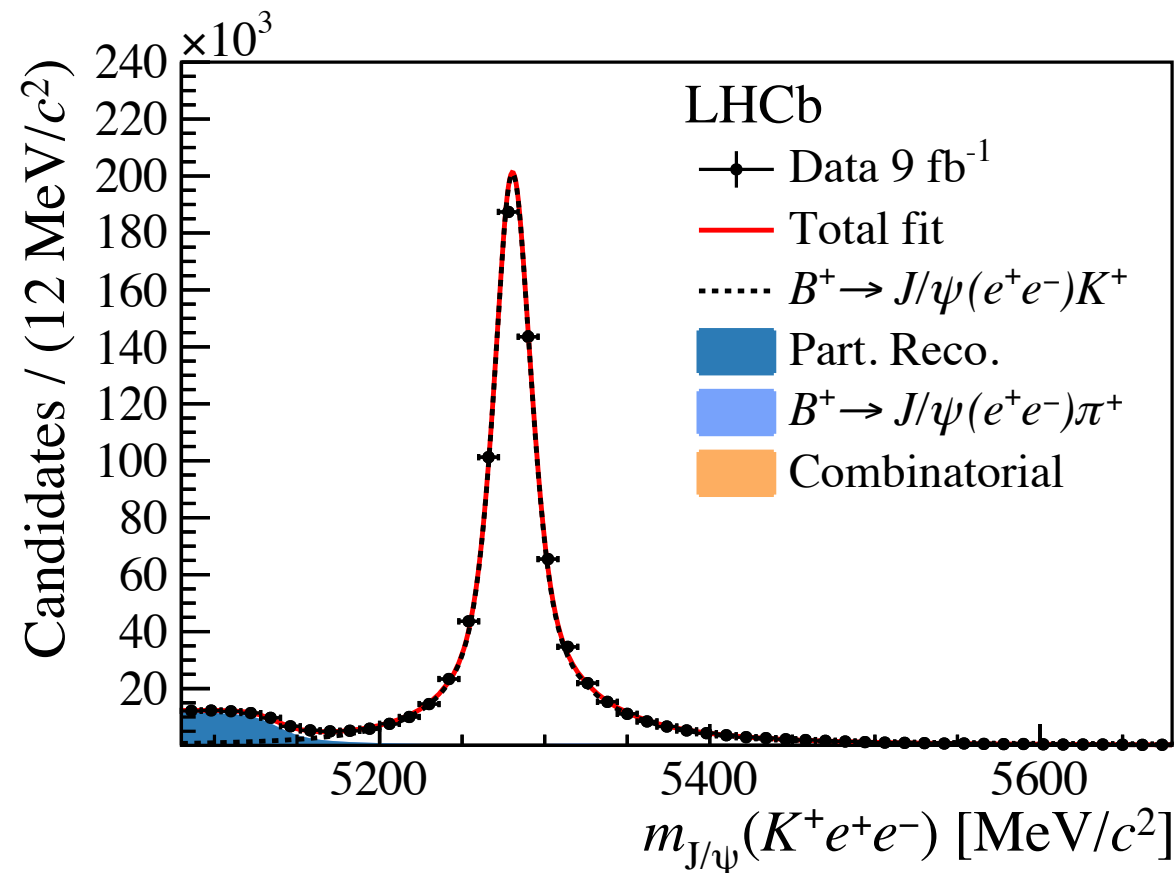
- Choose $m(K^+ e^+ e^-)$ window to suppress other backgrounds
 - Cross-check using control regions and changing $m(K^+ e^+ e^-)$ window

$1.1 < q^2 < 6.0 \text{ GeV}^2$
 $m_{J/\psi}^2 = 9.5 \text{ GeV}^2$



Charmonium control channel

LHCb arXiv:2103.11769



- $B^+ \rightarrow K^+ J/\psi(\ell^+\ell^-)$ decays are known (and expected) to respect LFU at 0.4% level
- Excellent control channel: samples of 750k electrons and 2.3M muons
- Can be isolated from background using J/ψ mass constrain

$$B \rightarrow K J/\psi$$

$$B(J/\psi \rightarrow \mu\mu) \stackrel{L.U.}{=} B(J/\psi \rightarrow ee)$$

Double ratio

$$R_K = \frac{BR(B \rightarrow K \mu \mu)}{BR(B \rightarrow K e e)} \Big|_{q^2 \in [1.1, 6.0] \text{ GeV}^2}$$

