

Beyond the cosmological standard model

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In the Ptolemic/Aristotlean standard cosmology (350 BC→1600 AD) the universe was *static* and *finite* and centred on the Earth



This was a *simple* model and fitted all the observational data ... but the underlying principle was un*physical*

Today we have a new 'standard Λ CDM model' of the universe ... dominated by dark energy and undergoing accelerated expansion



It too is 'simple' (counting Λ as one parameter) and fits all the observational data but lacks a *physical* foundation

The standard cosmological model is based on several key assumptions: maximally symmetric space-time + general relativity + ideal fluids





It is thus *natural* for data interpreted in this idealised model to imply that $\Omega_{\Lambda} (\equiv 1 - \Omega_{\rm m} - \Omega_k)$ is non-zero, i.e. Λ is of $O(H_0^2)$... given the inevitable uncertainties in measuring $\Omega_{\rm m}$ and Ω_k and the possibility of other components ($\Omega_{\rm x}$) which are *unaccounted* for in the Hubble equation



This has however been interpreted as evidence for 'vacuum energy'

 $\Rightarrow \rho_{\Lambda} = \Lambda / 8\pi G_{\rm N} \sim H_0^2 M_{\rm p}^2 \sim (10^{-12} \, {\rm GeV})^4$

The Standard $SU(3)_c \ge SU(2)_L \ge U(1)_Y$ 'Model' (viewed as an effective field theory up to some high energy cut-off scale M) describes *all* of microphysics

$$+\underbrace{M^{4}}_{Vacuum energy Higgs mass correction} \xrightarrow{\mu^{2}}{16\pi^{2}} \int_{0}^{M^{2}} dk^{2} = \frac{h_{t}^{2}}{16\pi^{2}} M^{2} \qquad \text{super-renormalisable} \\ \mathcal{L}_{eff} = F^{2} + \bar{\Psi} \not{D} \Psi + \bar{\Psi} \Psi \Phi + (D\Phi)^{2} + V(\Phi) \qquad \text{renormalisable} \\ + \underbrace{\bar{\Psi} \Psi \Phi \Phi}_{Neutrino mass} + \underbrace{\bar{\Psi} \Psi \bar{\Psi} \Psi}_{\text{proton decay, FCNC ...}} + \cdots \qquad \text{non-renormalisable}$$

New physics beyond the SM \Rightarrow non-renormalisable operators suppressed by M^n which *decouple* as $M \rightarrow M_P$... so neutrino mass is naturally small, proton decay is very slow *etc*

But as M is raised, the effects of the super-renormalisable operators are exacerbated (One solution for Higgs mass divergence \rightarrow 'softly broken' supersymmetry at O(TeV)... or the Higgs could be *composite* – a pseudo Nambu-Goldstone boson)

1st SR term couples to gravity so the *natural* expectation is $\rho_{\Lambda} \sim (1 \text{ TeV})^4 \Rightarrow 10^{60} \text{ x} (1 \text{ meV})^4$... i.e. the universe should have been inflating since (or collapsed at): $t \sim 10^{-12}$ s after BB **There must be a good reason why this did** *not* happen!

"Also, as is obvious from experience, the [zero_point energy] does not produce any gravitational field" – Wolfgang Pauli Die allgemeinen Prinzipien der Wellenmechanik, Handbuch der Physik, Vol. XXIV, 1933

1998: Distant SNIa appear fainter than expected for "standard candles" in a decelerating universe ... interpreted as \Rightarrow accelerated expansion below $z \sim 0.5$



Type la Supernovae

The observations are made at *one* instant (the redshift is taken as a proxy for time) so this is not a *direct* measurement of acceleration, nevertheless it is presently more direct than all other 'evidence'



Expansion History of the Universe



Assuming the sum rule, complementary observations implied: $\Omega_{\Lambda} \sim 0.7$, $\Omega_{\rm m} \sim 0.3$



Estimates of Ω_m are rather uncertain ... moreover there is *no* measurement of Ω_Λ *alone*

CMB data indicate $\Omega_k \approx 0$ so the FRW model is simplified further, leaving only two free parameters (Ω_Λ and Ω_m) to be fitted to data



But e.g. if we underestimate Ω_m , or if there is a $\Omega_x \implies a \text{ new component}$ which the FRW model does *not* include, then we will *incorrectly* infer $\Omega_{\Lambda} \neq 0$



This is what our universe actually looks like ... locally (out to ~300 Mpc) and on larger (SDSS) scales Is it justified to approximate it as *exactly* homogeneous? ... To assume that we are a *'typical'* observer? ... To assume that all observed directions are *equivalent*?



