

Experimental Exploration of QCD – Matter

Outline

QCD

Matter and phase transitions

QCD phase diagram

Nuclear liquid – gas phase transition

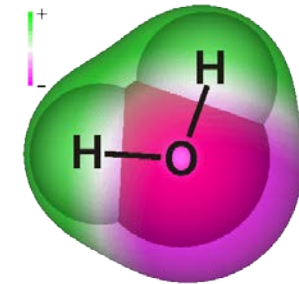
(s)QGP properties (LHC, RHIC)

Search for phase boundaries (STAR, SPS)

Outlook (FAIR)

Conclusion

QED – analog





QCD Lagrangian

$$\mathcal{L}_{QCD} = -\frac{1}{4}F_{\mu\nu}^a F^{a\mu\nu} + \sum_a \bar{\psi}_i^q (i\gamma^\mu D_{\mu ij} - m_q \delta_{ij}) \psi_j^q .$$
$$F_{\mu\nu}^a = \partial_\mu A_\nu^a - \partial_\nu A_\mu^a + g_s f^{abc} A_\mu^b A_\nu^c$$
$$D_{\mu ij} = \delta_{ij} \partial_\mu - ig_s T_{ij}^a A_\mu^a$$

where

- g_s is the QCD coupling constant
- f^{abc} are the structure constants of SU(3): $[T^a, T^b] = i f^{abc} T^c$ (a,b,c = 1,...,8)
- A_μ^a are the 8 *gluon* fields
- T_{ij}^a are 8 'colour matrices', i.e. generators of the SU(3) transformation acting on the fundamental (triplet) representation:

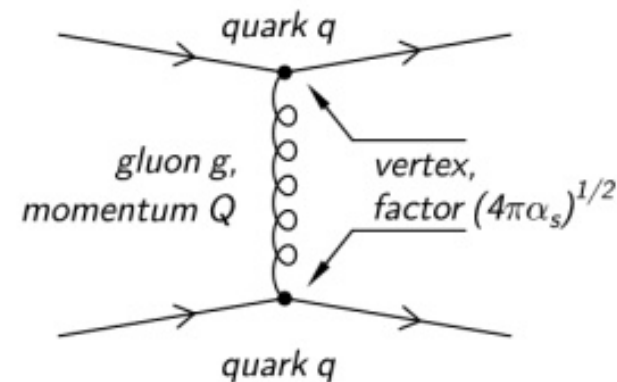
the QCD Lagrangian is invariant under local SU(3) transformations:

$$\psi \longrightarrow \exp \left(i \sum_{a=1}^8 T^a \alpha^a(x) \right) \psi$$
$$A_\mu^a \longrightarrow A_\mu^a - \frac{1}{g_s} \partial_\mu \alpha^a - \sum_{b,c=1}^8 f^{abc} \alpha^b A_\mu^c$$



Features of QCD

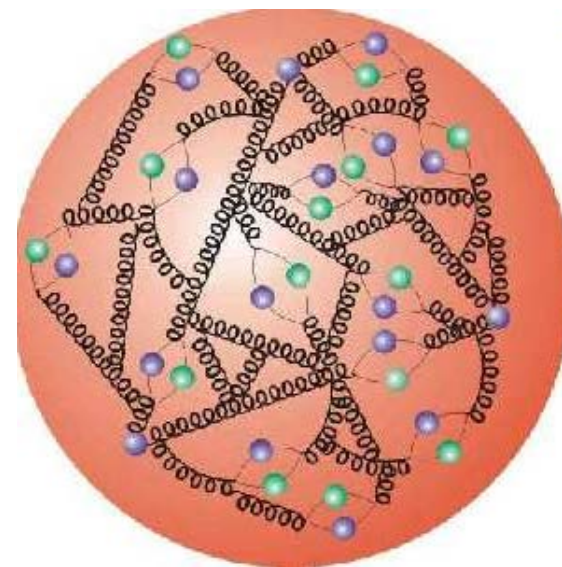
High energy behavior (large momentum transfers, small distances):
perturbative treatment possible

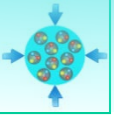


Low energy behavior (large distances)
non - perturbative treatment necessary

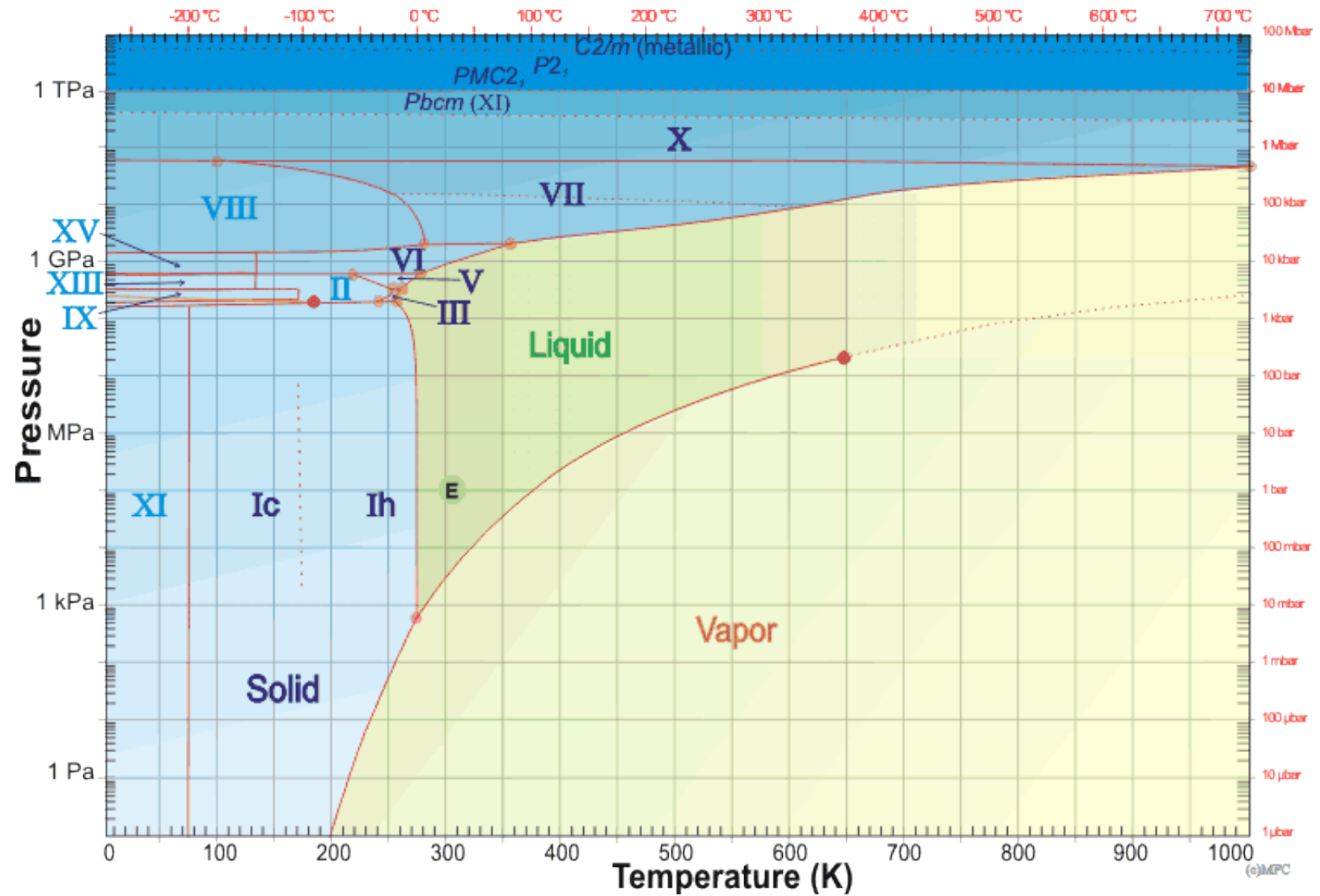
1) confinement

2) approximate chiral symmetry

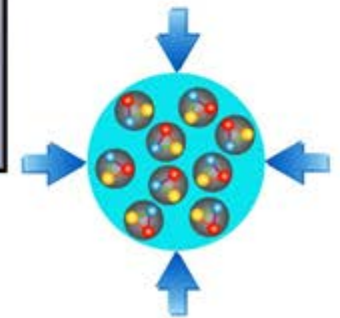
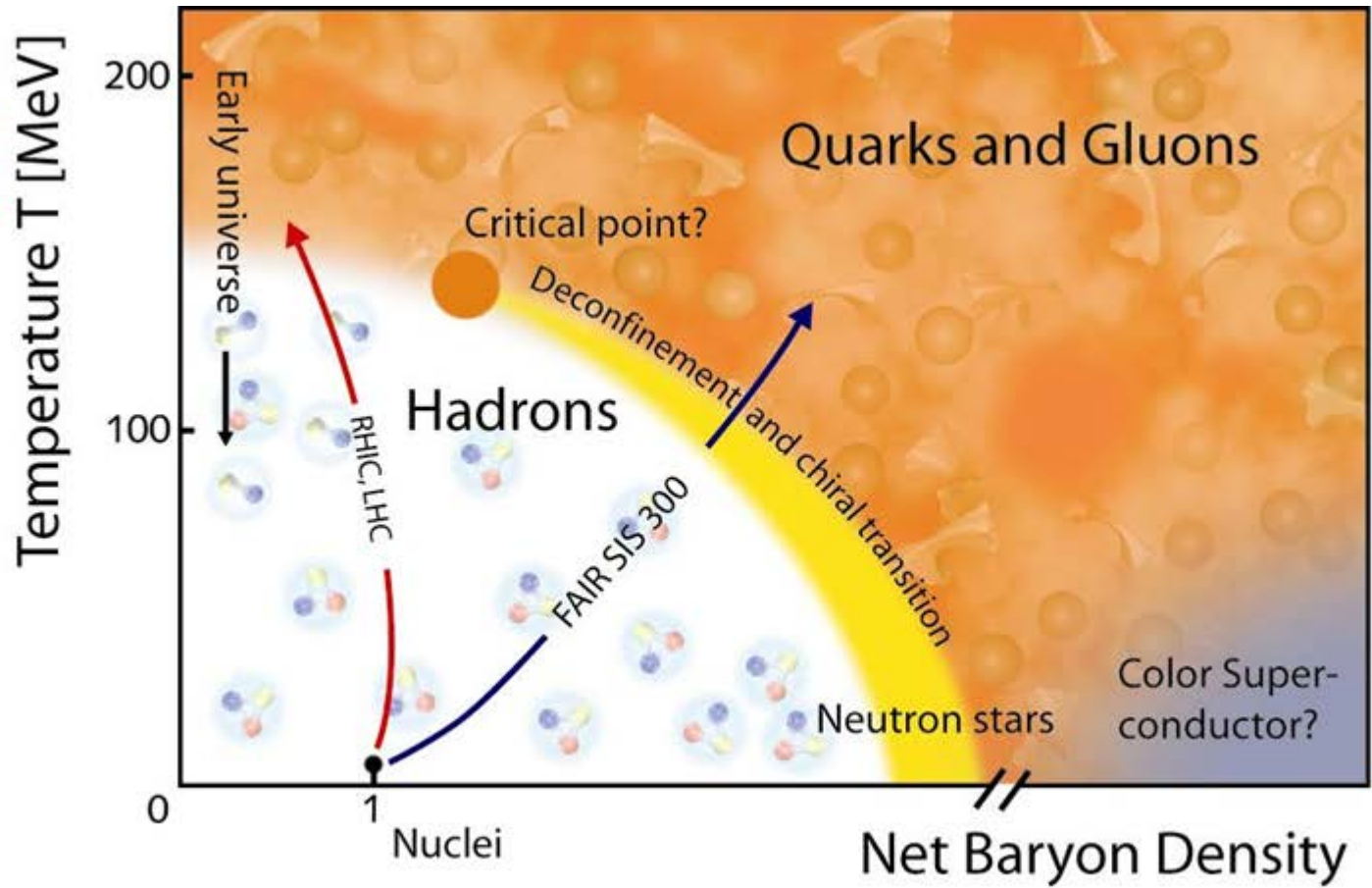




Phase diagram of water



QCD phase diagram

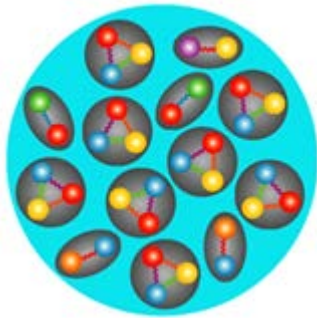




Phases and phase transitions

Thermodynamic description: choice of proper variables:

**Control parameters = external variables for reaction system
= independent variables in thermodynamic potential**



**Temperature T ,
Volume V ,
Particle number N**

Helmholtz free energy F :

$$F = F(T, V, N)$$

$$dF = -SdT - PdV + \mu dN$$

Entropy S , pressure P and chemical potential μ are system properties.

Relation between state variables is called Equation – of – State (EOS), e.g.

$$P = P(\rho, T)$$

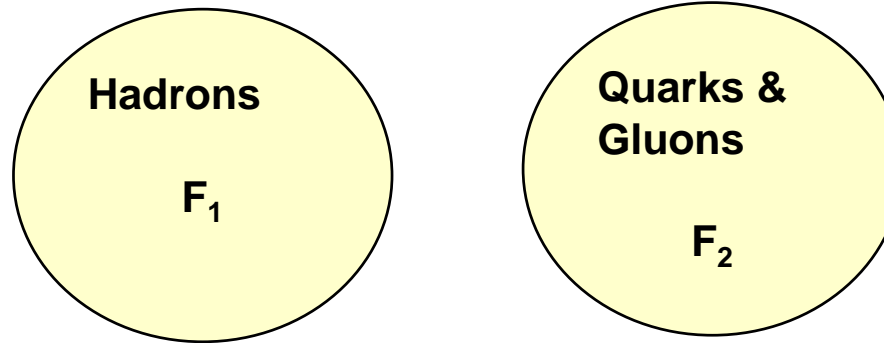
$$P = P(\varepsilon, T)$$

ρ – particle number density
 ε – energy density



Phase boundary

Nature prefers phase with lowest free energy F .



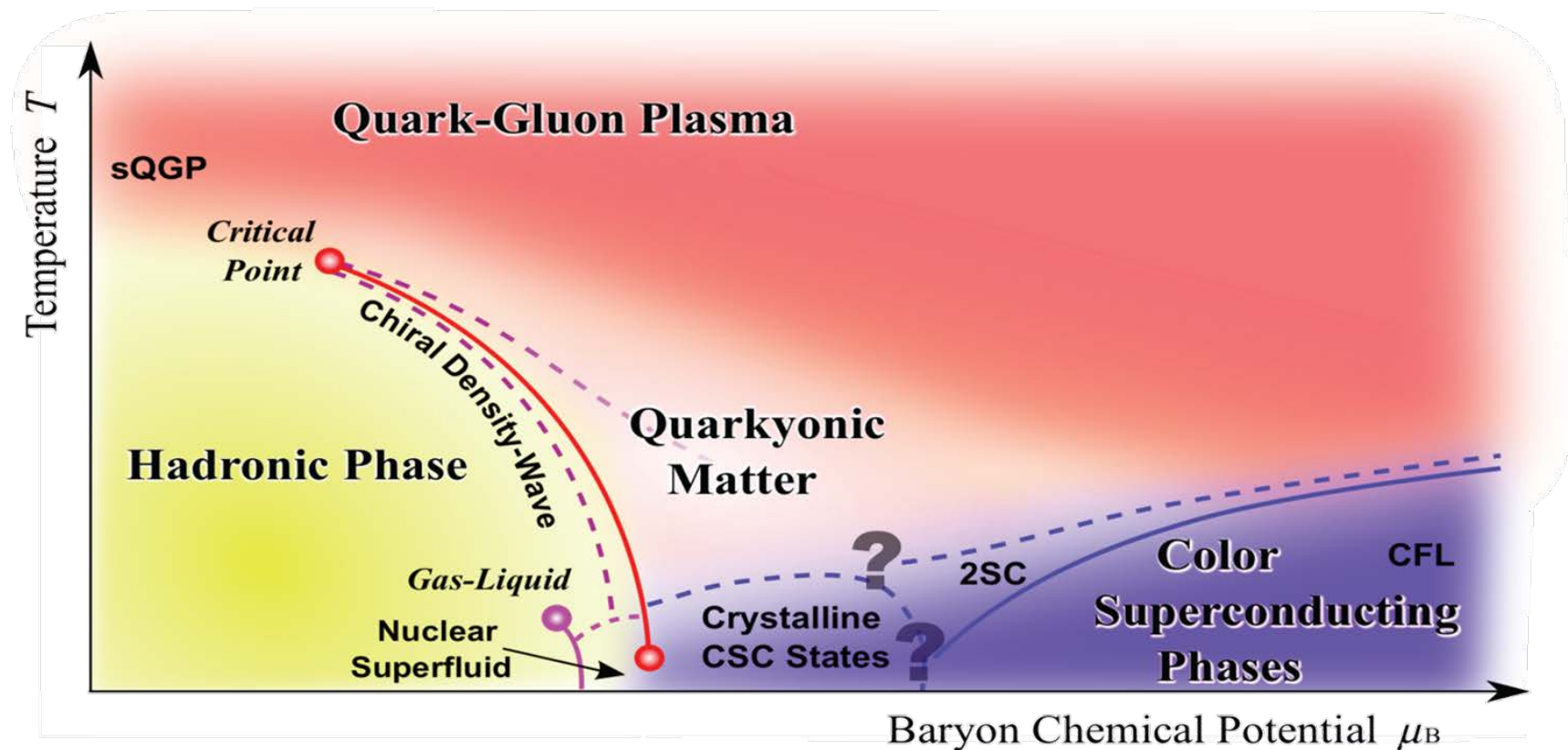
Phase equilibrium between 2 phases $j=1,2$:

$$dF|_{T,V} = \sum_j \mu_j dN_j \stackrel{!}{=} 0 \quad \Rightarrow \quad \mu_1(P,T) = \mu_2(P,T)$$



QCD phase diagram

K. Fukushima, C. Sasaki, *Prog.Part.Nucl.Phys.* 72 (2013) 99





History:

QGP concept

J.C. Collins, M.J. Perry, Phys. Rev. Lett. 34 (1975) 1373

N. Cabibbo, G. Parisi, Phys. Lett. B59 (1975) 67

Liquid – gas phase transition in nuclei

Theory

P.A. Siemens, Nature 305 (1983)

Experiments

(since ~1995)

New State of Matter (CERN 2000)

Perfect liquid (RHIC 2008)