$$R_K = \frac{N_S^{\mu\mu}}{N_S^{ee}} \left(\frac{\Sigma_S^{ee}}{\Sigma_S^{\mu\mu}} \right) \sim \frac{1}{3}$$

$$R_{J/\psi} = \frac{BR(B \rightarrow K J/\psi(\mu\mu))}{BR(B \rightarrow K J/\psi(ee))} = 1$$

$$\frac{R_K}{R_{J/\psi}} = \frac{N_S^{\mu\mu}}{N_S^{ee}} \frac{\Sigma_S^{ee}}{\Sigma_S^{\mu\mu}} \cdot \frac{N_N^{ee}}{N_N^{\mu\mu}} \frac{\Sigma_N^{\mu\mu}}{\Sigma_N^{ee}}$$

Double ratio with $\psi(2S)$

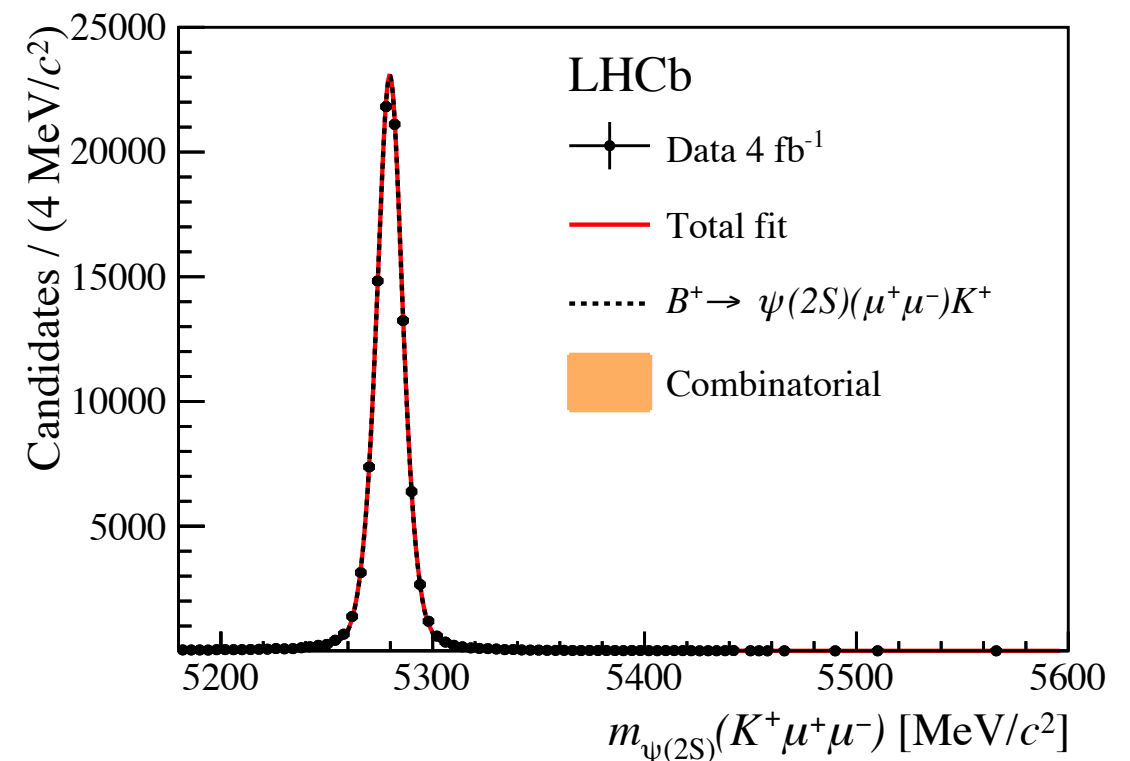
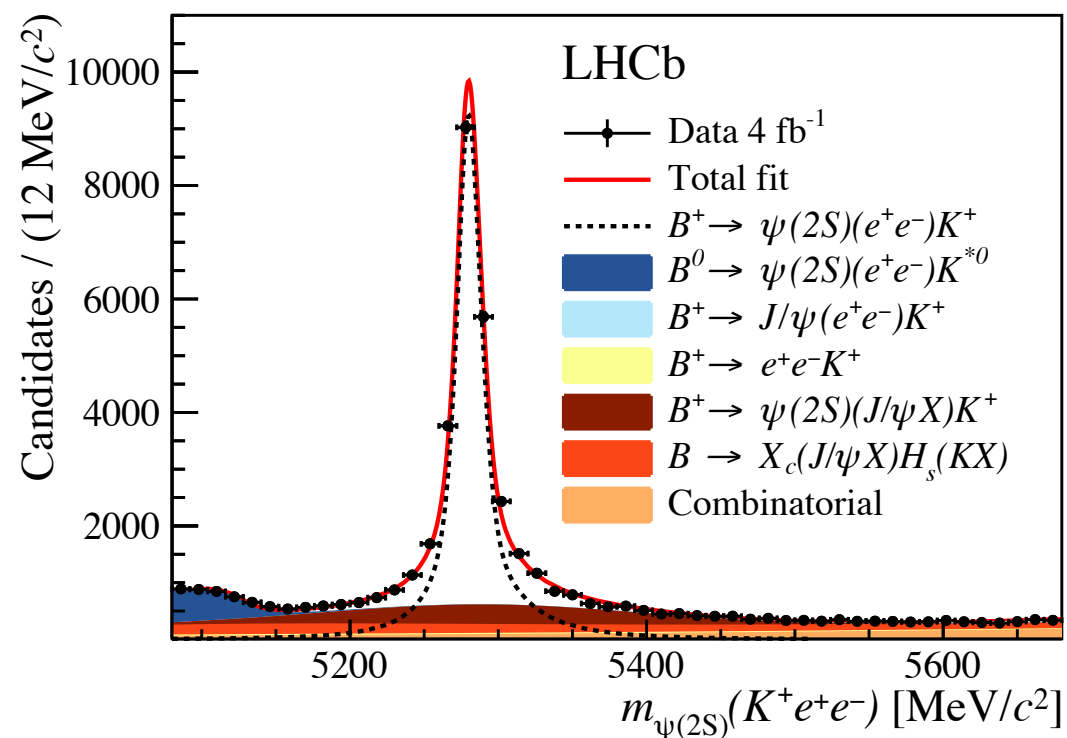
- Can also test that R_K measured at the $\psi(2S)$ is 1