Could dark energy be an artifact of approximating the universe as homogeneous?

Quantities averaged over a domain \mathcal{D} obey modified Friedmann equations Buchert 1999:

$$\begin{split} 3\frac{\ddot{a}_{\mathcal{D}}}{a_{\mathcal{D}}} &= -4\pi G \langle \rho \rangle_{\mathcal{D}} + \mathcal{Q}_{\mathcal{D}} ,\\ 3\left(\frac{\dot{a}_{\mathcal{D}}}{a_{\mathcal{D}}}\right)^2 &= 8\pi G \langle \rho \rangle_{\mathcal{D}} - \frac{1}{2} \langle^{(3)}R \rangle_{\mathcal{D}} - \frac{1}{2} \mathcal{Q}_{\mathcal{D}} , \end{split}$$

where $\mathcal{Q}_{\mathcal{D}}$ is the backreaction term,

$$\mathcal{Q}_{\mathcal{D}} = rac{2}{3} (\langle heta^2
angle_{\mathcal{D}} - \langle heta
angle_{\mathcal{D}}^2) - \langle \sigma^{\mu
u} \sigma_{\mu
u}
angle_{\mathcal{D}} \;.$$

Variance of the expansion rate.

Average shear.

If $Q_D > 4\pi G \langle \rho \rangle_D$ then a_D accelerates.

Can mimic a cosmological constant if $Q_D = -\frac{1}{3} \langle {}^{(3)}R \rangle_D = \Lambda_{\text{eff}}$.

Whether the backreaction can be sufficiently large is still an open question



Due to structure formation, the homogeneous solution of Einstein's equations is distorted - its average must be taken over the *actual* geometry



Courtesy: Thomas Buchert

'Back reaction' is hard to compute because spatial averaging and time evolution (along our past light cone) do *not* commute

Relativistic numerical simulations of structure formation have just begun to be performed ... and indicate significant backreaction effects

Interpreting Λ as vacuum energy raises the coincidence problem: why is $\Omega_\Lambda {\approx} \, \Omega_m \,$ today?

An evolving ultralight scalar field ('quintessence') can display 'tracking' behaviour: this requires $V(\varphi)^{1/4} \sim 10^{-12}$ GeV but $\sqrt{d^2 V/d\varphi^2} \sim H_0 \sim 10^{-42}$ GeV to ensure slow_roll ... i.e. just as much fine_tuning as a bare cosmological constant

A similar comment applies to models (e.g. 'DGP brane_world') wherein gravity is modified on the scale of the present Hubble radius $1/H_0$ so as to mimic vacuum energy ... this scale is *absent* in a fundamental theory and is just put in by hand

(similar fine-tuning in every proposal – e.g. massive gravity, chameleon fields, ...)

The only natural option is if $\Lambda \sim H^2$ always, but this is just a renormalisation of G_N ! (recall: $H^2 = 8\pi G_N/3 + \Lambda/3) \rightarrow$ ruled out by Big Bang nucleosynthesis (requires G_N to be within 5% of lab value) ... in any case this will *not* yield accelerated expansion

Thus there can be no physical explanation for the coincidence problem

Do we infer $\Lambda \sim H_0^2$ because that is just the observational sensitivity (in the FRW cosmology framework) ... just how strong is the evidence for accelerated expansion?



The 2015 Breakthrough Prize in Fundamental Physics "for the most unexpected discovery that the expansion of the universe is accelerating"









They are certainly not 'standard candles'



But they can be 'standardised' using the observed correlation between their peak magnitude and light_curve width (NB: this is *not* understood theoretically)



The scatter is thus reduced from a factor of ~10 to a factor of ~2 (NB: This requires observing the rise of the light curve *before* the SN peaks!)