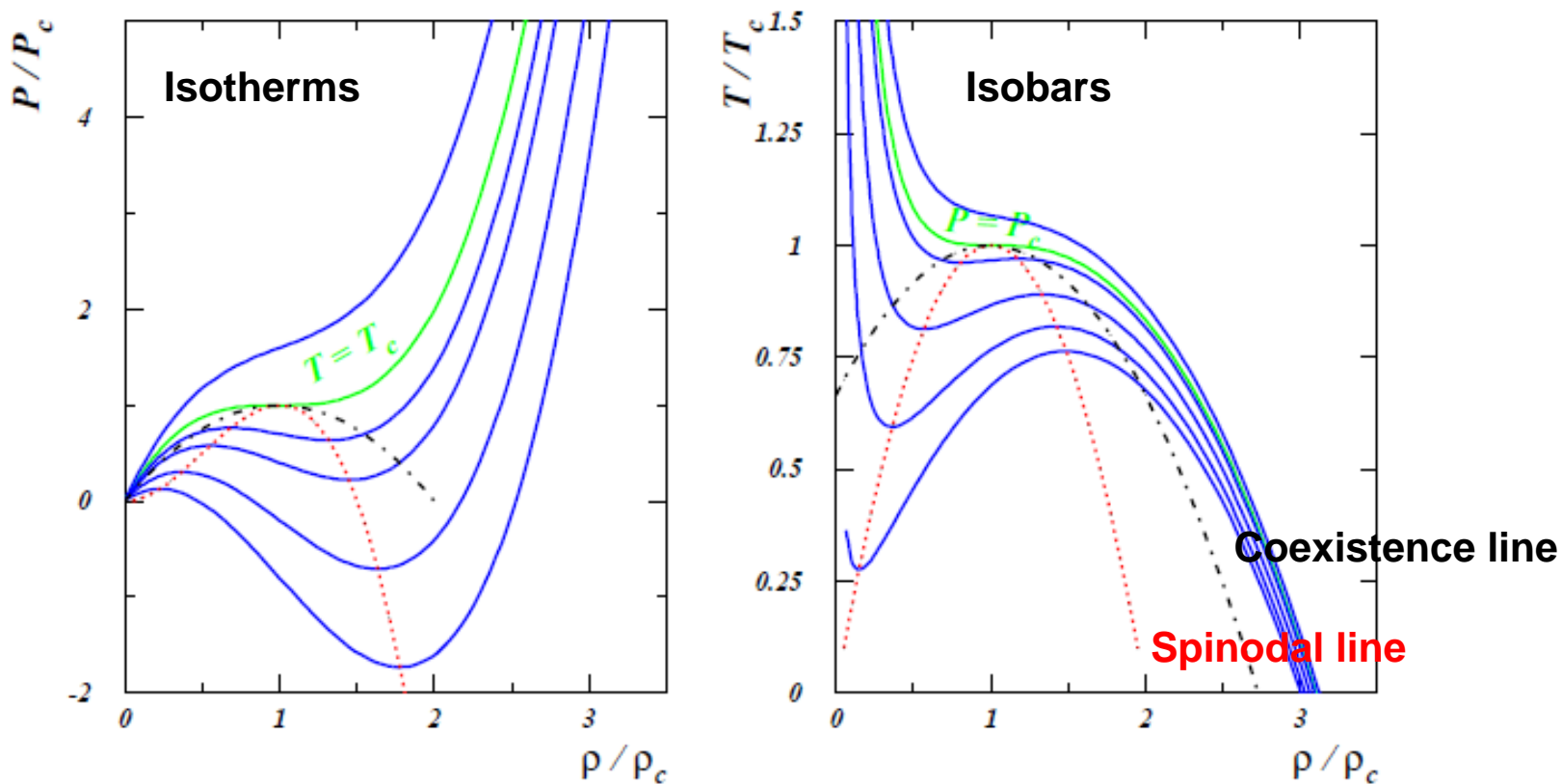
Helpful conditions: large long-lived systems!



Nuclear liquid – gas - phase transition

Nuclei show properties of liquid -> ‘liquid – drop model’,
Bethe – Weizsäcker mass formula.

NN – potential very similar to Lennard – Jones – potential.



Recent review:

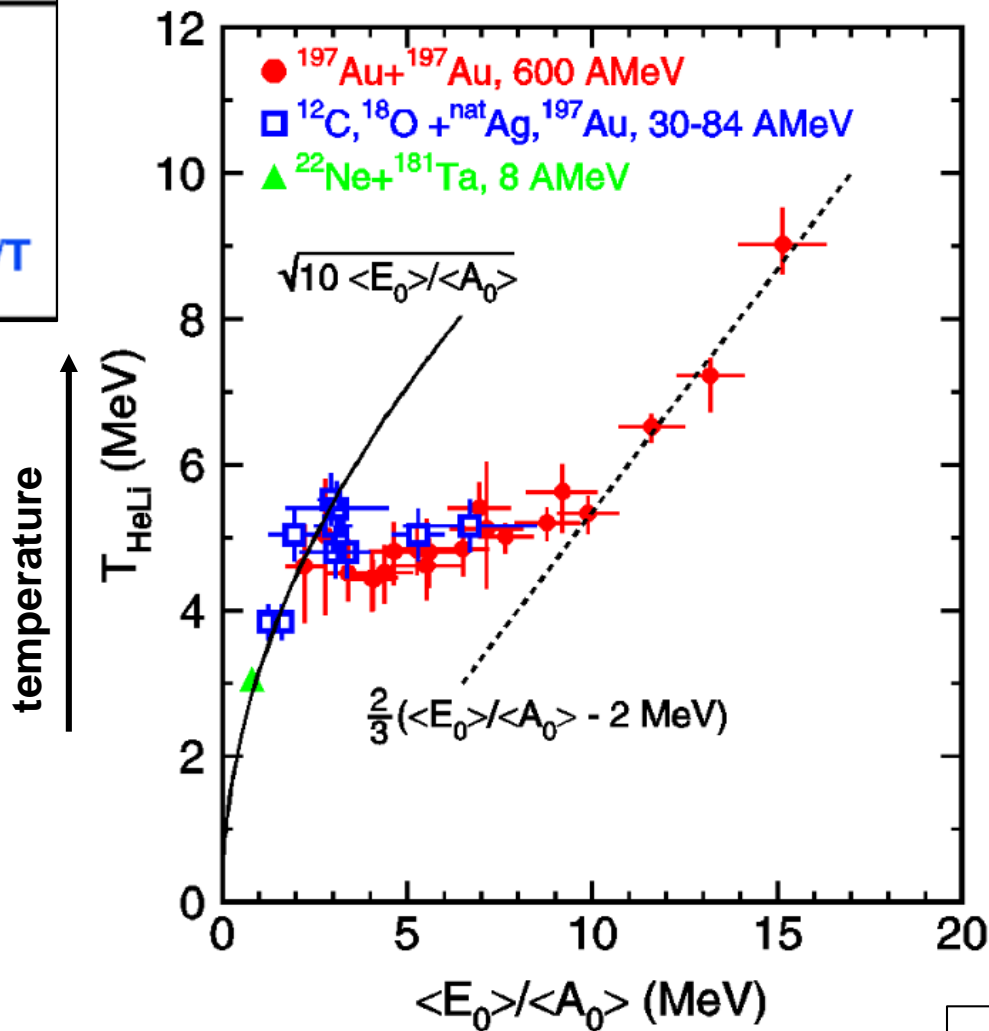
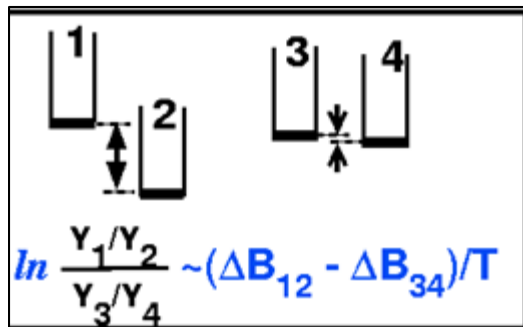
B. Borderie, M.F. Rivet,

“Nuclear multifragmentation and phase transition for hot nuclei”,
Progress in Particle and Nuclear Physics 61 (2008) 551-601

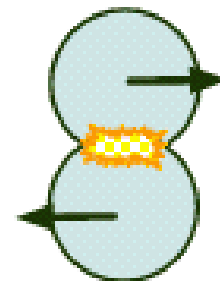


Caloric curve of nuclei

J. Pochodzalla et al. (ALADIN), PRL 75(1995) 1040



Peripheral
HI - collisions



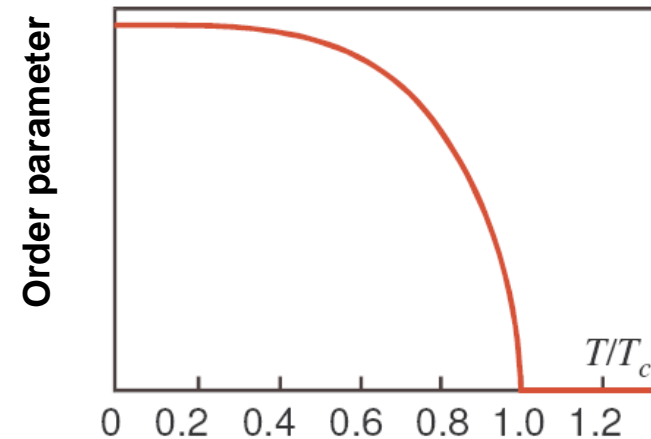
$$\langle E_0 \rangle = \left(\left\langle \sum_i m_i \right\rangle + \left\langle \sum_i K_i \right\rangle \right) - (\langle m_0 \rangle + \langle K_0 \rangle)$$

$$A_0 = \sum_i A_i$$



Description of phase transition

Phases are characterized by the presence of an order parameter that vanishes when going to a different phase.



Examples of order parameters:

- Liquid gas – density difference of liquid to gaseous phase
- Ferromagnet – spontaneous magnetisation
- Superconductor – energy gap in electron excitation spectrum

Thermodynamic Potential (e.g. Free energy) is non analytic function of order parameter.

Ehrenfest's classification of phase transitions:

Phase transition of n^{th} order = one of the n^{th} – derivatives of the potential is discontinuous, while all derivatives of lower order are continuous.



Critical exponents

Close to a critical point the thermodynamic behaviour of physical systems is universal and depends within a universality class only on

$$t = \frac{T - T_C}{T_C}$$

Thermodynamic quantities show a power law behaviour:

Heat capacity: $C \sim |t|^{-\alpha}$

Order parameter: $M \sim |t|^\beta$

Susceptibility: $\chi \sim |t|^{-\gamma}$

Equation – of – state: $M \sim |H|^\frac{1}{\delta}$

Correlation length: $\xi \sim |t|^{-\nu}$

Griffiths universality hypothesis

R.B. Griffiths, PRL 24, 1479 (1970):

Critical exponents are universal and depend only on:

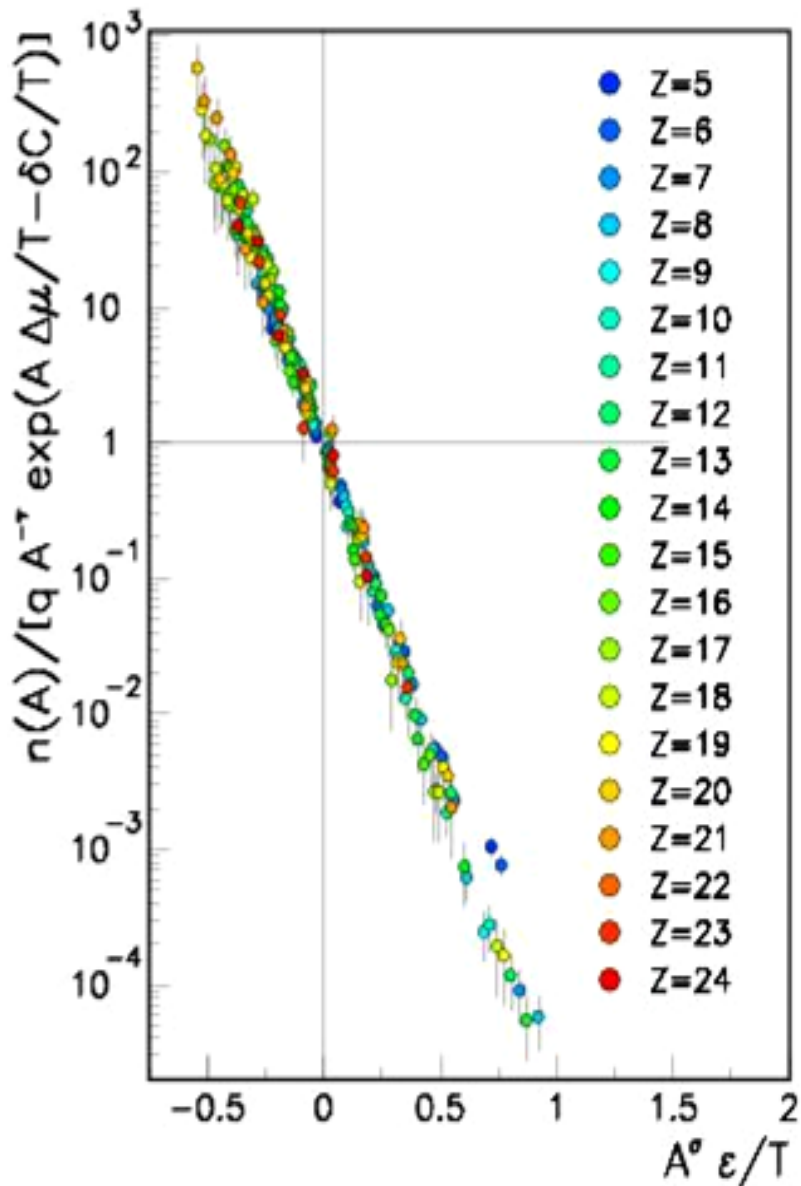
- 1) Dimension of the system
- 2) Range of the interaction
- 3) Spin dimensionality

Note: Only 2 of the critical exponents are independent.



Nuclear liquid - gas phase transition

M. D'Agostino et al., NPA 724, 455 (2003)



Fragment distribution

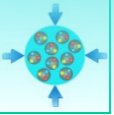
(Fisher droplet model 1967)

$$n_A = q_o A^{-\tau} \exp\left(\frac{-c_o \epsilon A^\sigma}{T}\right)$$

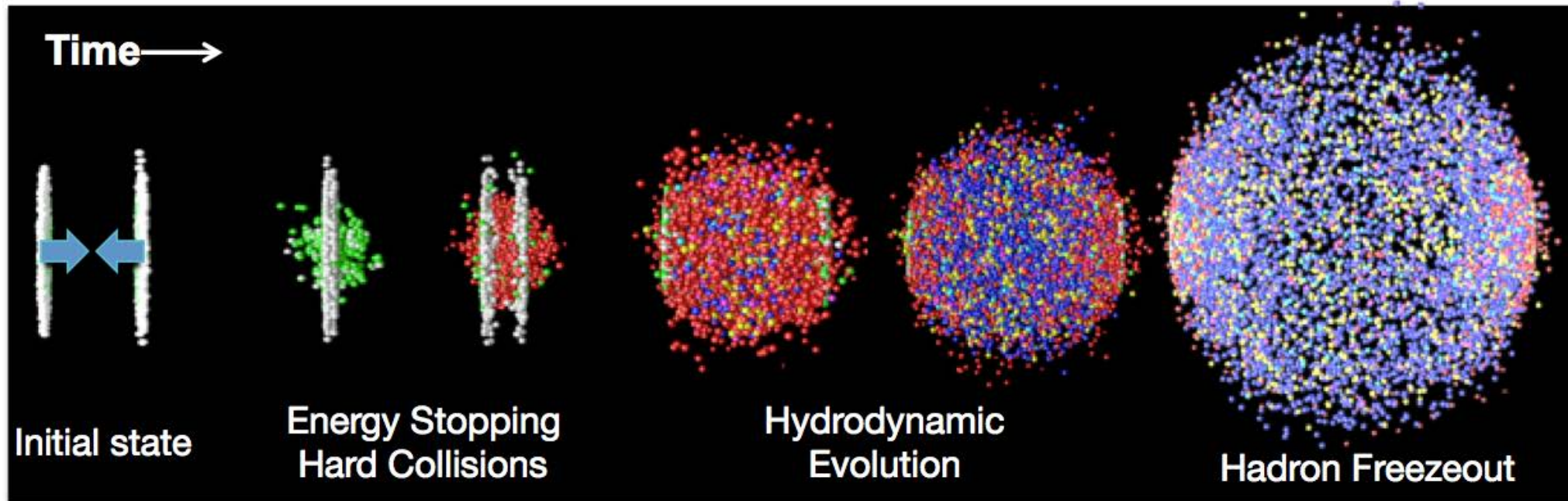
$$\epsilon = \frac{T_c - T}{T_c}$$

Universal critical exponents in the vicinity of the critical point:

	Au	Liquid-Gas
τ	2.1 ± 0.1	2.196 ± 0.024
σ	0.66 ± 0.02	0.647 ± 0.006



How to produce a phase of QCD matter ?



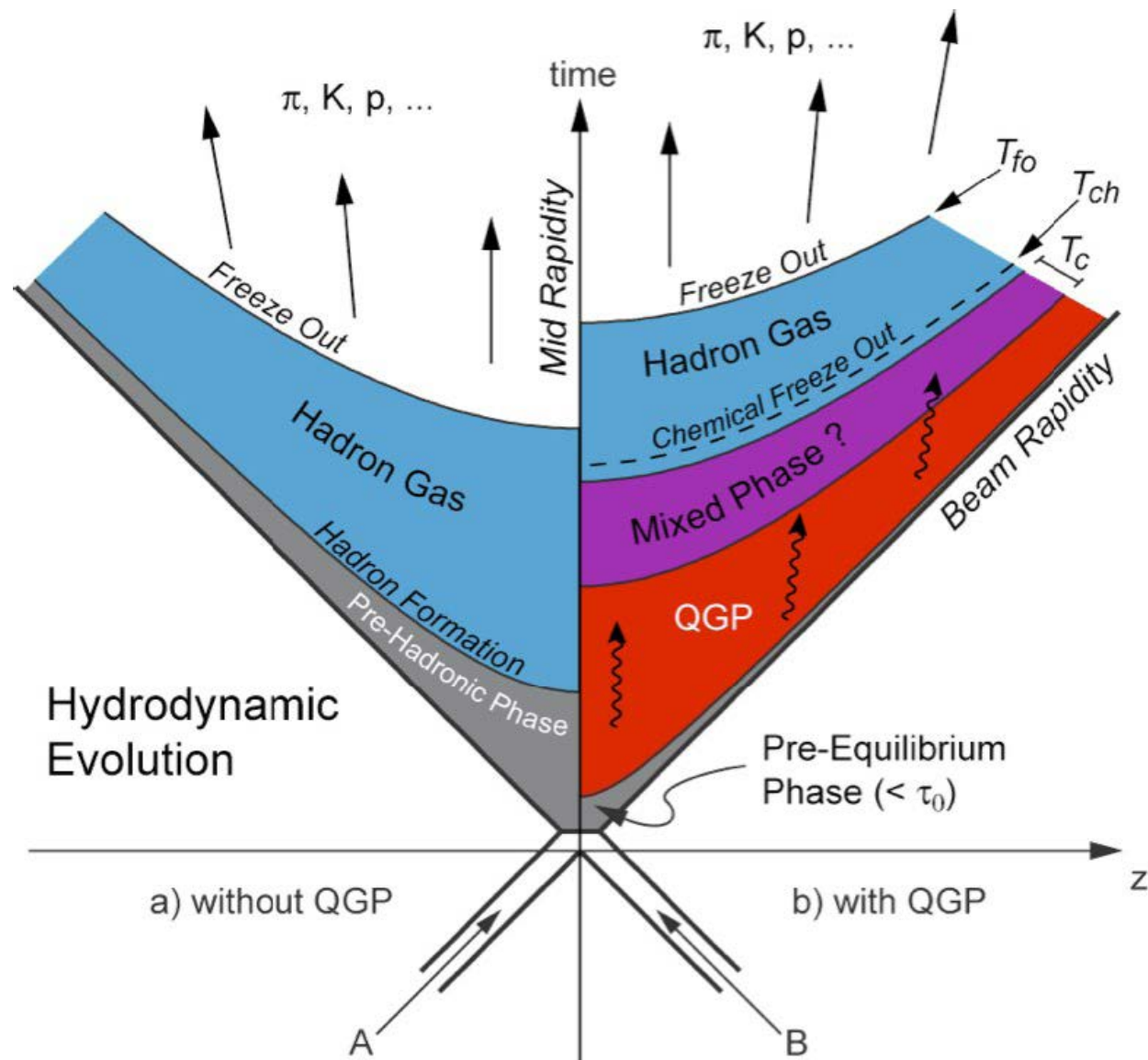
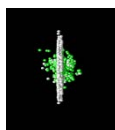
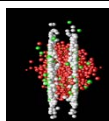
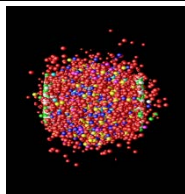
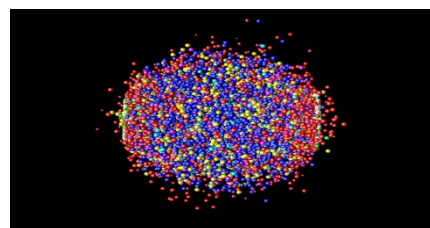
Dynamical Evolution

Thermalization ?