$$R_{\psi(2S)} = \frac{\mathcal{B}(B^+ \rightarrow K^+ \psi(2S)(\mu^+ \mu^-))}{\mathcal{B}(B^+ \rightarrow K^+ J/\psi(\mu^+ \mu^-))} \bigg/ \frac{\mathcal{B}(B^+ \rightarrow K^+ \psi(2S)(e^+ e^-))}{\mathcal{B}(B^+ \rightarrow K^+ J/\psi(e^+ e^-))} = 1$$

- Validation of q^2 dependence of efficiency correction

- Compatible with unity to 1% precision:

$$R_{\psi(2S)} = 0.997 \pm 0.011(\text{stat} + \text{syst})$$



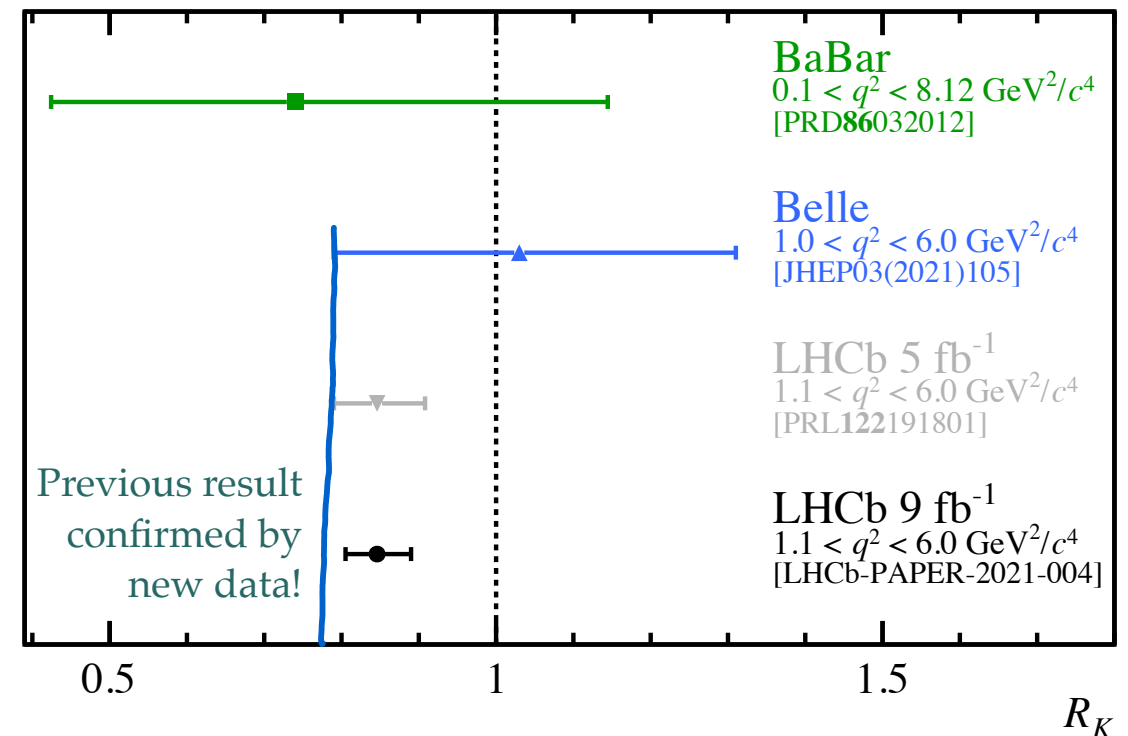
R_K result

LHCb arXiv:2103.11769

- Measured with full dataset
(9/fb at $\sqrt{s}=7, 8$ and 13 TeV)

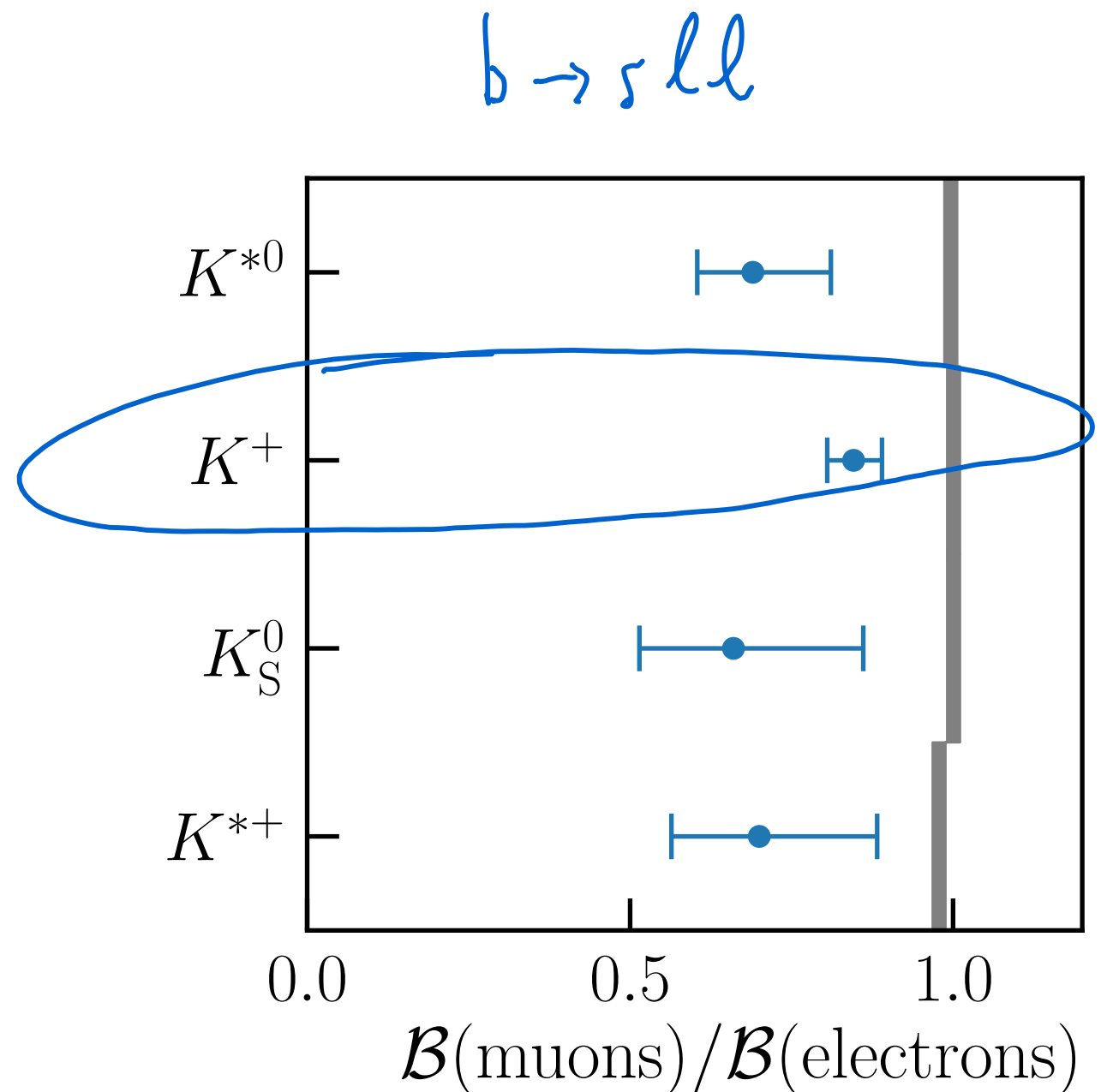
$$R_K = 0.846^{+0.042}_{-0.039}(\text{stat})^{+0.013}_{-0.012}(\text{syst})$$