Spectral Adaptive Lightcurve Template

(For making 'stretch' and 'colour' corrections to the observed lightcurves)

$$\mu_B = m_B^* - M + \alpha X_1 - \beta \mathcal{C}$$

B-band

SALT 2 parameters

Betoule et al., arXiv:1401.4064

Name	Zcmb	m_B^{\star}	X_1	С	$M_{ m stellar}$?
03D1ar	0.002	23.941 ± 0.033	-0.945 ± 0.209	0.266 ± 0.035	10.1 ± 0.5	?
03D1au	0.503	23.002 ± 0.088	1.273 ± 0.150	-0.012 ± 0.030	9.5 ± 0.1	?
03D1aw	0.581	23.574 ± 0.090	0.974 ± 0.274	-0.025 ± 0.037	9.2 ± 0.1	?
03D1ax	0.495	22.960 ± 0.088	-0.729 ± 0.102	-0.100 ± 0.030	11.6 ± 0.1	?
03D1bp	0.346	22.398 ± 0.087	-1.155 ± 0.113	-0.041 ± 0.027	10.8 ± 0.1	?
03D1co	0.678	24.078 ± 0.098	0.619 ± 0.404	-0.039 ± 0.067	8.6 ± 0.3	?
03D1dt	0.611	23.285 ± 0.093	-1.162 ± 1.641	-0.095 ± 0.050	9.7 ± 0.1	
03D1ew	0.866	24.354 ± 0.106	0.376 ± 0.348	-0.063 ± 0.068	8.5 ± 0.8	
03D1fc	0.331	21.861 ± 0.086	0.650 ± 0.119	-0.018 ± 0.024	10.4 ± 0.0	
03D1fq	0.799	24.510 ± 0.102	-1.057 ± 0.407	-0.056 ± 0.065	10.7 ± 0.1	
03D3aw	0.450	22.667 ± 0.092	0.810 ± 0.232	-0.086 ± 0.038	10.7 ± 0.0	
03D3ay	0.371	22.273 ± 0.091	0.570 ± 0.198	-0.054 ± 0.033	10.2 ± 0.1	
03D3ba	0.292	21.961 ± 0.093	0.761 ± 0.173	0.116 ± 0.035	10.2 ± 0.1	
03D3bl	0.356	22.927 ± 0.087	0.056 ± 0.193	0.205 ± 0.030	10.8 ± 0.1	

There may well be other variables that the magnitude correlates with ...

Cosmology

$$\mu \equiv 25 + 5 \log_{10}(d_{\rm L}/{\rm Mpc}), \text{ where:}$$

$$d_{\rm L} = (1+z) \frac{d_{\rm H}}{\sqrt{\Omega_k}} \sin\left(\sqrt{\Omega_k} \int_0^z \frac{H_0 dz'}{H(z')}\right),$$

$$d_{\rm H} = c/H_0, \quad H_0 \equiv 100h \text{ km s}^{-1} \text{Mpc}^{-1},$$

$$H = H_0 \sqrt{\Omega_{\rm m}(1+z)^3 + \Omega_k(1+z)^2 + \Omega_\Lambda},$$

$$\sinh \phi \sin \alpha_k > 0 \text{ and } \sin \phi \sin \phi \cos \alpha_k < 0$$

$$\mu_{\mathcal{C}} = m - M = -2.5 \log \frac{F/F_{\rm ref}}{L/L_{\rm ref}} = 5 \log \frac{d_L}{10 \, \mu_C}$$

What is measured?

Distance modulus

Redshift z and apparent magnitude (at maximum) m_B^* ... then fit to SALT-2 template

$$\mu_B = m_B^* - M + \alpha X_1 - \beta \mathcal{C}$$

How strong is the evidence for cosmic acceleration?



But they *adjust* σ_{int} to get χ^2 of 1/d. σ . f. for the fit to the *assumed* Λ CDM model!

Joint Lightcurve Analysis data (740 SNe) Betoule et al, arXiv:1401.4064



This page contains links to data associated with the SDSS-II/SNLS3 Joint Light-Curve Analysis (Betoule et al. 2014, submitted to A&A).

The release consists in:

VA /1.ma 301 41.

1. Release history V1 (January 2014, paper submitted): V2 (March 2014): V3 (April 2014, pape accepted): V4 (June 2014): V5 (March 2015): V6 (March 2015):	 The end products of the analysis and a C++ code to compute the likelihood of this data associated to a cosmological model. The code enables both evaluations of the <i>complete</i> likelihood, and <i>fast</i> evaluations of an <i>approximate</i> likelihood (see Betule et al. 2014, Appendix E). The version 2.4 of the SALT2 light-curve model used for the analysis plus 200 random realizations usable for the propogation of model uncertainties. The exact set of Supernovae light-curves used in the analysis. We also deliver presentation material. Since March 2014, the JLA likelihood plugin is included in the official release of cosmomc. For older versions, the plugin is still available (see below: <i>Installation of the cosmom plugin</i>).
 Installation of the C likelihood code 	** To analyze the JLA sample with SNANA, see \$SNDATA_ROOT/sample_input_files/JLA2014/AAA_README.
Installation of the cosmome plugin	1 Release history
3. SALT2 model 4. Error propagation	V1 (January 2014, paper submitted):
Error decomposition SALT2 light-curve m	First arxiv version. del
uncertainbes	viz (march 2014);
	V3 (April 2014, paper accepted):