Relativistic Reaction Dynamics





Theory: Thermal model

P. Braun-Munzinger et al., arXiv:nucl-th/0304013

Chemical thermal model:

assume a common 'surface' at which all particles decouple (inelastic collisions stop)

Grand canonical formulation (i.e. energy and particle exchange with heat bath)

Partition function:

$$Z^{GC}(T, V, \mu_Q) = \text{Tr} \left[e^{-\beta \left(H - \sum_i \mu_{Q_i} Q_i \right)} \right]$$

Q_i = conserved quantum numbers (baryon number, strangeness, isospin, charm,...)

$\beta = 1/T$, T = Temperature

H = Hamiltonian of non-interacting hadron gas

Grand canonical potential J :

$$J(T, V, \mu_Q) = -T \ln Z^{GC}(T, V, \mu_Q)$$

$$F(T, V, N) = J(T, V, \mu_Q) + \sum_i \mu_{Q_i} N_i$$

Decomposition into individual hadronic species:

$$\ln Z^{GC}(T, V, \mu) = \sum_i \ln Z_i^{GC}(T, V, \mu)$$



Thermal model for particle production

P. Braun-Munzinger et al., arXiv:nucl-th/0304013

Chemical equilibrium concept.

Density of particle species i:

$$n_i(\mu, T) = \frac{N_i}{V} = -\frac{T}{V} \frac{\partial \ln Z_i}{\partial \mu_i} = \frac{g_i}{2\pi^2} \int \frac{p^2 dp}{e^{\frac{E_i - \mu_i}{T}} \pm 1}$$

$$\mu_i = \mu_B B_i + \mu_S S_i + \mu_{I_3} I_{3,i}$$

“+” for fermions, “-” for bosons
 g_i – spin degeneracy factor

Chemical potentials μ_i are constrained by conservation of quantum numbers:

baryon number:

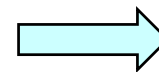
$$V \sum_i n_i B_i = Z + N \rightarrow V$$

strangeness:

$$V \sum_i n_i S_i = 0 \rightarrow \mu_S$$

charge:

$$V \sum_i n_i I_{3,i} = \frac{Z - N}{2} \rightarrow \mu_{I_{3,i}}$$



**3 equations,
5 unknowns**



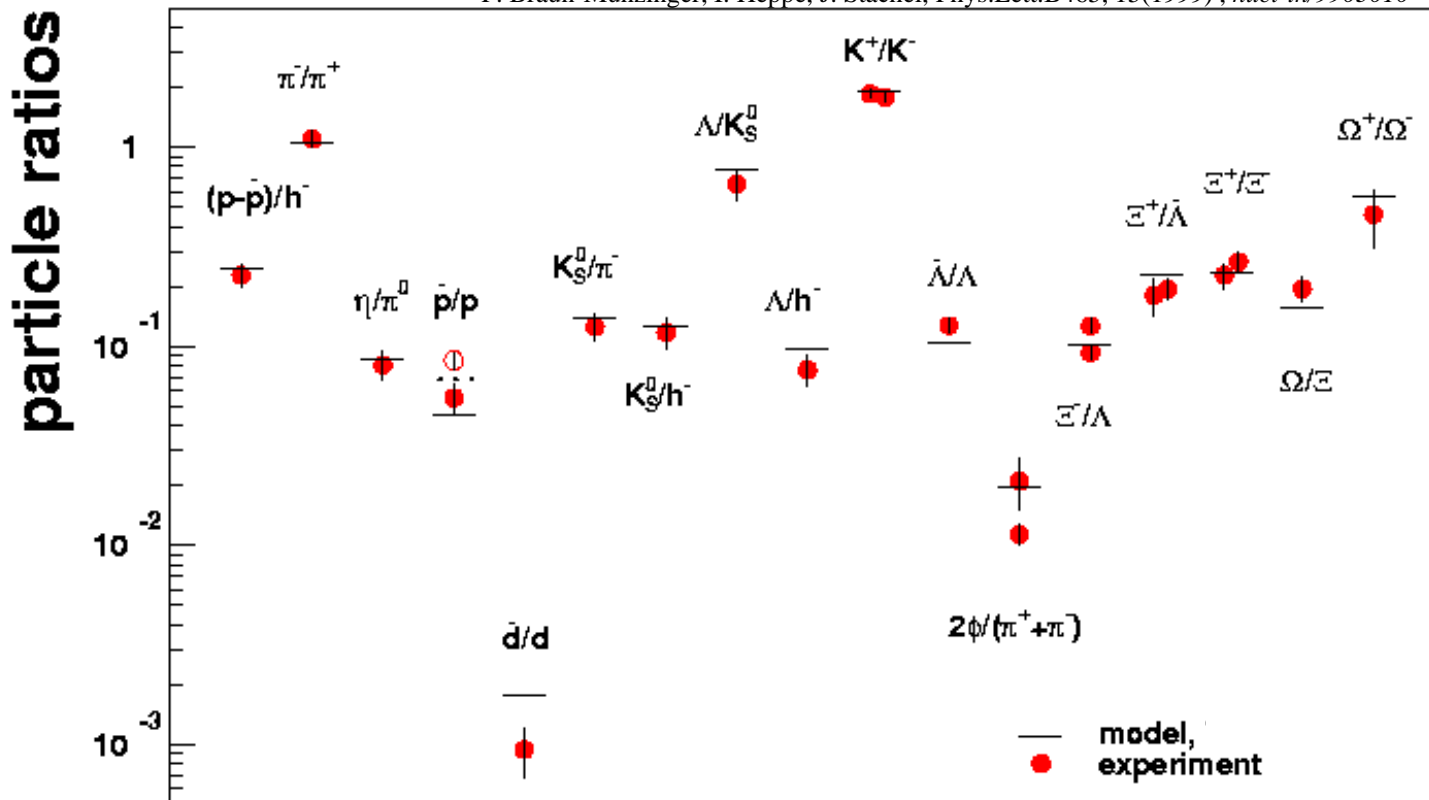
2 free parameter



Chemical equilibrium

Example: SPS data, $E_{\text{beam}}=158 \text{ AGeV}$, Pb+Pb

P. Braun-Munzinger, I. Heppe, J. Stachel, Phys.Lett.B465, 15(1999), nucl-th/9903010



Model parameter:

$$T = 168 \pm 2.4 \text{ MeV}$$

$$\mu_B = 266 \pm 5 \text{ MeV}$$

Note: volume is not needed for description of particle ratios.

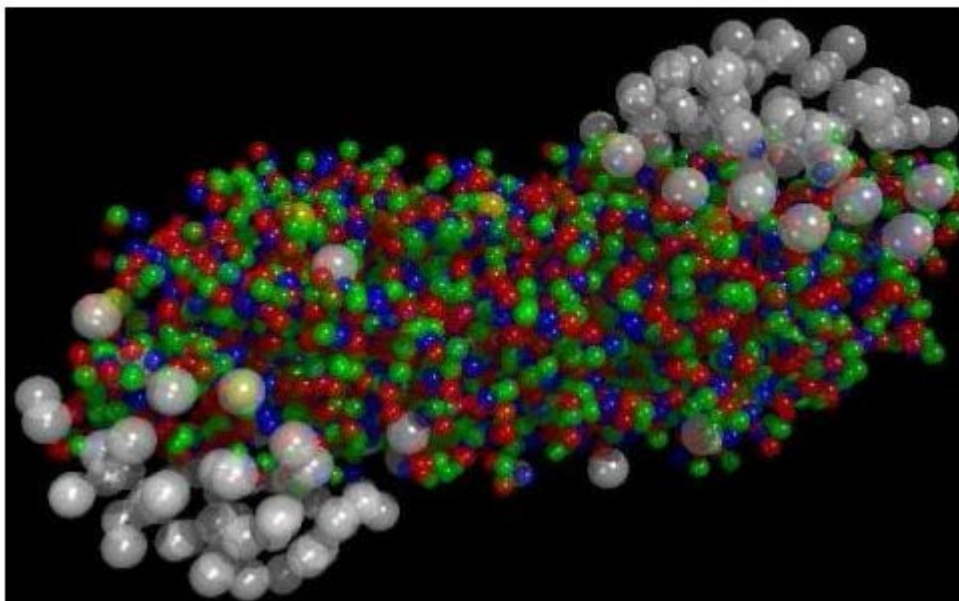
$$\mu_S = 71.1 \text{ MeV}$$

$$\mu_{I_3} = -5. \text{ MeV}$$



New State of Matter created at CERN

10 Feb 2000



<http://press.web.cern.ch/press-releases/2000/02/new-state-matter-created-cern>

Based on a (unpublished) 'common assessment' of results from ~ half dozen experiments

collected & published over the course of the SPS Pb program (1994 - 2000)

<http://arxiv.org/abs/nucle-th/0002042v1>

“The collected data from the experiments gives compelling evidence that a new state of matter has been created. This state of matter found in heavy ion collisions at the SPS features many of the characteristics of the theoretically predicted quark-gluon plasma..”

'.. a QGP-like state ..'



Signature of the “QGP” – phase

Thermodynamic behavior at freeze – out

Strangeness enhancement

J/Ψ – production

Low – mass dileptons

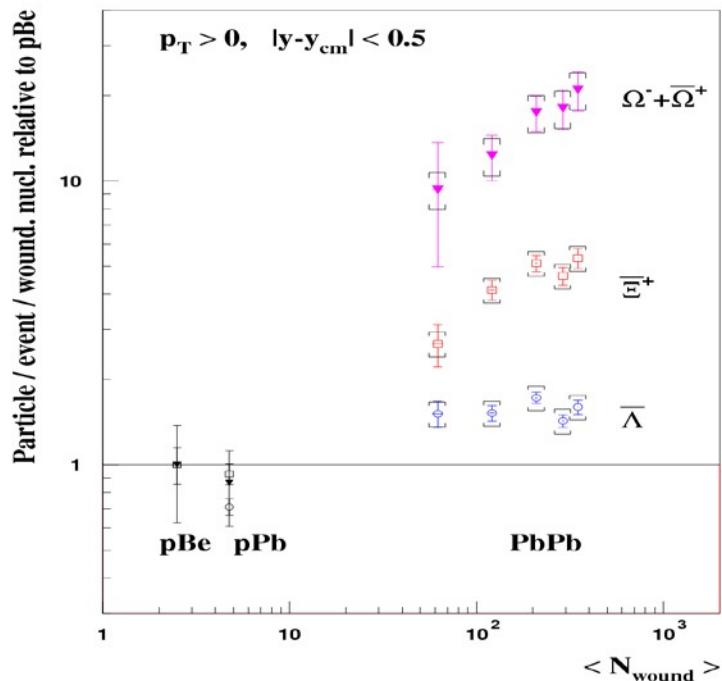
Partonic flow

Jet – propagation in hot QCD – matter



Main results from SPS

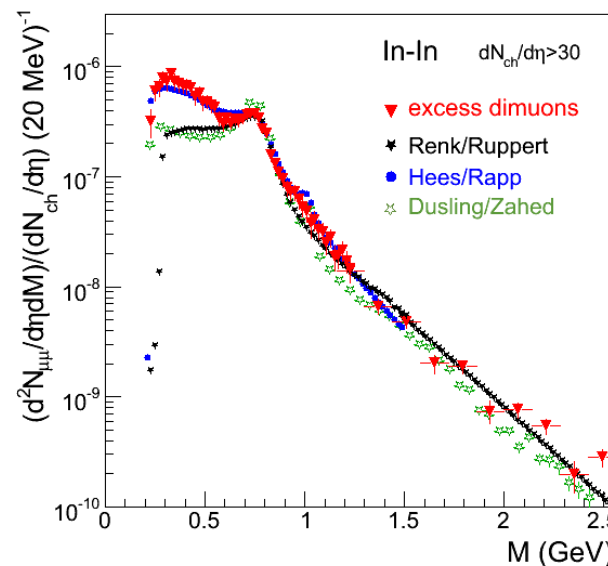
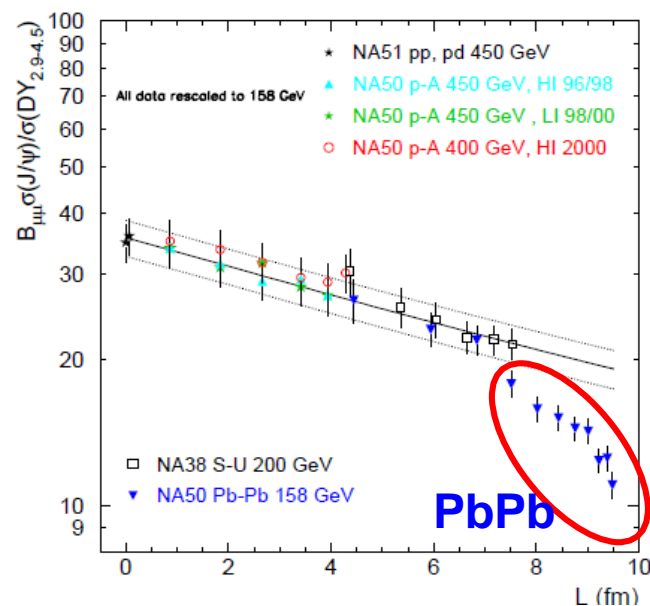
Strangeness enhancement



Enhancement of low mass lepton pairs

ρ – melting, chiral symmetry restoration

anomalous J/Y suppression



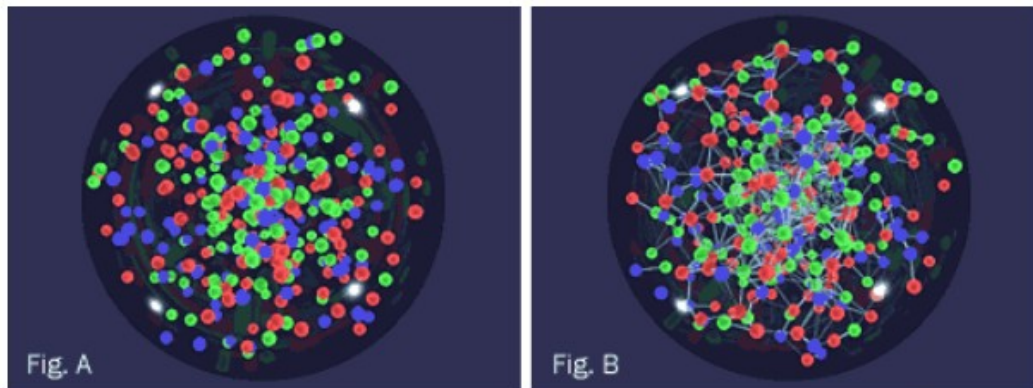


RHIC press release (2005)

RHIC Scientists Serve Up "Perfect" Liquid

New state of matter more remarkable than predicted -- raising many new questions

April 18, 2005



These images contrast the degree of interaction and collective motion, or "flow," among quarks in the predicted gaseous quark-gluon plasma state (Figure A, see [mpeg animation](#)) vs. the liquid state that has been observed in gold-gold collisions at RHIC (Figure B, see [mpeg animation](#)). The green "force lines" and collective

[+ENLARGE](#)

<http://www.bnl.gov/newsroom/news.php?a=1303>

Based on a (published) comprehensive (re)analysis of the first years of RHIC (2000 - 2004)

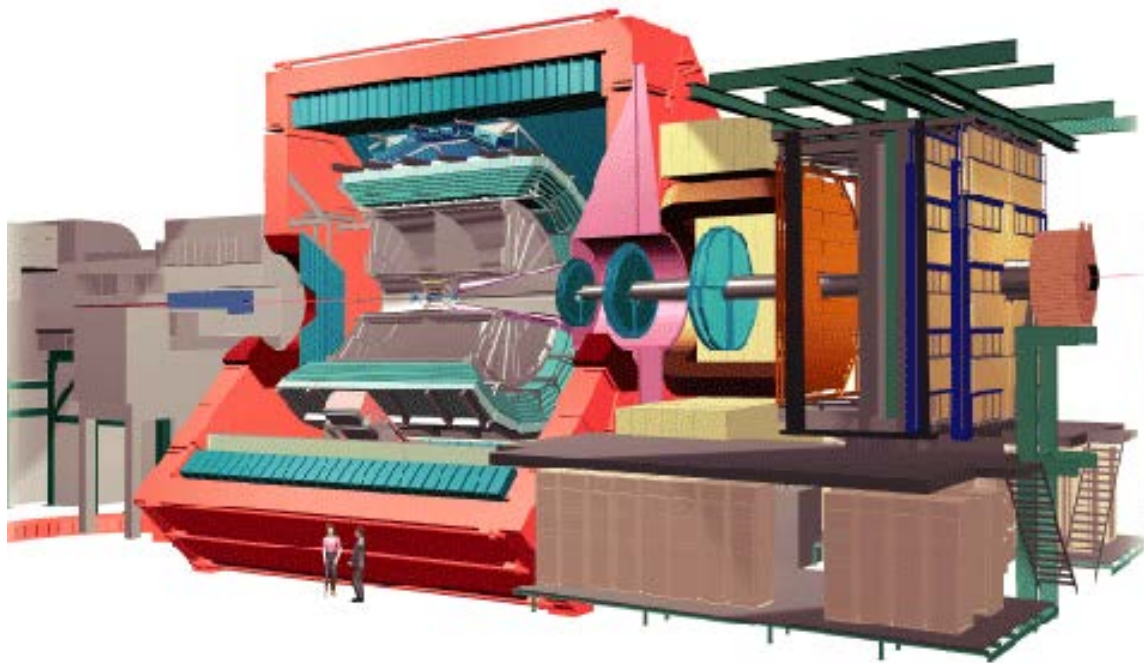
Nucl.Phys.A757:1-284,2005

.. created a new state of hot, dense matter out of the quarks and gluons .., but it is a state quite different and even more remarkable than had been predicted.