- Yield of ~ 1640 $B^+ \rightarrow K^+ e^+ e^-$ events
(vs ~ 3850 in $B^+ \rightarrow K^+ \mu^+ \mu^-$) driving
the total uncertainty:
 - 5% statistical error vs 1.5% systematic
- R_K is found to be lower than 1 by
 $\sim 15\%$ with a significance of 3.1σ



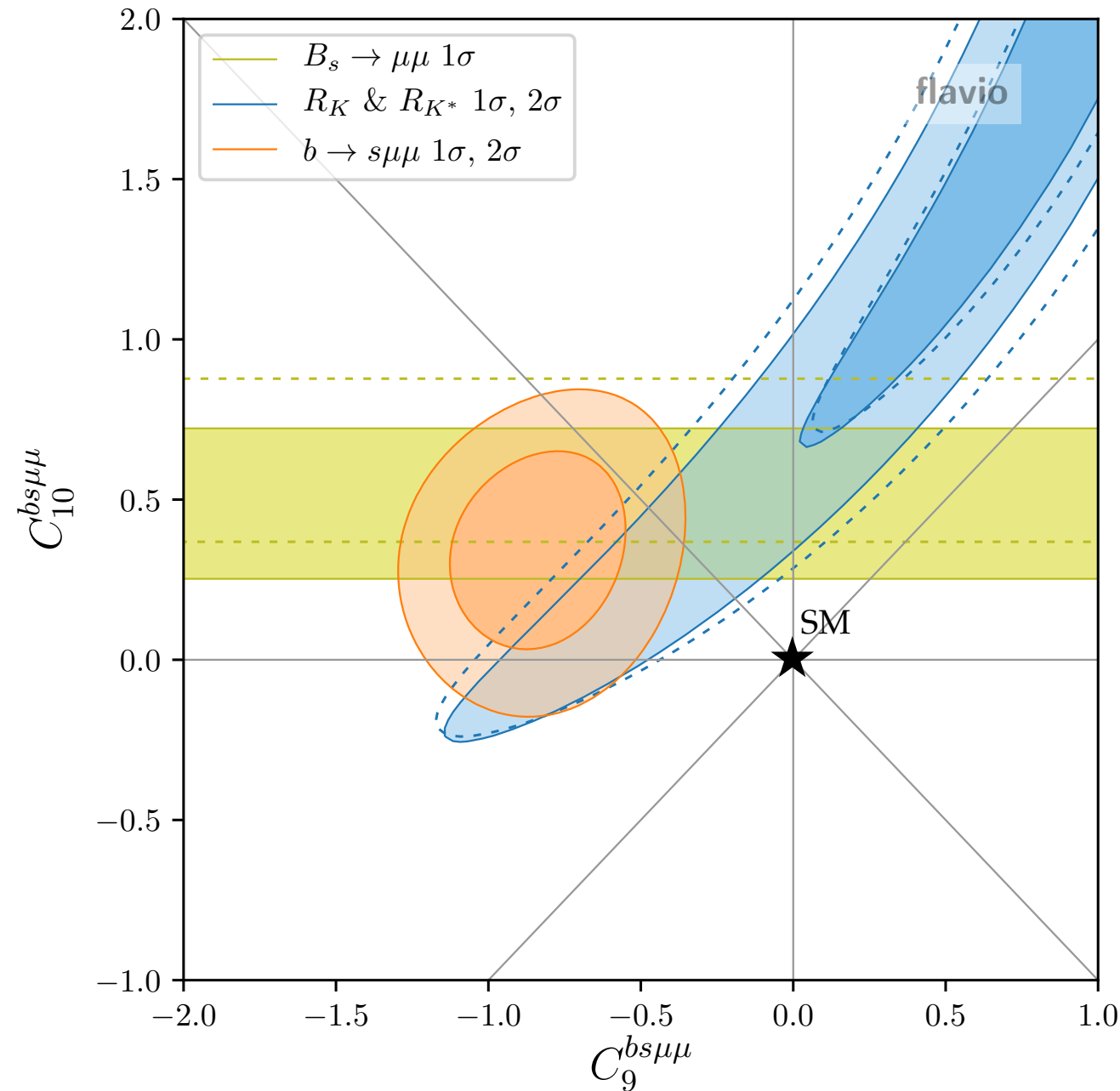