Same as v2 with the addition of a C++ likelihood code in an independant archive (jla_likelihood_v3.tgz).

Data *publicly* available

http://supernovae.in2p3.fr/sdss_snls_jla/ ... has been *corrected* for Malmqvist bias

We use *exactly* the same dataset but apply a *principled* statistical analysis Nielsen *et al*, arXiv:1506.01354

Construct a Maximum Likelihood Estimator

$$\begin{aligned} \mathcal{L} &= \text{probability density(data|model)} \\ \mathcal{L} &= p[(\hat{m}_B^*, \hat{x}_1, \hat{c}) | \theta] \\ &= \int p[(\hat{m}_B^*, \hat{x}_1, \hat{c}) | (M, x_1, c), \theta_{\text{cosmo}}] \quad \text{Cosmological model} \\ &\times p[(M, x_1, c) | \theta_{\text{SN}}] dM dx_1 dc \qquad \text{Supernova model} \end{aligned}$$

/ -





$$p[(M, x_1, c)|\theta] = p(M|\theta)p(x_1|\theta)p(c|\theta),$$

$$p(M|\theta) = \frac{1}{\sqrt{2\pi\sigma_M^2}} \exp\left(-\left[\frac{M-M_0}{\sigma_{M0}}\right]^2/2\right)$$

$$p(x_1|\theta) = \frac{1}{\sqrt{2\pi\sigma_{x0}^2}} \exp\left(-\left[\frac{x_1 - x_{10}}{\sigma_{x0}}\right]^2/2\right)$$

$$p(c|\theta) = \frac{1}{\sqrt{2\pi\sigma_{c0}^2}} \exp\left(-\left[\frac{c-c_0}{\sigma_{c0}}\right]^2/2\right)$$

Nielsen, Guffanti & Sarkar, arXiv:1506.01354

Likelihood

$$p(Y|\theta) = \frac{1}{\sqrt{|2\pi\Sigma_l|}} \exp\left[-\frac{1}{2}(Y-Y_0)\Sigma_l^{-1}(Y-Y_0)^{\mathrm{T}}\right]$$

$$p(\hat{X}|X,\theta) = \frac{1}{\sqrt{|2\pi\Sigma_d|}} \exp\left[-\frac{1}{2}(\hat{X}-X)\Sigma_d^{-1}(\hat{X}-X)^{\mathrm{T}}\right]$$

$$\mathcal{L} = \frac{1}{\sqrt{|2\pi(\Sigma_d + A^{\mathrm{T}}\Sigma_l A)|}} \begin{array}{c} \text{intrinsic} \\ \text{distributions} \\ \times \exp\left(-\frac{1}{2}(\hat{Z}-Y_0 A)(\Sigma_d + A^{\mathrm{T}}\Sigma_l A)^{-1}(\hat{Z}-Y_0 A)^{\mathrm{T}}\right) \\ \text{cosmology} \end{array}$$
SALT2

Confidence regions Nielsen, Guffanti & Sarkar, <u>arXiv:1506.01354</u>

$$p_{\text{cov}} = \int_{0}^{-2\log \mathcal{L}/\mathcal{L}_{\text{max}}} \chi^{2}(x;\nu) dx$$
$$\mathcal{L}_{p}(\theta) = \max_{\phi} \mathcal{L}(\theta,\phi)$$

1,2,3-sigma

solve for Likelihood value

Data consistent with *uniform* expansion rate $@ < 3\sigma!$



Our result has been confirmed by a subsequent Bayesian analysis



... much more computationally intensive (MCMC scan) hence contours are ragged

Epilogue

Rubin & Hayden (arXiv:1610.08972) say that our model for the distribution of the light curve fit parameters should have included a dependence on redshift (to allow for 'Malmqvist bias' – which JLA say they have *already* corrected for) ... they describe this by **adding 12 more parameters** to our (10 parameter) model



Figure 2. $\Omega_m - \Omega_\Lambda$ constraints enclosing 68.3% and 95.4% of the samples from the posterior. Underneath, we plot all samples. The left panel shows the constraints obtained with x_1 and c distributions that are constant in redshift, as in the N16 analysis; the right panel shows the constraints from our model. The red square and blue circle show the location of the median of the samples from the respective posteriors.