sQGP: strongly interacting QGP



ALICE @ LHC

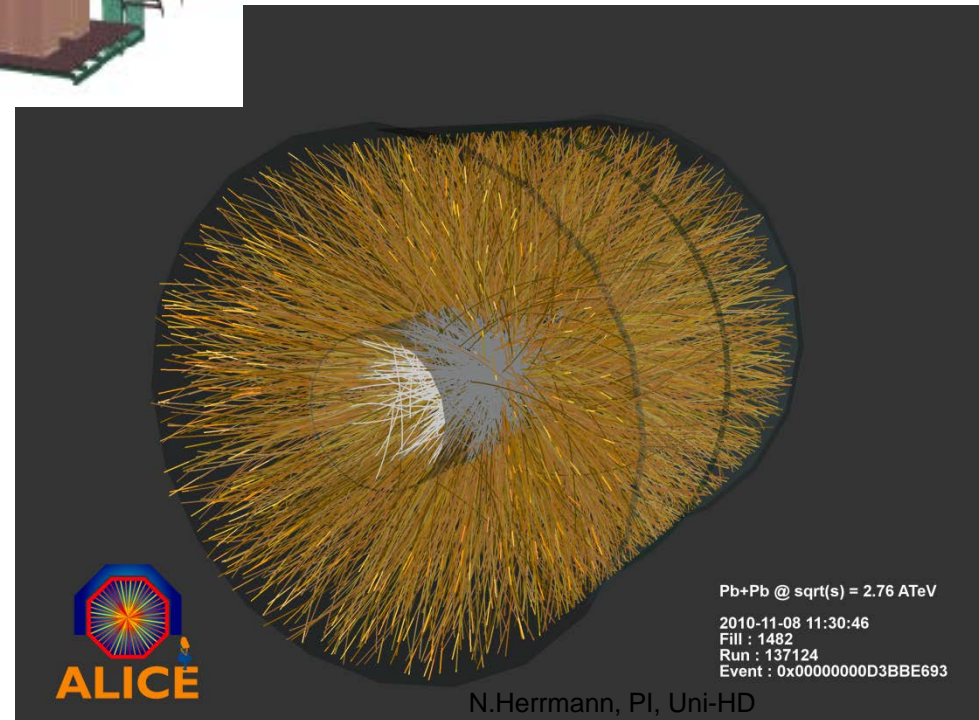


Pb+Pb collisions at LHC (2011)

$\sqrt{s} = 2.76 \text{ ATeV} = 574 \text{ TeV}$

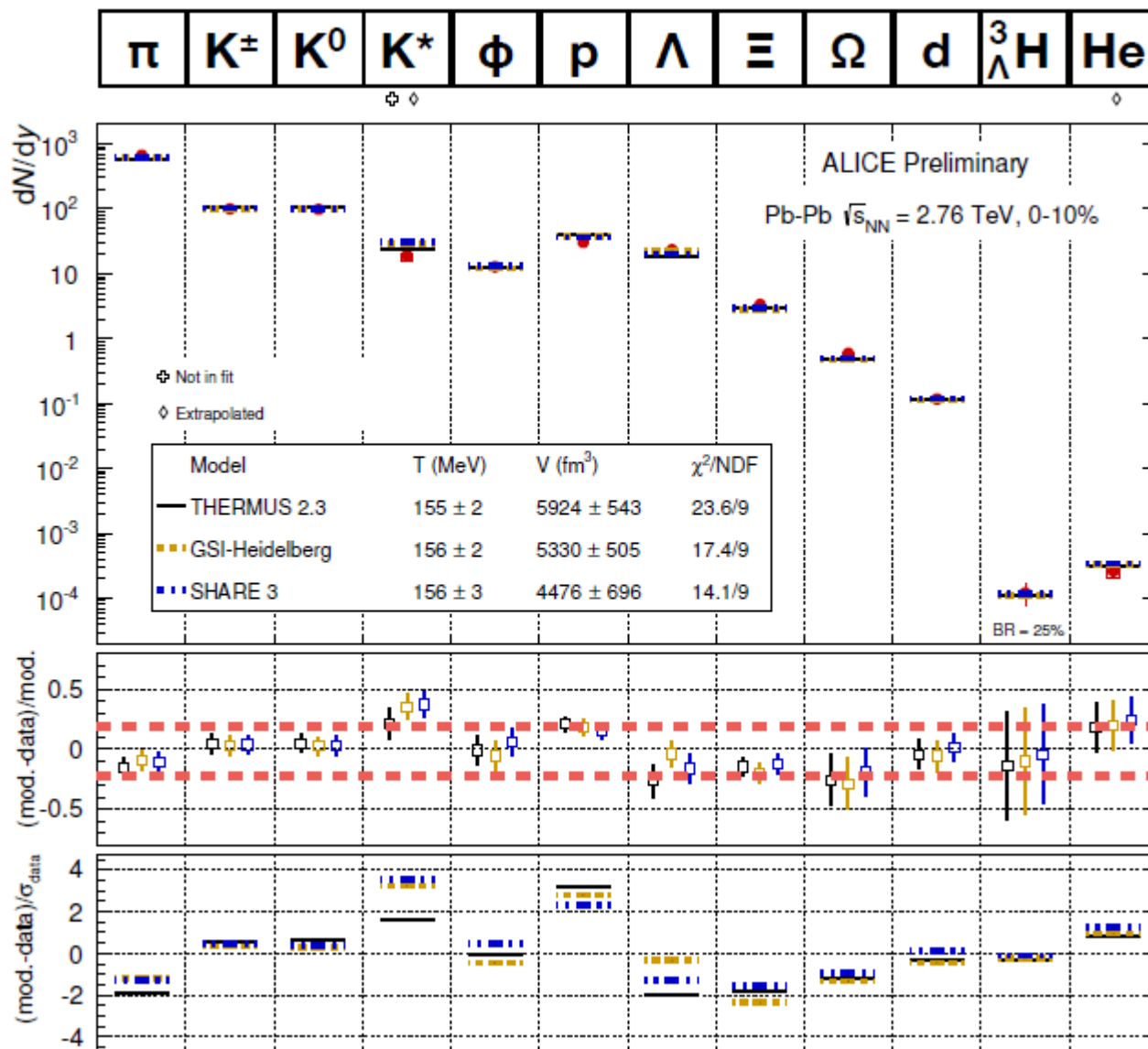
$R_{\text{interaction}} = 5 \text{ kHz}$

$N_{\text{particles}} < 20.000$





Particle Yields at LHC (ALICE)



N.B.
at RHIC
 $\sqrt{s}=200$ A GeV STAR
 χ^2 /NDF ~ 1

Petran et al, arXiv:1310.5108
Wheaton et al, Comput.Phys.Commun, 180 84
Andronic et al, PLB 673 142



Tension Thermal Model / Data

- **Incomplete hadron spectrum in the model** PRL 113, 072001 (2014)
arXiv:1405.7298
 - **Affects feed-down and hence final abundances**

- **Inelastic interactions in the hadronic phase** PRC 90, 054907 (2014)
 - **May deplete baryons**

- **Flavor ordering at freeze-out** PRL 111, 202302 (2013)
 - **Different T preferred by s and $u-d$**

- **Non-equilibrium thermal model** PRC, 88, 021901 (2013)
 - **reflects equilibrium in the preceding QGP phase**



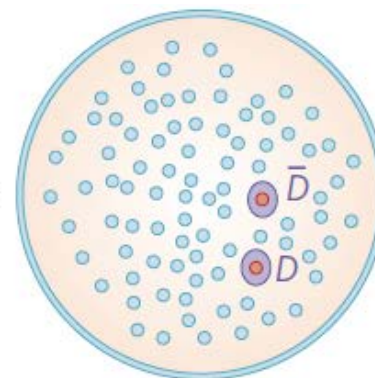
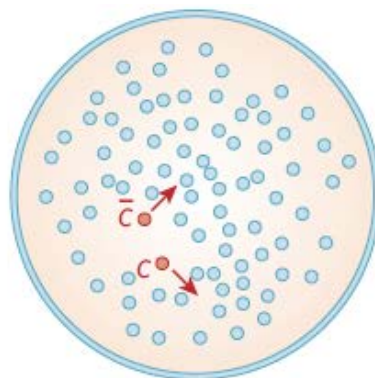
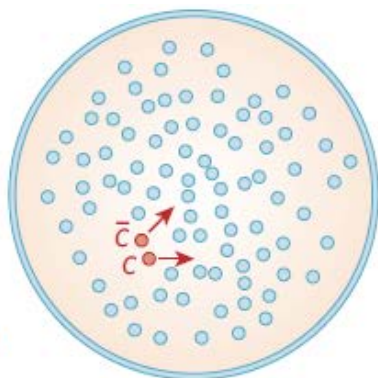
J/ψ – production in HIC

production

equilibration

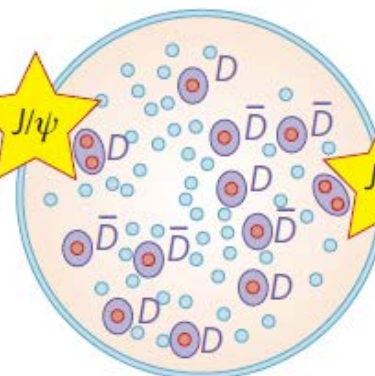
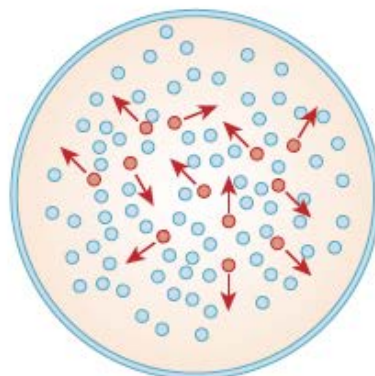
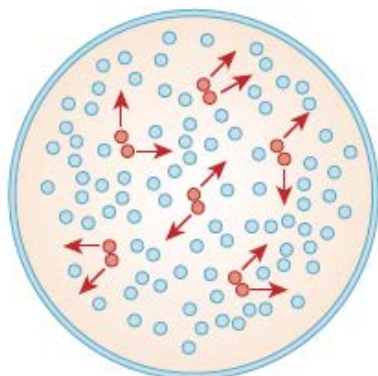
freeze-out

“low” energy
SPS, RHIC



suppression

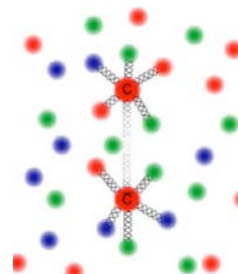
“high” energy
LHC



enhancement

Debye – screening:

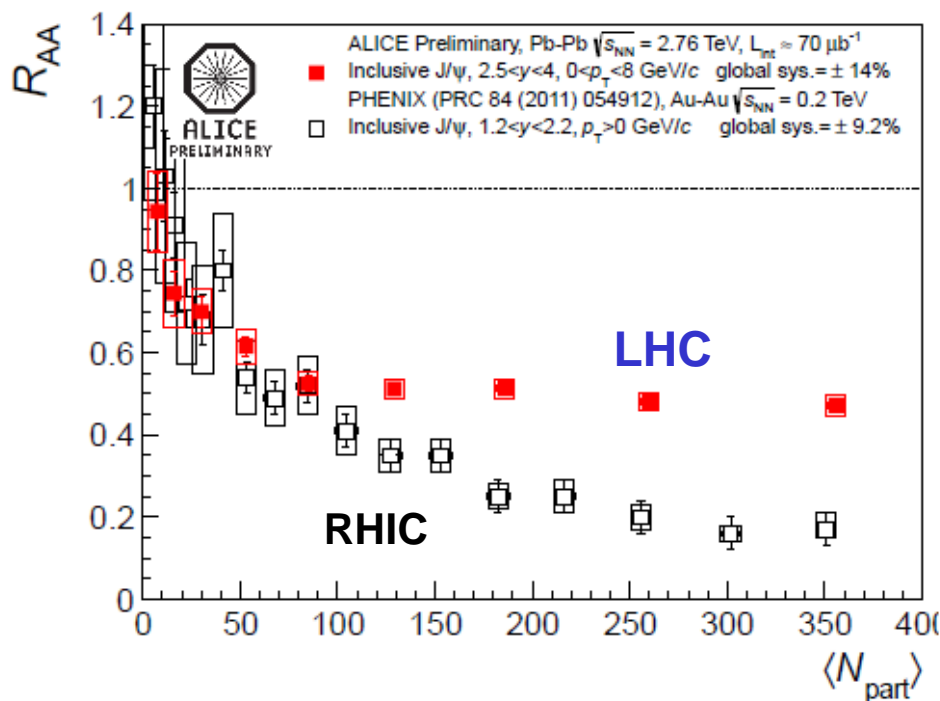
$$V(r) = -\frac{4}{3} \frac{\alpha_s}{r} e^{-\frac{r}{\lambda_D}}$$



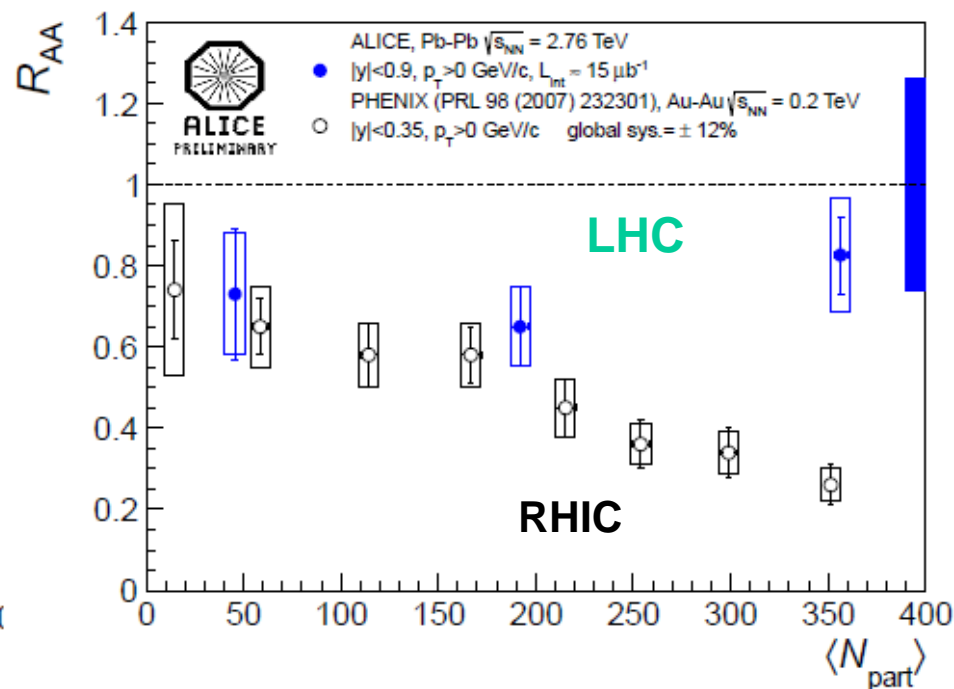


J/Ψ – production at LHC

Forward rapidity



Central rapidity

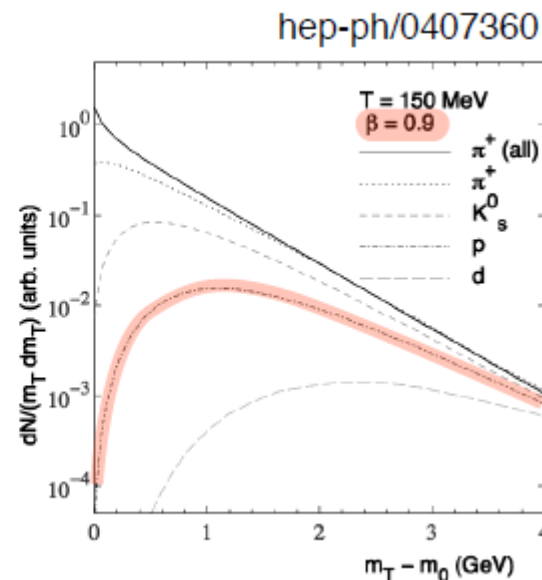
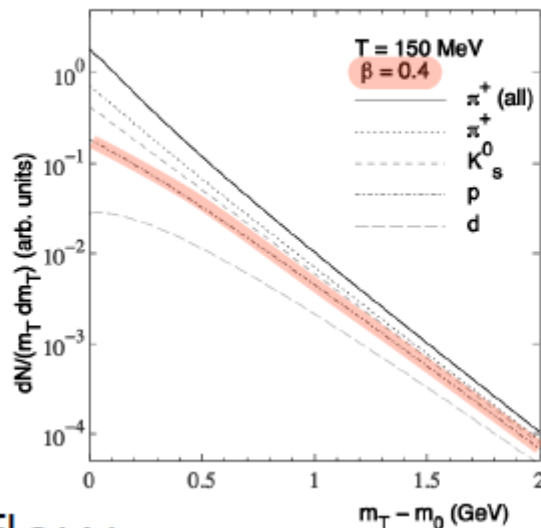
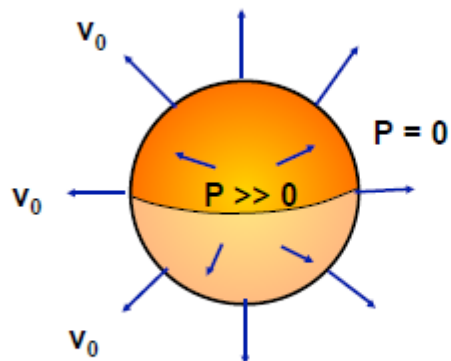


**J/Ψ – suppression much less pronounced at LHC ($\sqrt{s_{NN}} = 2.76 \text{ TeV}$)
as compared to RHIC ($\sqrt{s_{NN}} = 0.2 \text{ TeV}$).**