Other LU tests

- Tested LU in other decay channels
- Precision limited, but coherent results
- Combination not trivial (cannot simply average)



Interpretation

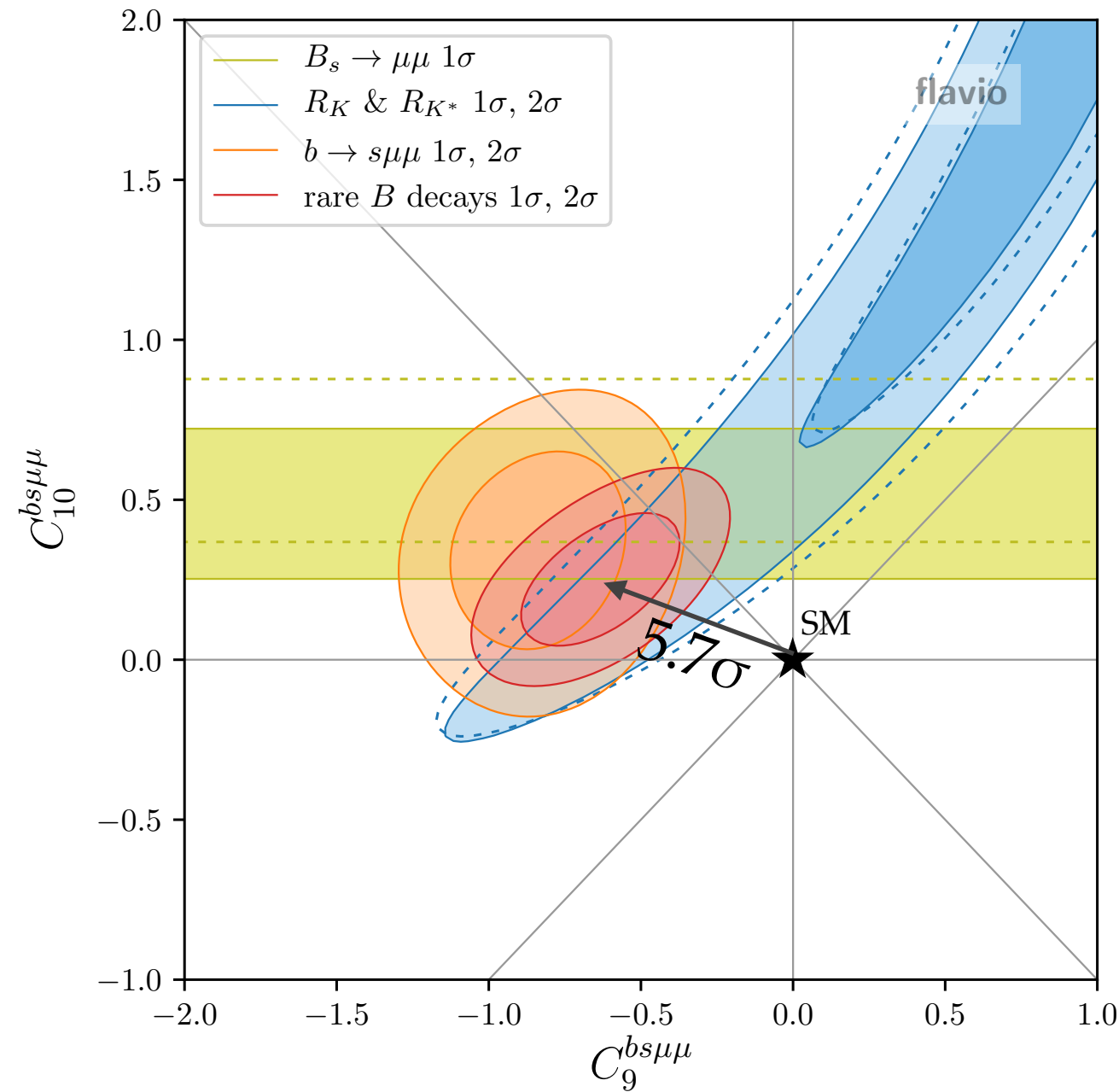
Fit from W. Altmannshofer and P. Stangl [arXiv:2103.13370](https://arxiv.org/abs/2103.13370)