Even if this is justified, the significance with which a non-accelerating universe is rejected is raised to only ≲4σ ... still inadequate to claim a 'discovery' (even though the dataset has increased from ~50 to 740 SNe Ia in the past 20 yrs)! Acceleration is a *kinematic* quantity so the data can be analysed simply by expanding the time variation of the scale factor in a Taylor series, *without* reference to a dynamical model (e.g. Visser, arXiv:gr-qc/0309109)



This yields 2.8σ evidence for acceleration in our approach ... increasing to only 3.7σ when an *ad-hoc* redshift-dependence is allowed in the light-curve fitting parameters

What about the evidence from BAO, H(z), growth of structure, ...?



The 'independent' lines of evidence are usually obtained using Λ CDM templates!



All data are equally consistent with non-accelerated expansion

Whether the expansion rate is accelerating needs to be *directly* tested using a Laser Comb on the European Extremely Large Telescope to measure redshift drift of the Lyman- α forest over ~15 yr



What about the precision data on CMB anisotropies?

There is no direct sensitivity of the CMB to dark energy ... it is all inferred (in the framework of ACDM model)

Is not dark energy (cosmic acceleration) independently established from combining CMB & large-scale structure observations? Answer: No!

The formation of large-scale structure is akin to a scattering experiment

The **Beam: inflationary density perturbations**

No 'standard model' – assumed to be adiabatic and close to scale-invariant

The Target: dark matter (+ baryonic matter)

Identity unknown - usually taken to be cold and collisionless

The **Detector: the universe**

Modelled by a 'simple' FRW cosmology with parameters $h, \Omega_{ ext{CDM}}, \Omega_{ ext{B}}, \Omega_{\Lambda}, \Omega_{k}$

The Signal: CMB anisotropy, galaxy clustering, weak lensing ... measured over scales ranging from $\sim 1 - 10000$ Mpc ($\Rightarrow \sim 8$ e-folds of inflation)

But we *cannot* uniquely determine the properties of the **detector** as well as of the (unknown) **beam** and **target**, from their convolution!

... hence need to adopt 'priors' on h, Ω_{CDM} ..., and assume a primordial powerlaw spectrum, in order to break inevitable **parameter degeneracies** With different assumptions can match same data without Λ (Hunt & Sarkar, arXiv:0706.2443) E.g. if there is a 'bump' in the spectrum (around the first acoustic peak), the CMB data can be fitted without dark energy $(\Omega_m = 1, \Omega_\Lambda = 0)$ if $h \sim 0.43$ Hunt & Sarkar, arXiv:0706.2443, 0807.4508

While significantly below the *local* value of $h \sim 0.67$, this agrees with its value in the effective E-deS relativistic inhomogeneous model that matches stellar ages (H(z) data)

The small-scale power would be excessive unless damped by free-streaming But adding 3 vs of mass ~0.5 eV ($\Rightarrow \Omega_v \approx 0.1$) gives *good* match to large-scale structure (note that $\Sigma m_v \approx 1.5$ eV ... well above 'CMB bound' – but detectable by KATRIN!)

Fit gives $\Omega_{\rm b}h^2 \approx 0.021 \rightarrow \text{BBN } \checkmark \Rightarrow$ baryon fraction in clusters predicted to be ~11% \checkmark

Summary

The 'standard model' of cosmology was established long before there was any observational data ... and its empirical foundations (homogeneity, ideal fluids) have never been rigorously tested. Now that we have data, it should be a priority to *test the model assumptions* – not simply measure its parameters ... moreover these should be 'blind' analyses (i.e. not assuming the answer beforehand!)

It is not simply a choice between a cosmological constant ('dark energy') and 'modified gravity' – there are other interesting possibilities (e.g. 'back-reaction' and 'effective viscosity')

➤ The fact that the standard model implies an *unnatural* value for the cosmological constant, $\Lambda \sim H_0^2$, ought to motivate further work on developing and testing alternative models ... rather than pursuing "precision cosmology" of what may well turn out to be an illusion