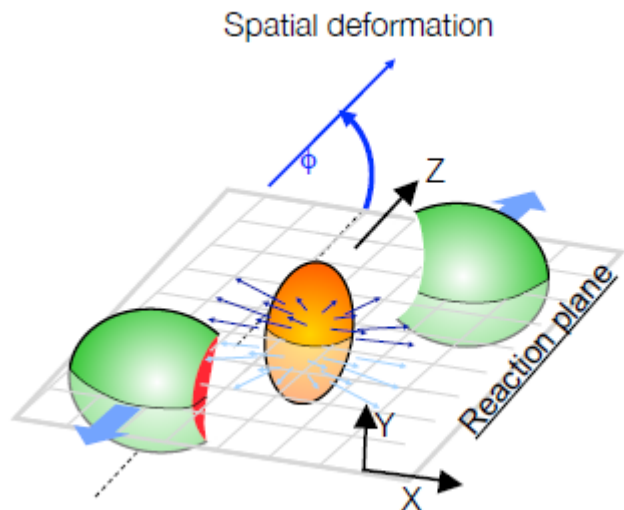


Collective flow

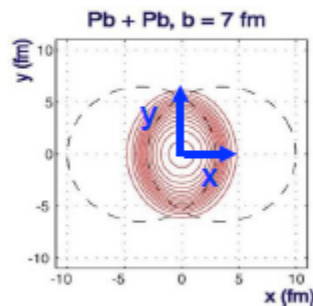
Isotropic (radial) flow



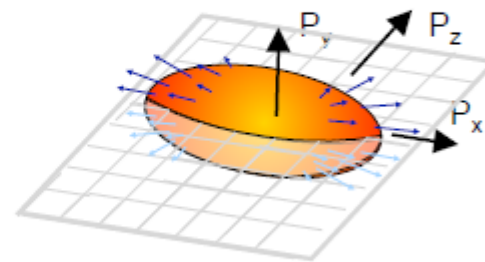
Anisotropic (elliptic) flow



Azimuthal (ϕ)
pressure gradients



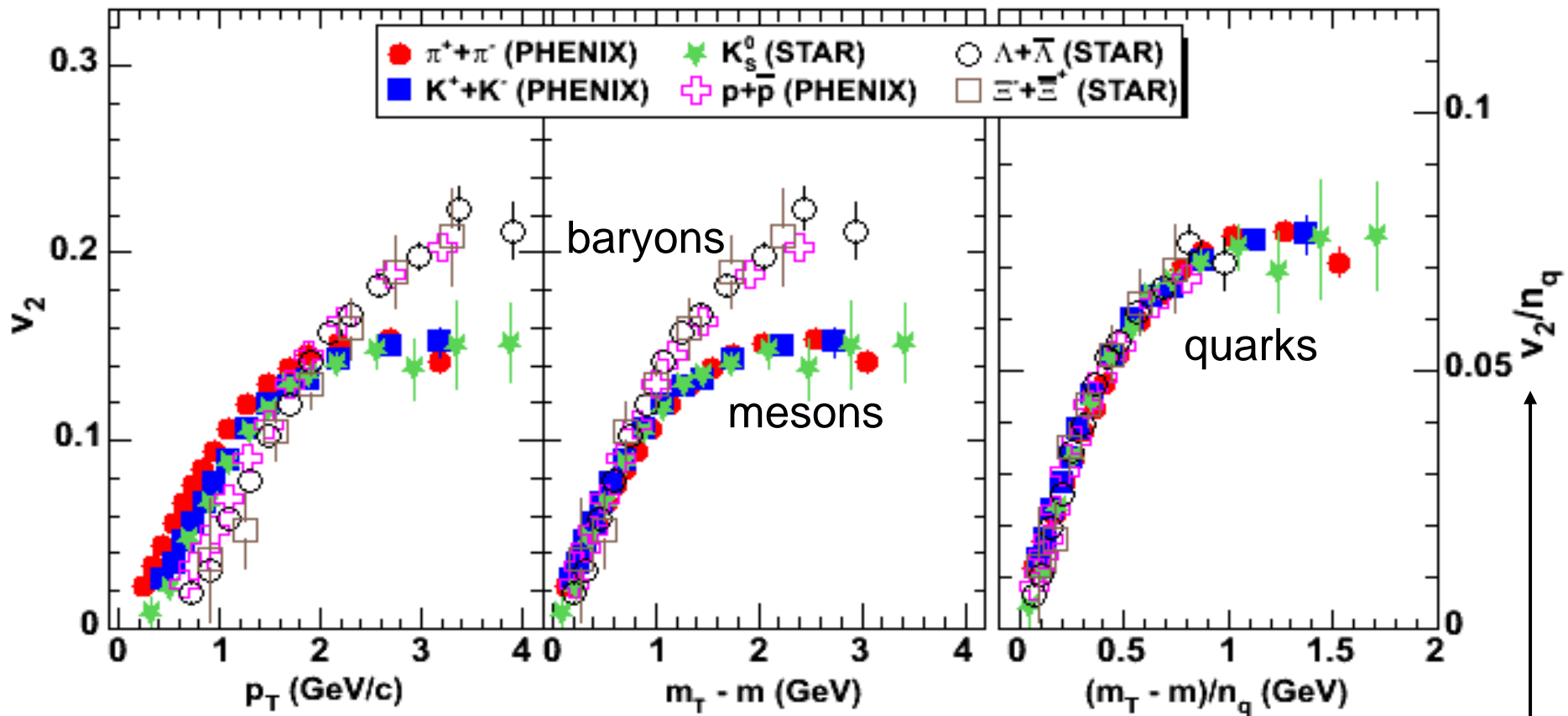
Anisotropic particle density



$$\frac{dN}{d\phi} \propto 1 + 2v_1 \cos[\phi - \Psi_1] + 2v_2 \cos[2(\phi - \Psi_2)] + 2v_3 \cos[3(\phi - \Psi_3)] + \dots$$



Scaling with Number of Quarks @ 200A GeV



mass ordering

both axes scaled by number of constituent quarks

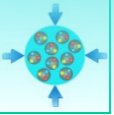
quarks have v_2 before hadronization

S. Voloshin, QM02, 379c (2003)

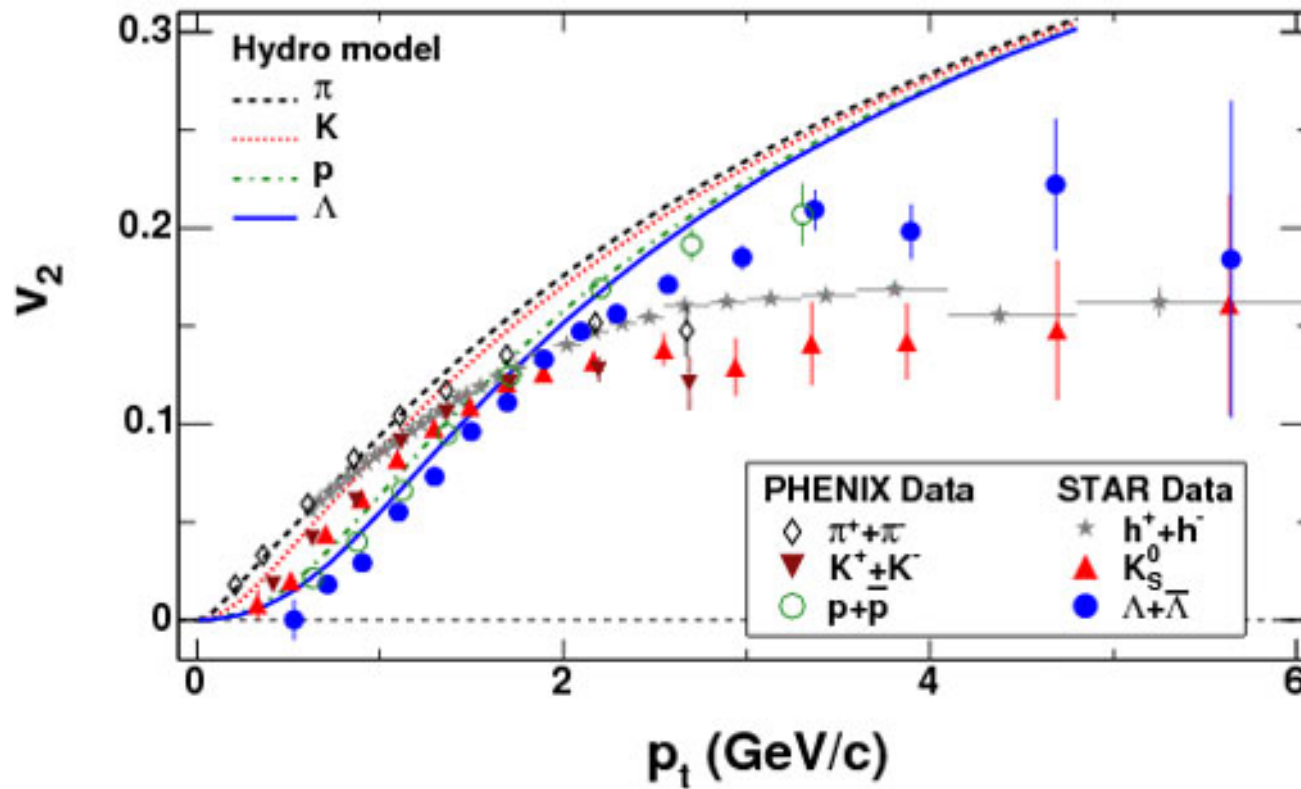
STAR, PRL **95**, 122301 (2005) PHENIX, PRL **98**, 162301 (2007)

$n_q = 2$ for mesons

$n_q = 3$ for baryons



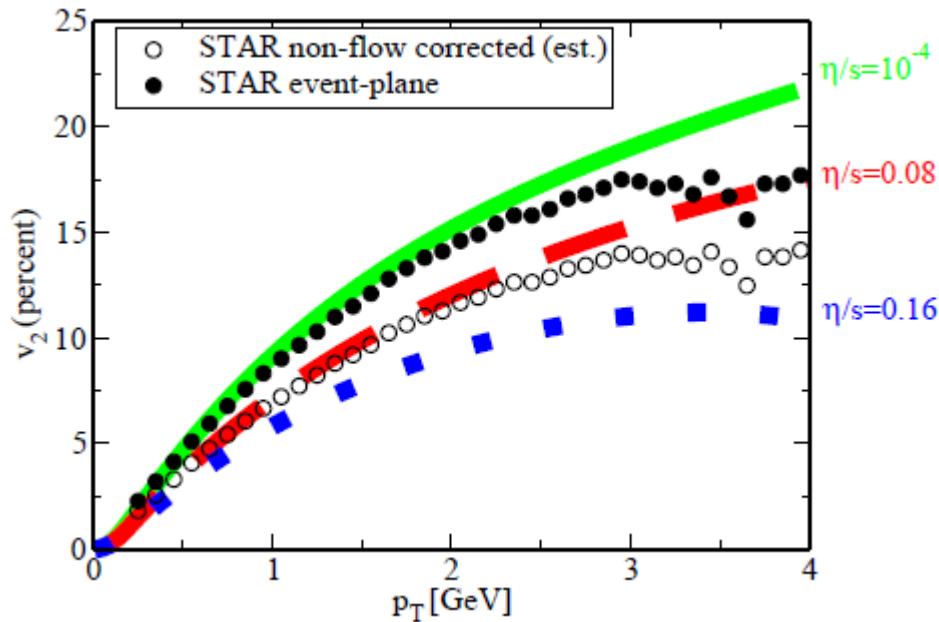
Hydrodynamical description of flow pattern





Perfect liquid

M.Luzum, P. Romatschke, arXiv:0804.4015



Hydrodynamics

local thermal equilibrium
mean free path \ll system size
successfully describes flow data.

Magnitude of flow can be tuned by
viscosity / entropy density

Extracted η/s – value is much smaller
than for any other known substance:

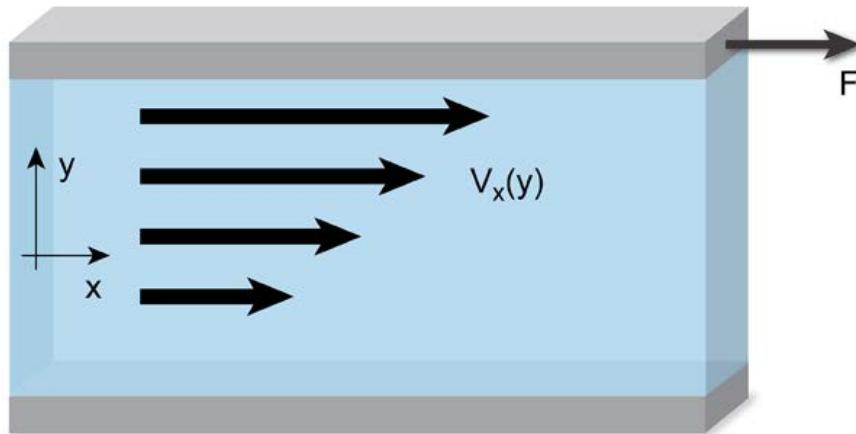
at T_c :	He	0.8
	H ₂ O	2.1



Viscosity and fluidity

T. Schäfer, Physics 2, 88 (2009)

Shear viscosity η



Friction force / unit area:

$$\frac{F}{A} = \eta \nabla_y v_x$$

	η (Pa . s)
LHe	$2 \cdot 10^{-15}$
sQGP	$5 \cdot 10^{+11}$

Fluidity \leftrightarrow large Reynold number

$$\text{Re} = \left(\frac{mn}{\eta} \right) vL$$

mass density $m \cdot n$
length scale L

η / n has units of \hbar ,
 n is not conserved in relativistic fluid,
however: with entropy density s and $s / n \sim k_B$

$$\left(\frac{mn}{\eta} \right) \rightarrow \frac{\eta}{s} \left[\frac{\hbar}{k_B} \right]$$

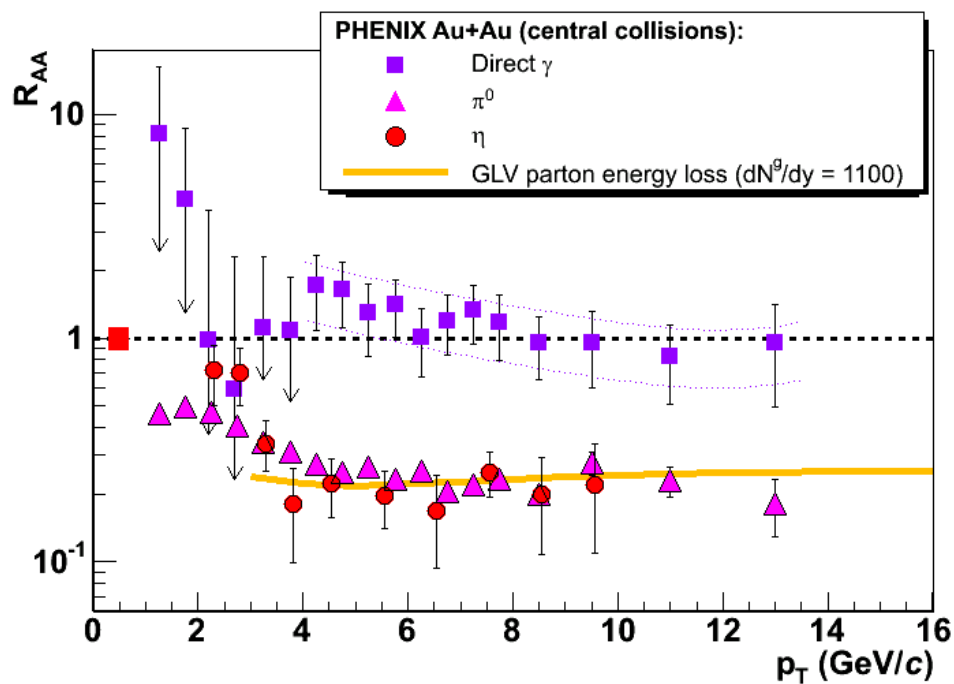


Nuclear modification factor R_{AA}

K. Reygers, QM2008

Compare data from heavy – ion reaction to scaled proton - proton data:

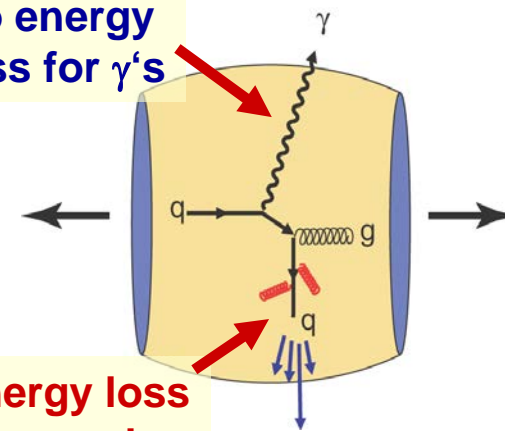
“Jet – quenching”



$$R_{AA} = \frac{\left. \frac{d\sigma}{dp_t} \right|_{A+A}}{N_{coll} \cdot \left. \frac{d\sigma}{dp_t} \right|_{p+p}}$$