Similar fits from other groups:
Algueró et al., [arXiv:1903.09578](https://arxiv.org/abs/1903.09578)
Kowalska et al., [arXiv:1903.10932](https://arxiv.org/abs/1903.10932)
Ciuchini et al., [arXiv:2011.01212](https://arxiv.org/abs/2011.01212)
Datta et al., [arXiv:1903.10086](https://arxiv.org/abs/1903.10086)
Arbey et al., [arXiv:1904.08399](https://arxiv.org/abs/1904.08399)
Geng et al., [arXiv:2103.12738](https://arxiv.org/abs/2103.12738)

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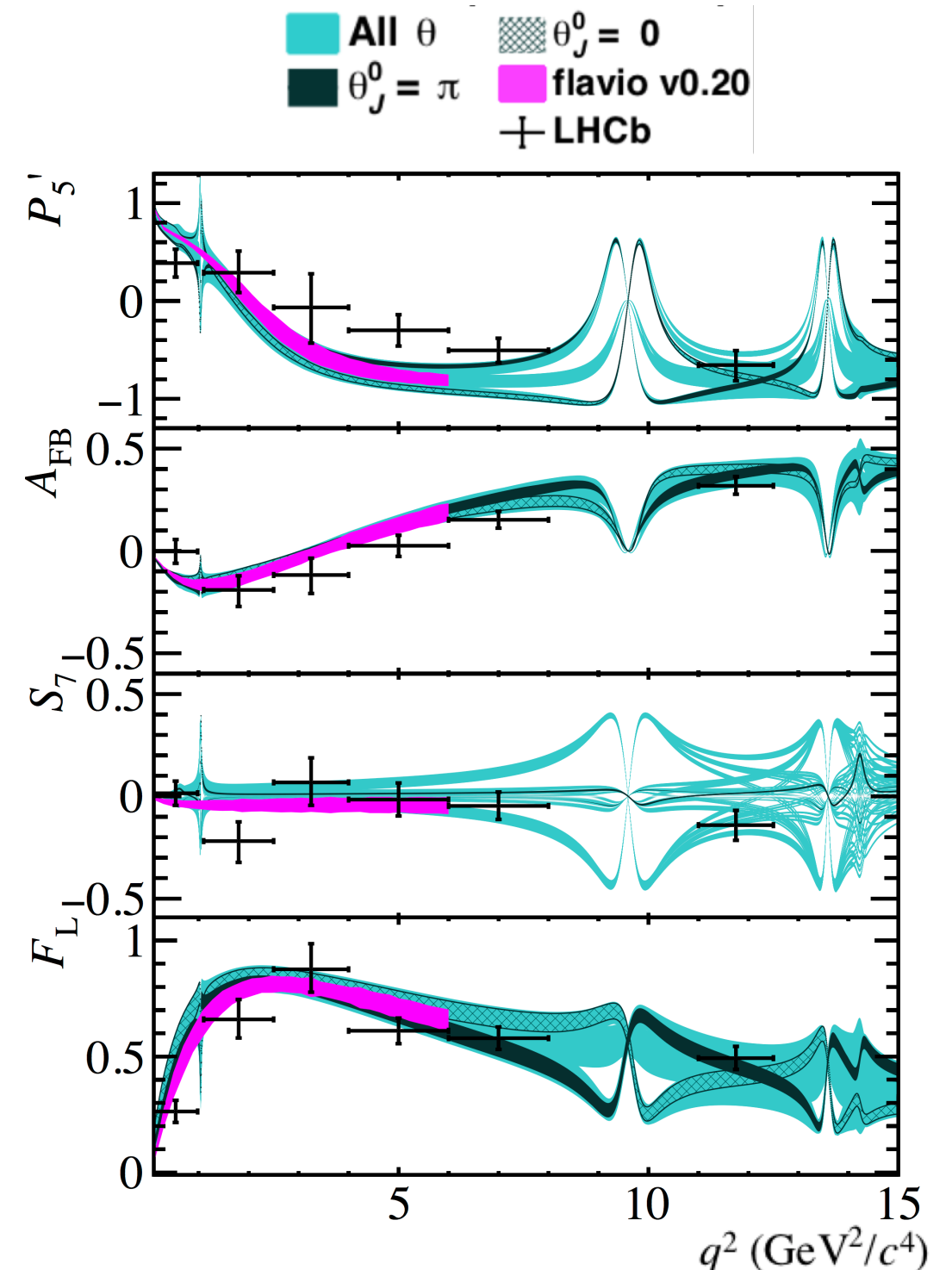
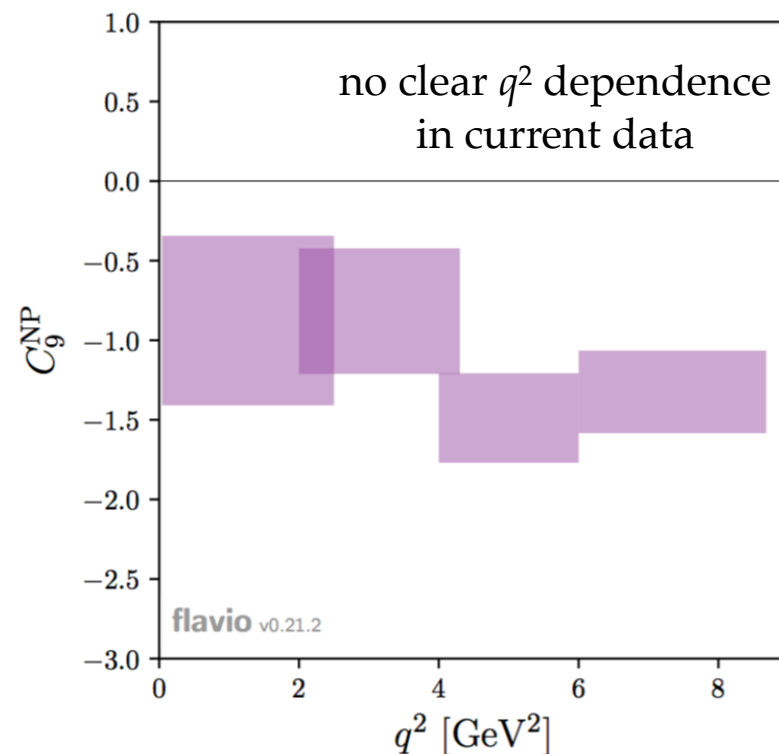


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Backup

A handle on the $c\bar{c}$ loop

- Experimental handles on $c\bar{c}$ loop:
 - NP in C9 would give helicity and q^2 independent effect while hadronic effects **could** be helicity and q^2 dependent
 W.Altmannshofer et al Eur.Phys.J. C77 (2017) no.6, 377
 - Perform full angular analysis of $B \rightarrow K^* \mu \mu$ including $c\bar{c}$ resonances and measure interference phases
 Blake et al., arXiv:1709.03921



$B_s \rightarrow e^+e^-$ and $B_s \rightarrow \tau^+\tau^-$

- Different levels of helicity suppression depending on the lepton mass
- Electrons and taus present additional experimental challenges
- LHCb has search for both and has set upper limits
 $BR(B_s^0 \rightarrow e^+e^-) < 11.2 \times 10^{-9}$ at 95 % CL
 $BR(B_s^0 \rightarrow \tau^+\tau^-) < 6.8 \times 10^{-3}$ at 95 % CL