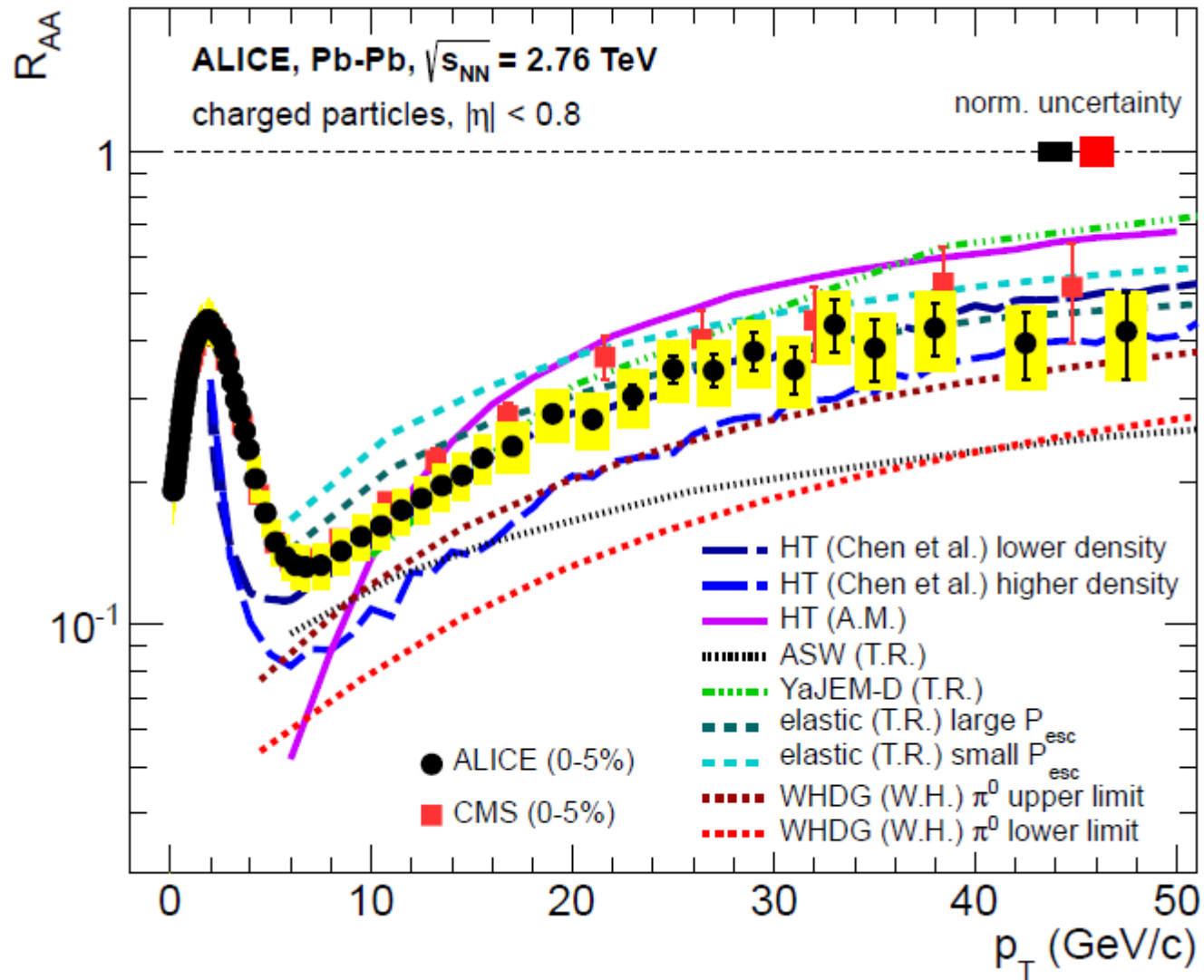
No energy loss for γ 's

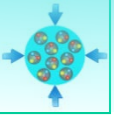
energy loss for q and g



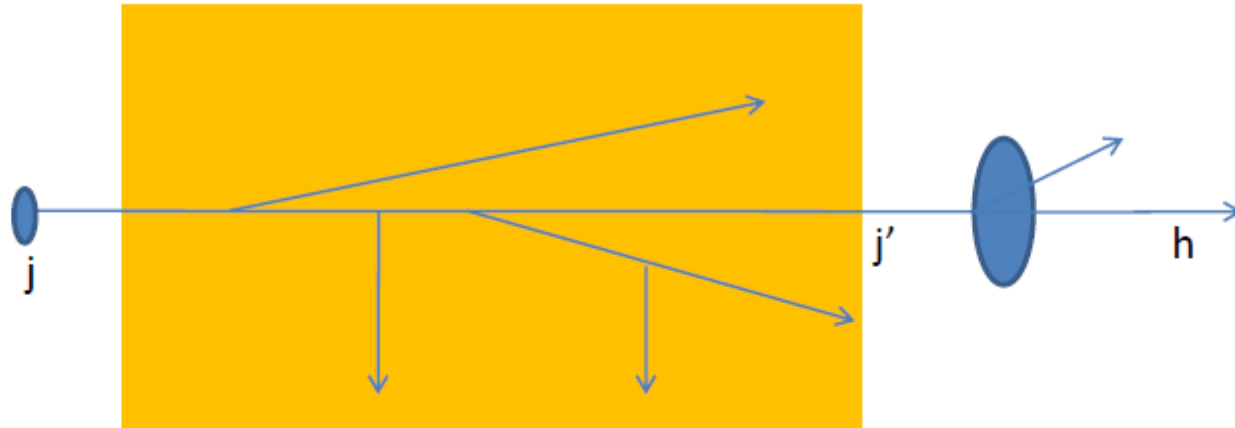
Jet quenching at the LHC

ALICE, arXiv:1208.2711
PLB 720, 52

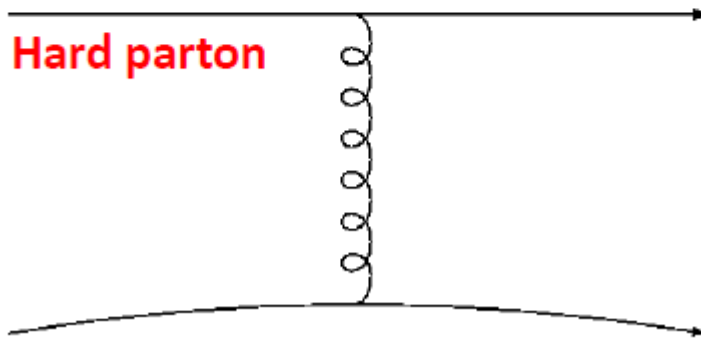




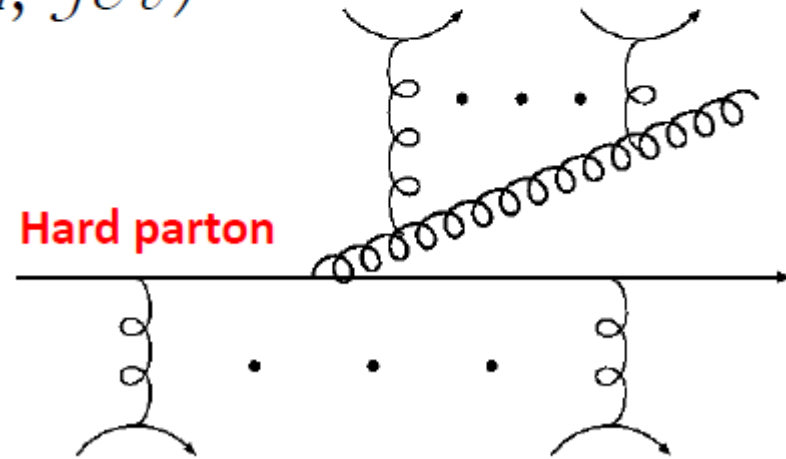
Energy loss of partons in QGP



$$P_{j \rightarrow j'}(\text{medium, jet})$$

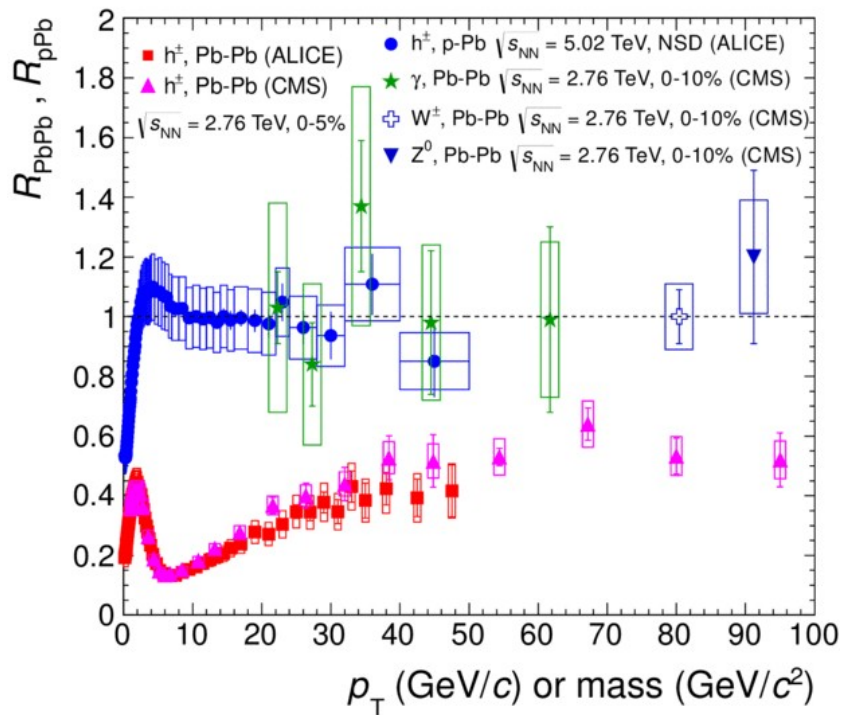


Elastic (collisional)

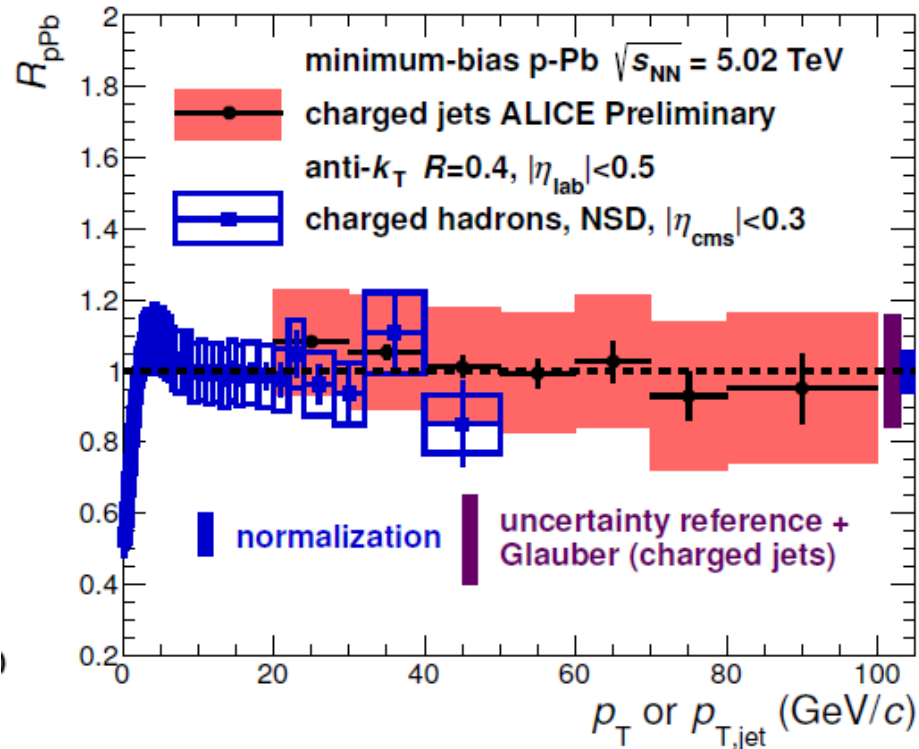


Inelastic (radiative)

Control experiment: p + Pb



ALI-PUB-75263



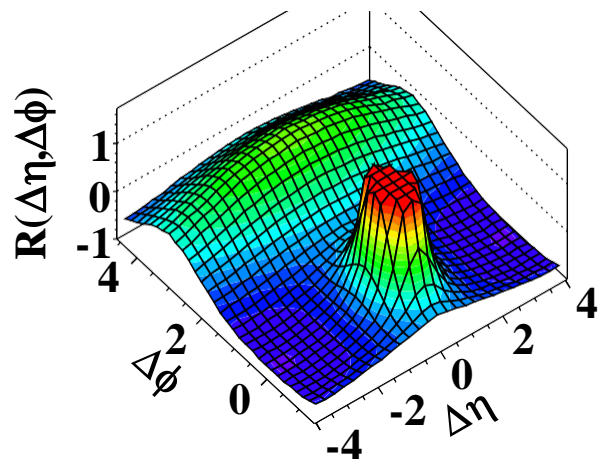
ALI-PREL-80555



2 – particle correlation functions

pp

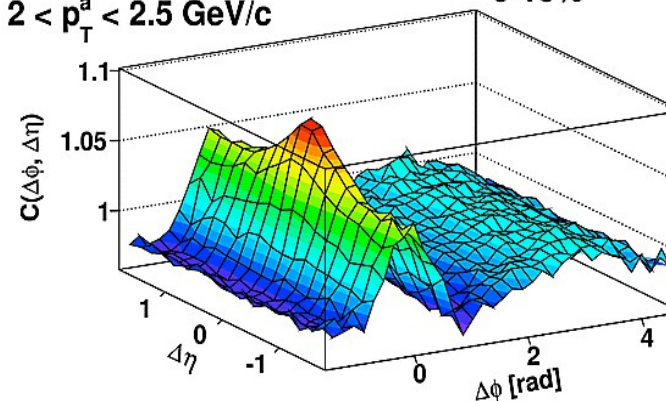
(b) CMS MinBias, $1.0 \text{ GeV}/c < p_T < 3.0 \text{ GeV}/c$



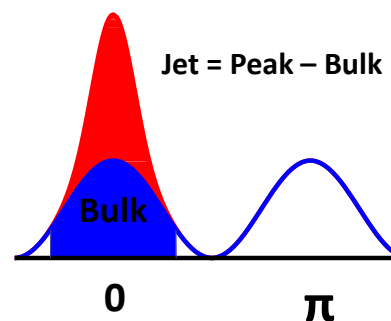
AA

$3 < p_T^t < 4 \text{ GeV}/c$
 $2 < p_T^a < 2.5 \text{ GeV}/c$

Pb-Pb 2.76 TeV
0-10%



ALI-PUB-14107

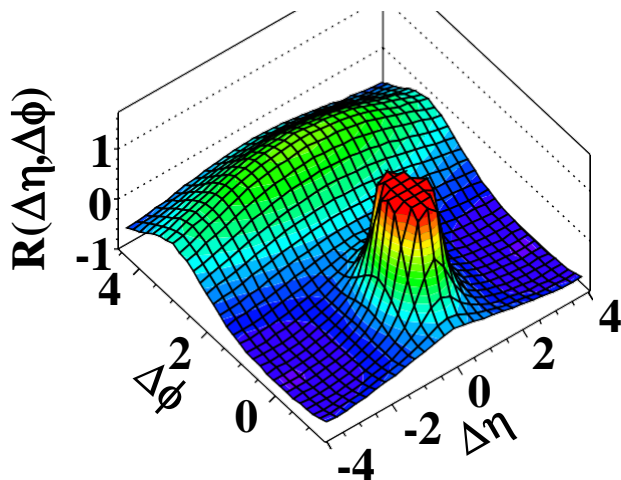




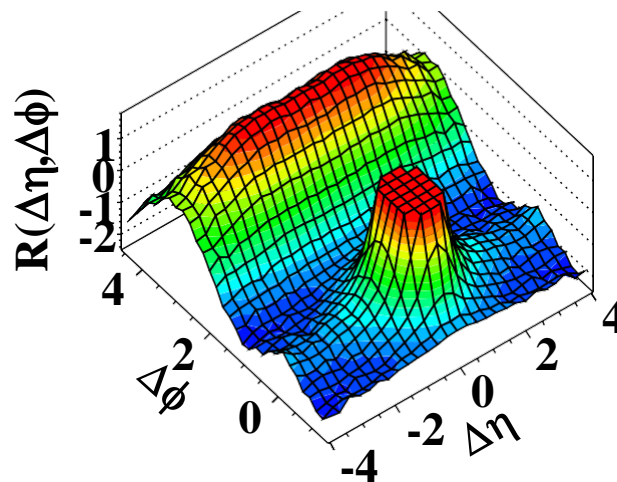
LHC discovery

JHEP 1009:091,2010
arXiv:1009.4122

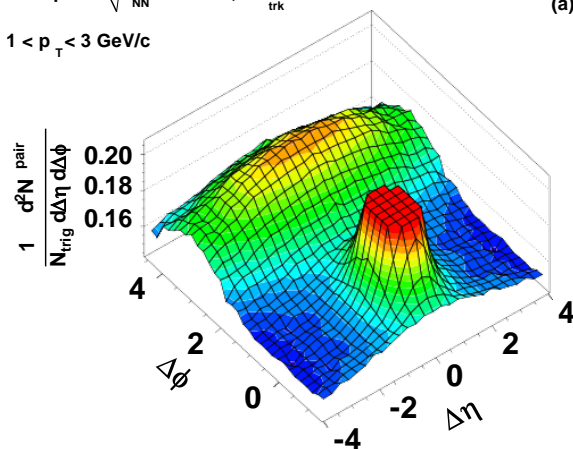
(b) CMS MinBias, $1.0 \text{ GeV}/c < p_T < 3.0 \text{ GeV}/c$



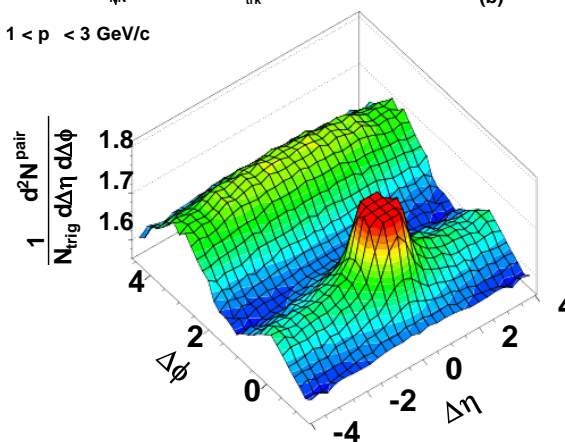
(d) CMS $N \geq 110$, $1.0 \text{ GeV}/c < p_T < 3.0 \text{ GeV}/c$



CMS pPb $\sqrt{s_{NN}} = 5.02 \text{ TeV}$, $N_{\text{trk}}^{\text{offline}} < 35$
 $1 < p_T < 3 \text{ GeV}/c$



(a) CMS pPb $\sqrt{s_{NN}} = 5.02 \text{ TeV}$, $N_{\text{trk}}^{\text{offline}} \geq 110$
 $1 < p_T < 3 \text{ GeV}/c$



PLB 718 (2013)
arXiv:1210.5482

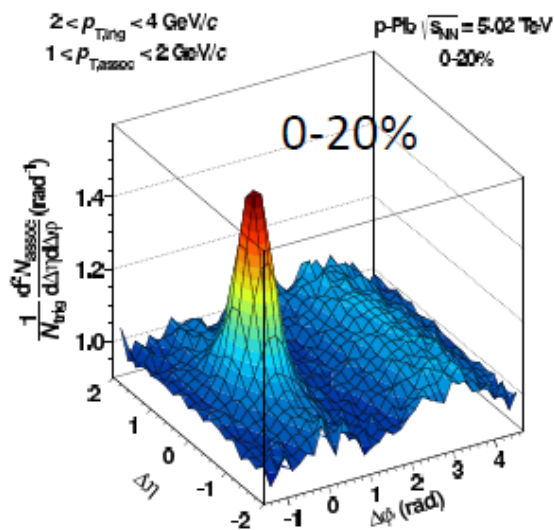
Nearside ridge structure in high multiplicity pp and pPb events !



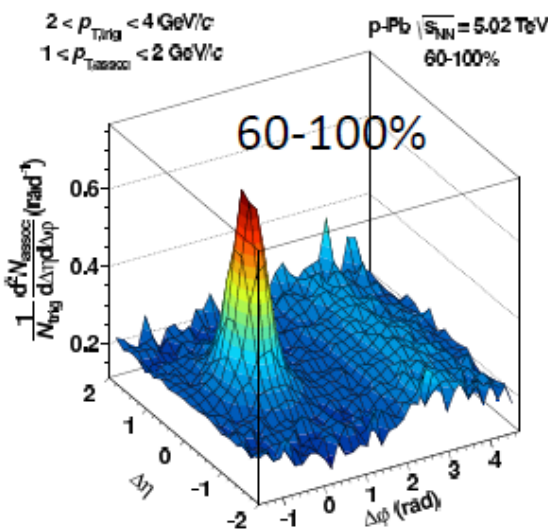
Double ridge structure in pPb

Subtraction of 2 – particle correlations measured in high – multiplicity and low – multiplicity events

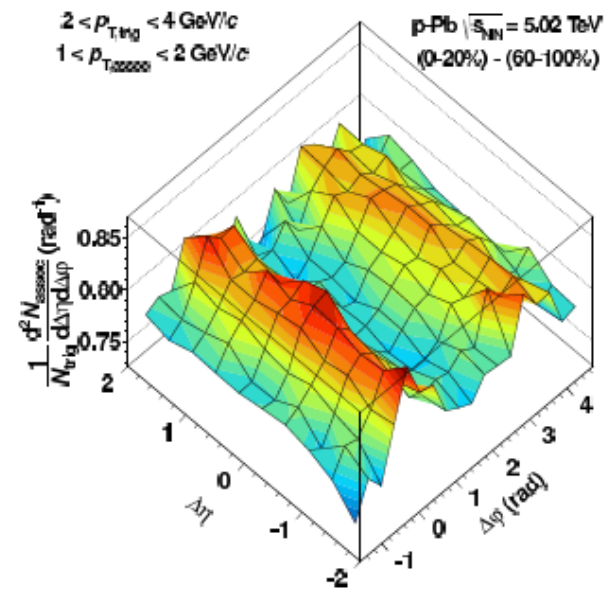
PLB 719 (2013)
arXiv:1212.2001



—



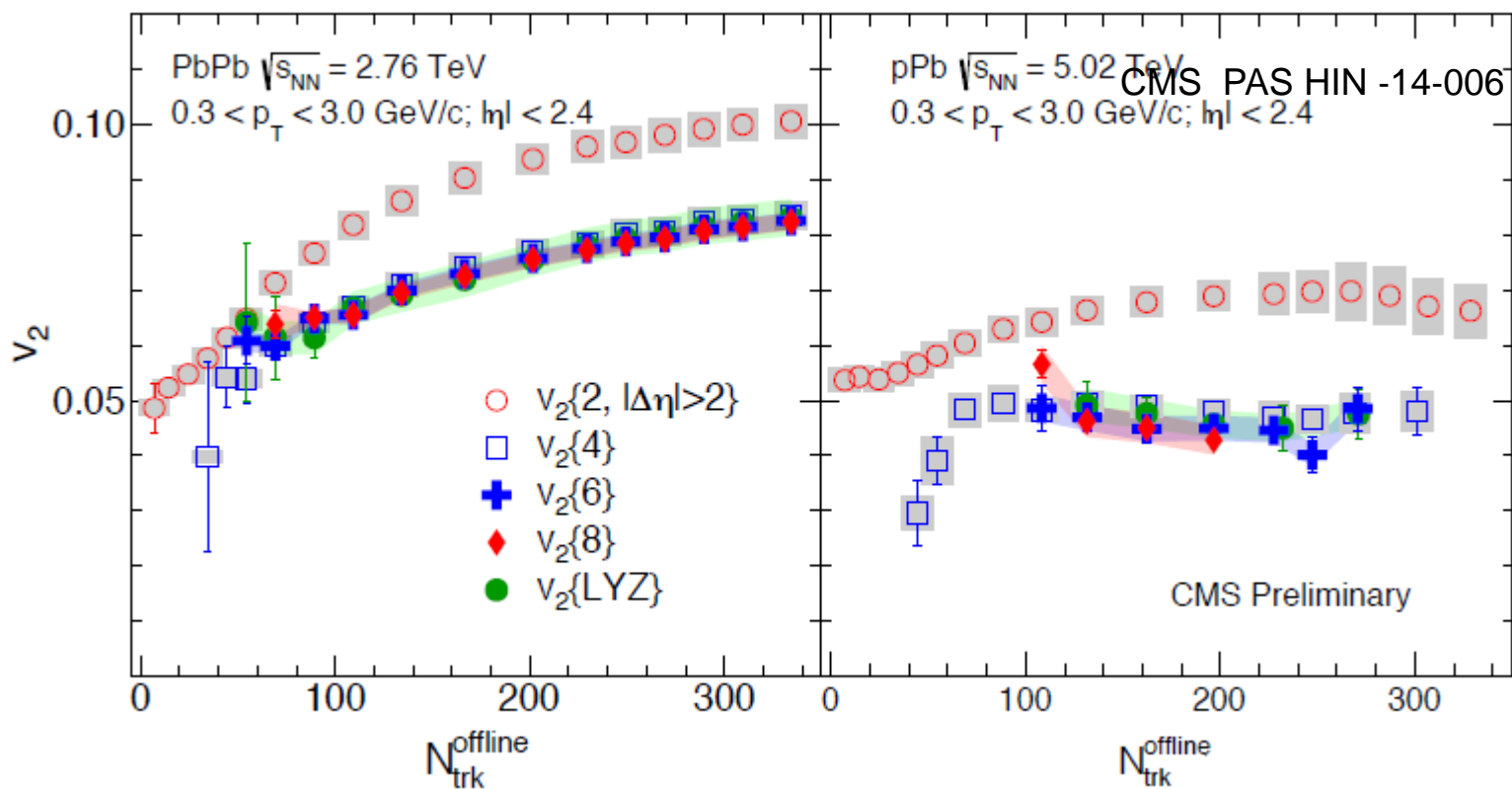
=



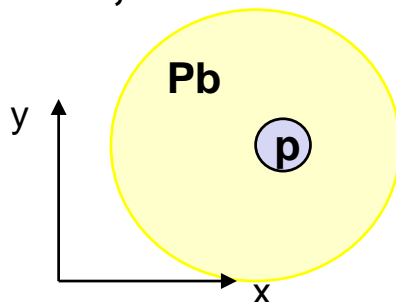


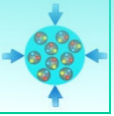
Multiparticle correlations in pPb

Higher order cumulants remove all non – flow effects.



Collective behavior in pPb observed, also at RHIC (STAR & PHENIX).
Where does it come from?





Back to phase transitions ...



Chiral symmetry of QCD

Decomposition of states (spinors) $\psi = \psi_R + \psi_L = \frac{1}{2}(1 + \gamma^5)\psi + \frac{1}{2}(1 - \gamma^5)\psi$

Decomposition of currents:

$$\begin{aligned} j &= \bar{\psi}\gamma^\mu\psi = (\bar{\psi}_R + \bar{\psi}_L)\gamma^\mu(\psi_R + \psi_L) \\ &= (\bar{\psi}_R\gamma^\mu\psi_R + \bar{\psi}_R\gamma^\mu\psi_L + \bar{\psi}_L\gamma^\mu\psi_R + \bar{\psi}_L\gamma^\mu\psi_L) \\ &= (\bar{\psi}_R\gamma^\mu\psi_R + \bar{\psi}_L\gamma^\mu\psi_L) \end{aligned}$$

u,d,s – quarks are massless on QCD – scale (1GeV).

Consequences for QCD with massless quarks:

Dirac equation: $(i\gamma^\mu\partial_\mu - m)\psi = 0 \rightarrow i\gamma^\mu\partial_\mu\psi = 0$

Interaction with vector field conserves chirality (\rightarrow QED): $i\gamma^\mu D_\mu\psi_L = 0$

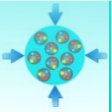
$$i\gamma^\mu D_\mu\psi_R = 0$$

L and R handed states do not interact.

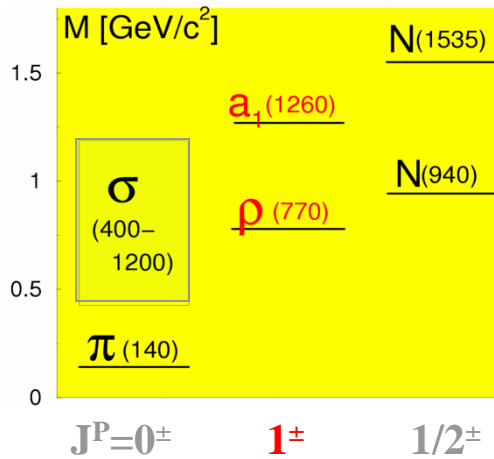
New Symmetry group:

$$SU(3)_L \times SU(3)_R$$

Current quark mass breaks this symmetry explicitly.



Spontaneous chiral symmetry breaking



Exact chiral symmetry:

all hadrons should exist in 2 degenerate parity states!

Parity operator $P = \gamma^0$:

$$P_R = \frac{1}{2}(1 + \gamma^5)$$

$$P_L = \frac{1}{2}(1 - \gamma^5)$$

$$P |q_R\rangle = |q_L\rangle$$

$$P |q_L\rangle = |q_R\rangle$$

Construct: $|\psi_\pm\rangle = \frac{1}{\sqrt{2}}(|q_R\rangle \pm |q_L\rangle)$

$$P |\psi_+\rangle = + |\psi_+\rangle$$

$$P |\psi_-\rangle = - |\psi_-\rangle$$

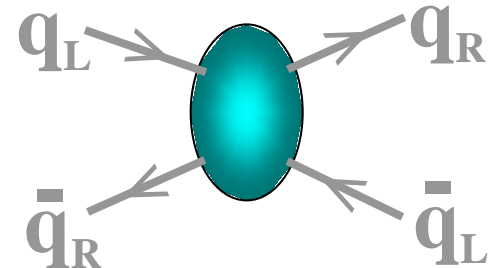
These 2 states should have the same energy / mass.

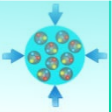
This feature is not observed in nature,

Mass difference between chiral partners much larger than current quark mass difference

⇒ chiral symmetry is spontaneously broken.

$$\langle \bar{q}q \rangle = \langle \bar{q}_L q_R + \bar{q}_R q_L \rangle \neq 0$$





Analogy: magnetism \leftrightarrow QCD

Heisenberg magnet (rotationally invariant):

$$H_{\text{int}} = g \sum_{i \neq j} \vec{s}_i \cdot \vec{s}_j$$

Excitation modes: spin waves = magnons

Excitation spectrum is gapless.

(infinitely long wavelength corresponds to rotation of whole matter block, rotation without external field does not cost energy)

Ground state characterized by macroscopic magnetisation M

$$\vec{M} = \langle \vec{S}_i \rangle$$

M is modified by external magnetic field B :

$$H_{\text{int}} = g \sum_{i \neq j} \vec{s}_i \cdot \vec{s}_j + \vec{B} \cdot \sum_i \vec{s}_i$$

B breaks rotational invariance explicitly.

Due to presence of B is excitation spectrum no longer gapless.

$M=M(T)$, M vanishes above critical temperature. Rotational symmetry is restored.

M is the order parameter of phase transition.

QCD in chiral limit ($m_q=0$)

**Hadrons in QCD vacuum
Massless Goldstone bosons**

Quark condensate $\langle q\bar{q} \rangle$

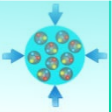
$$\langle \bar{q}q \rangle \approx -(240 \text{ MeV})^3 \times N_f$$

Current masses break chiral symmetry of QCD - Lagrangian explicitly

**Goldstone bosons acquire mass
(\rightarrow Pseudoscalar mesons,
Gell-Mann Oaks Renner relation)**

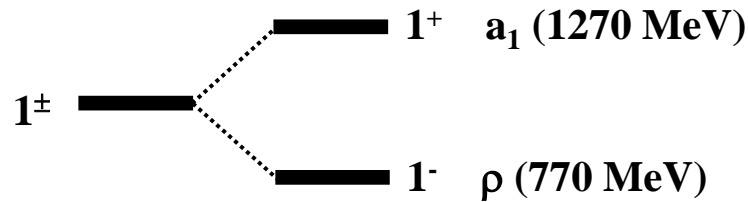
A phase transition to chirally symmetric state exists.

$\langle q\bar{q} \rangle$ is order parameter.



Consequences of Spontaneous Chiral Symmetry Breaking

1) All hadrons have well defined parity, chiral J^P doublets not observed.

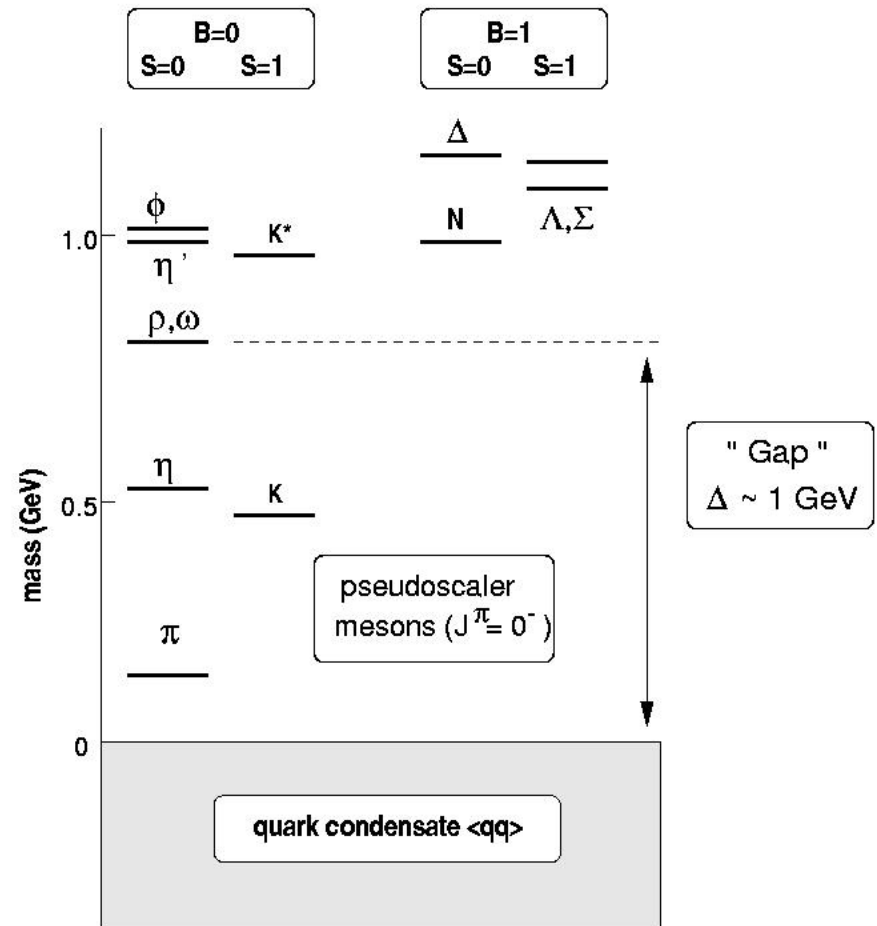


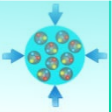
2) Chiral symmetry spontaneously broken, vacuum is filled with $q\bar{q}$ – condensate.

3) Goldstone theorem:
Any spontaneously broken continuous symmetry generates a massless boson (→ Goldstone bosons).

4) Characteristic mass scale of hadrons
1 GeV mass gap to quark condensate

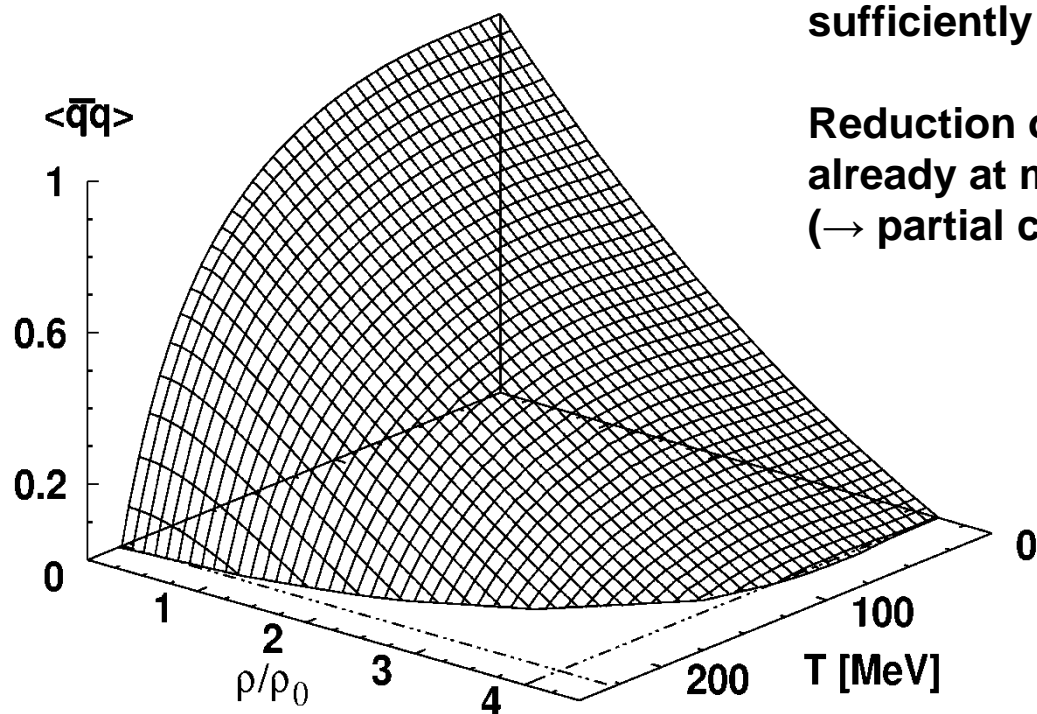
pseudoscalar mesons are
Pseudo - Goldstone bosons:
 $\pi, \eta,$ and K





Chiral symmetry restoration of QCD

Chiral Condensate



W.Weise, Prog. Theor. Phys. Suppl. 149 (2003) 1
 initially: S.Klimt et al., PLB 249, 386 (1990)

Chiral symmetry should be restored at sufficiently high temperatures and baryon densities.

Reduction of vacuum value should be visible already at moderate densities
 (→ partial chiral symmetry restoration)

Symmetry breaking pattern of Chiral Symmetry of QCD

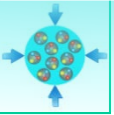
Gell-Mann-Oaks-Renner Relation:

$$m_\pi^2 f_\pi^2 = -\frac{1}{2}(m_u + m_d) \langle \bar{u}u + \bar{d}d \rangle + O(m_q^2)$$

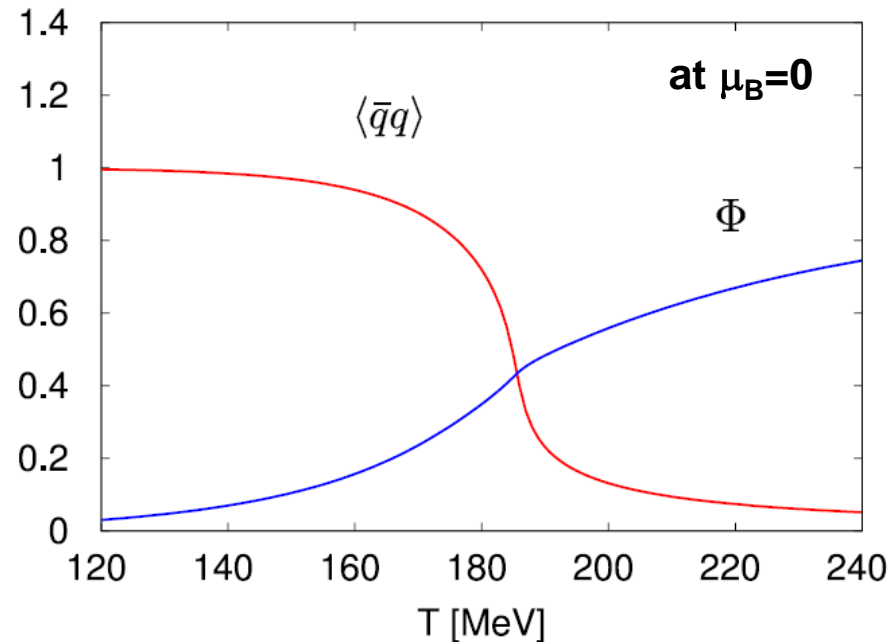
$$m_K^2 f_K^2 = -\frac{1}{2}(m_u + m_s) \langle \bar{u}u + \bar{s}s \rangle + O(m_s^2)$$

↑
 explicit symmetry breaking

↑
 spontaneous symmetry breaking



Order parameters in QCD



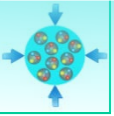
Order parameters:

chiral symmetry: Quark condensate $\langle \bar{q}q \rangle$

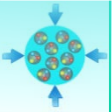
deconfinement: Polyakov loop $\Phi \sim e^{-\beta F_q}$

with $\beta=1/T$, F_q = free energy of free quark

Chiral and Polyakov loop order parameters show transition at the same temperature.



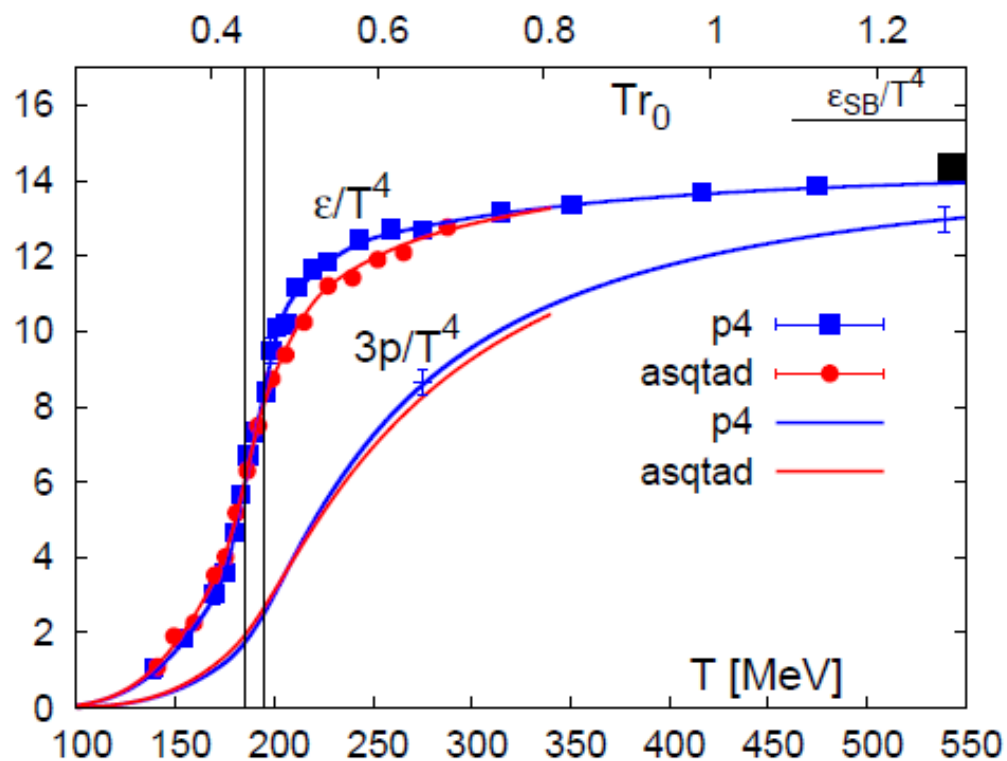
Lattice – QCD



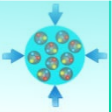
Lattice QCD equation – of – state

Owe Philipsen, arXiv:1207.5999 [hep-lat]

Calculations for $\mu_B=0$:

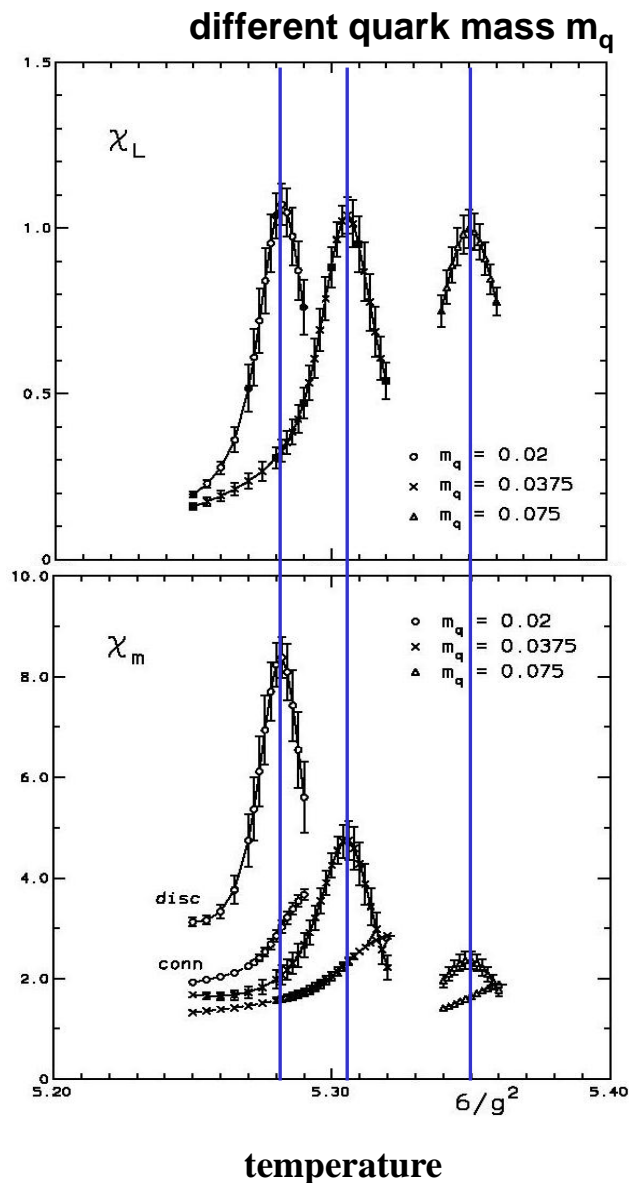


jump in energy density: $T_C \sim 170$ MeV, $\epsilon_C \sim 0.7$ GeV/fm³



The QCD phase transition

Polyakov loop
response function

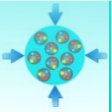


chiral susceptibility

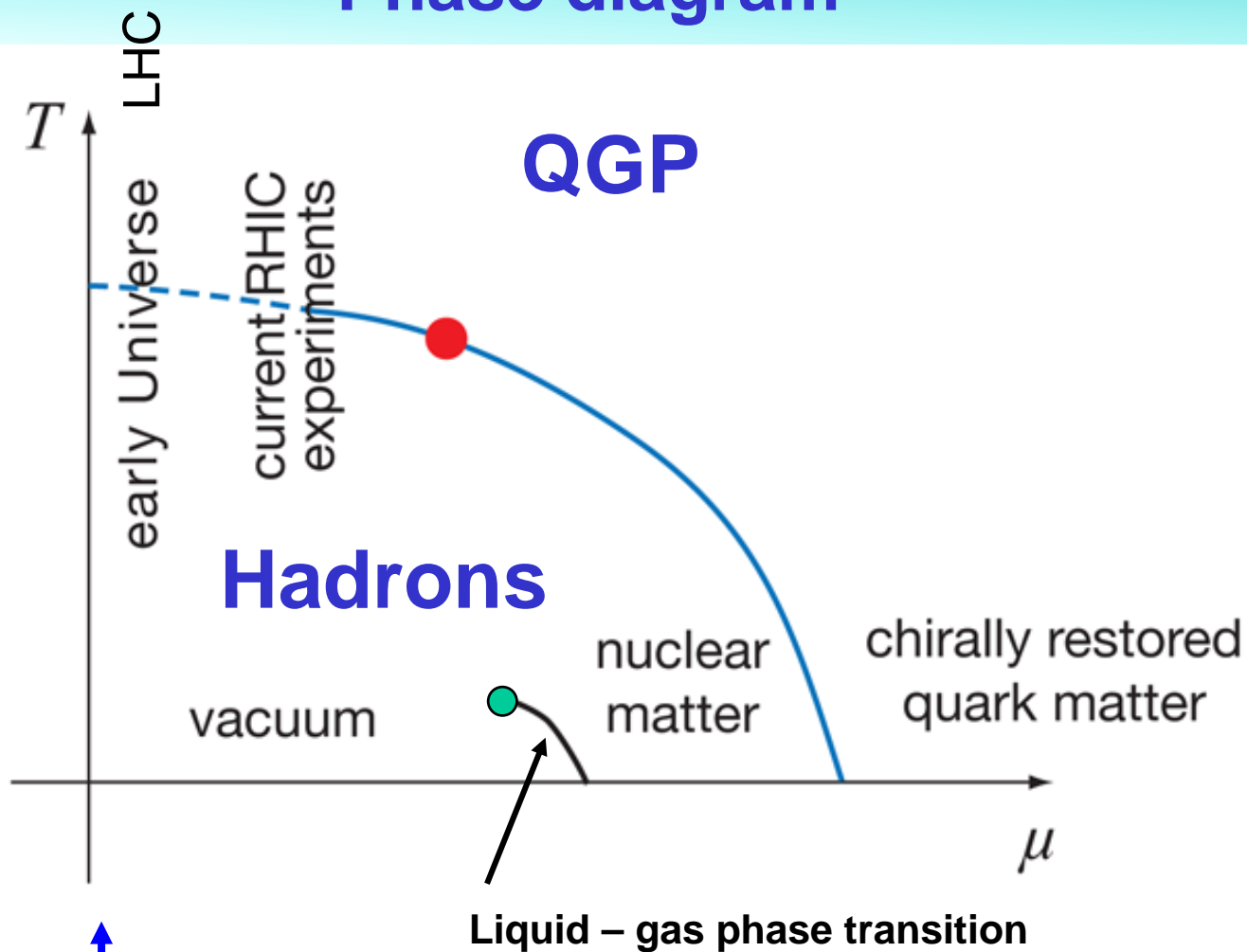
deconfinement

chiral symmetry restoration

Susceptibilities not divergent
-> rapid cross over

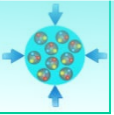


Phase diagram



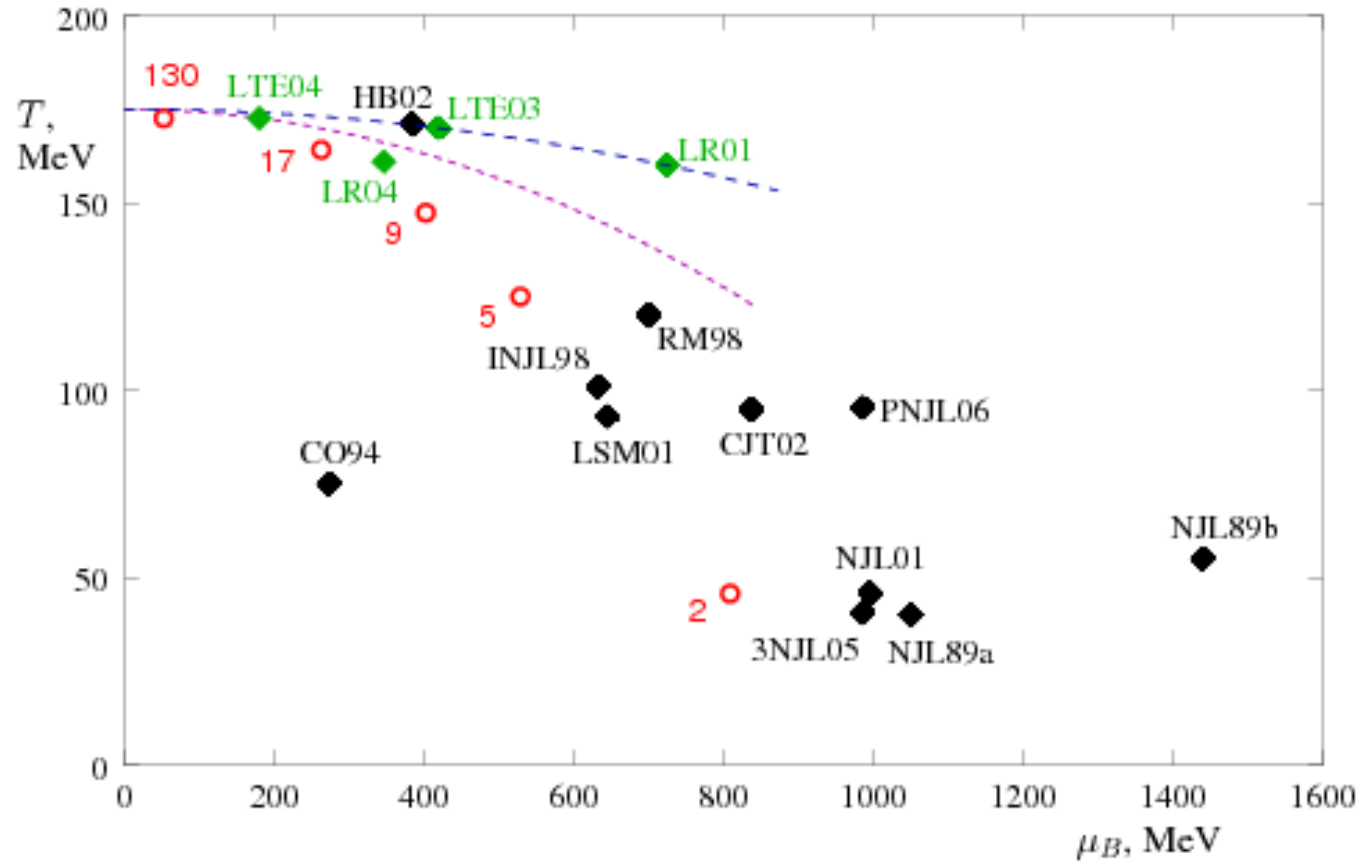
Lattice QCD applicable,
deconfinement & χ PT coincide

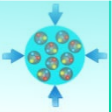
No firm predictions available
From L-QCD for $\mu > 0$,
→ QCD - inspired models



Location of the critical point

M.A. Stephanov, hep-lat/0701002

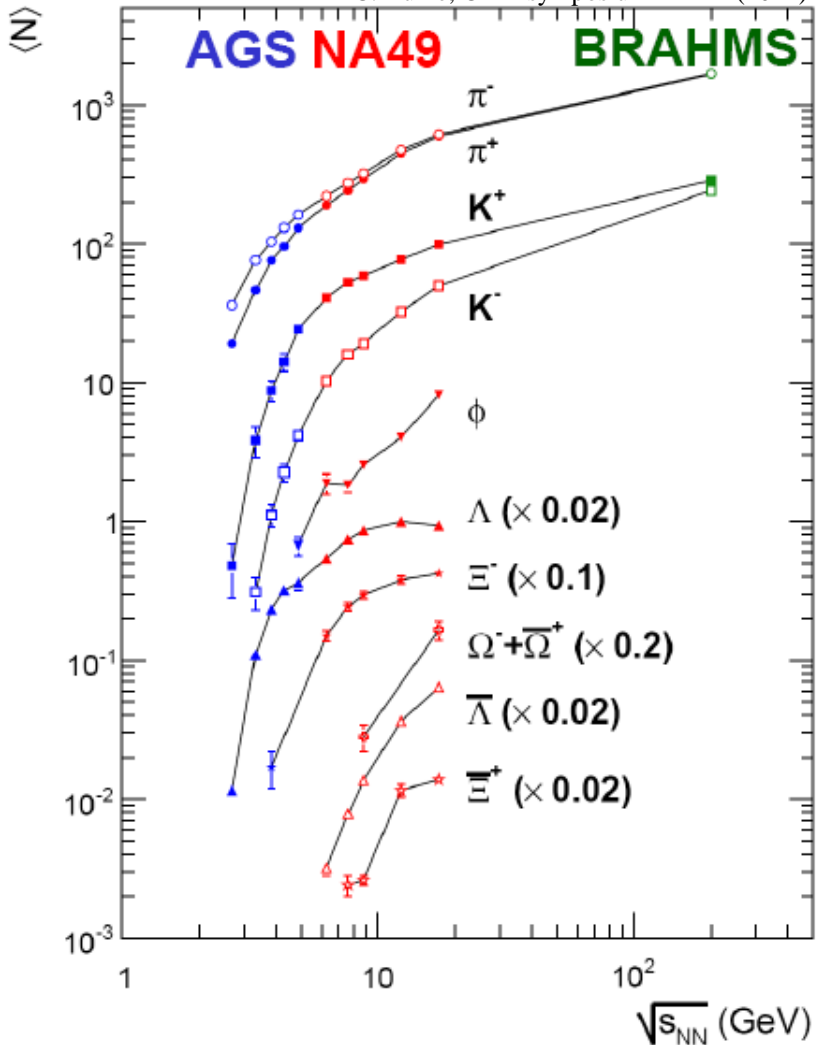




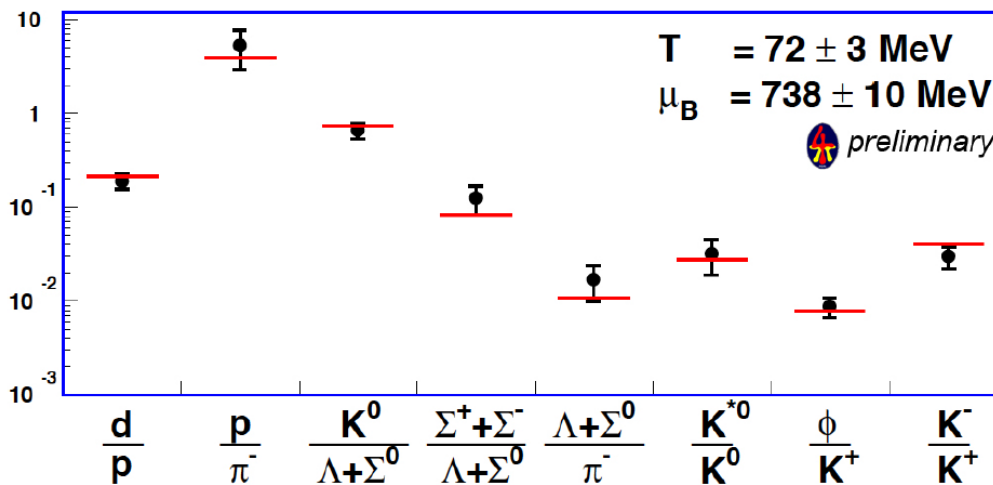
Excitation function of particle production

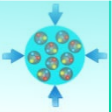
Central Au+Au collisions, 4 π yields

C.Blume, CBM symposium HZDR (2011)

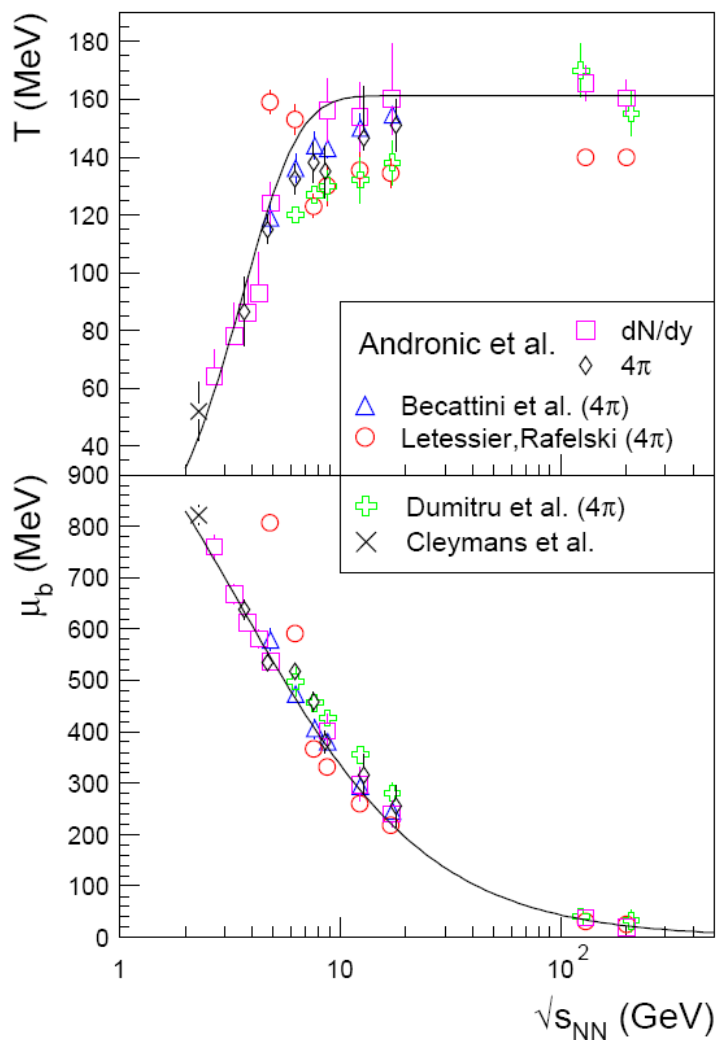


Low energies (SIS18): light systems only e.g. Al + Al at 1.91 AGeV





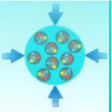
Excitation function of particle production



Limiting temperature

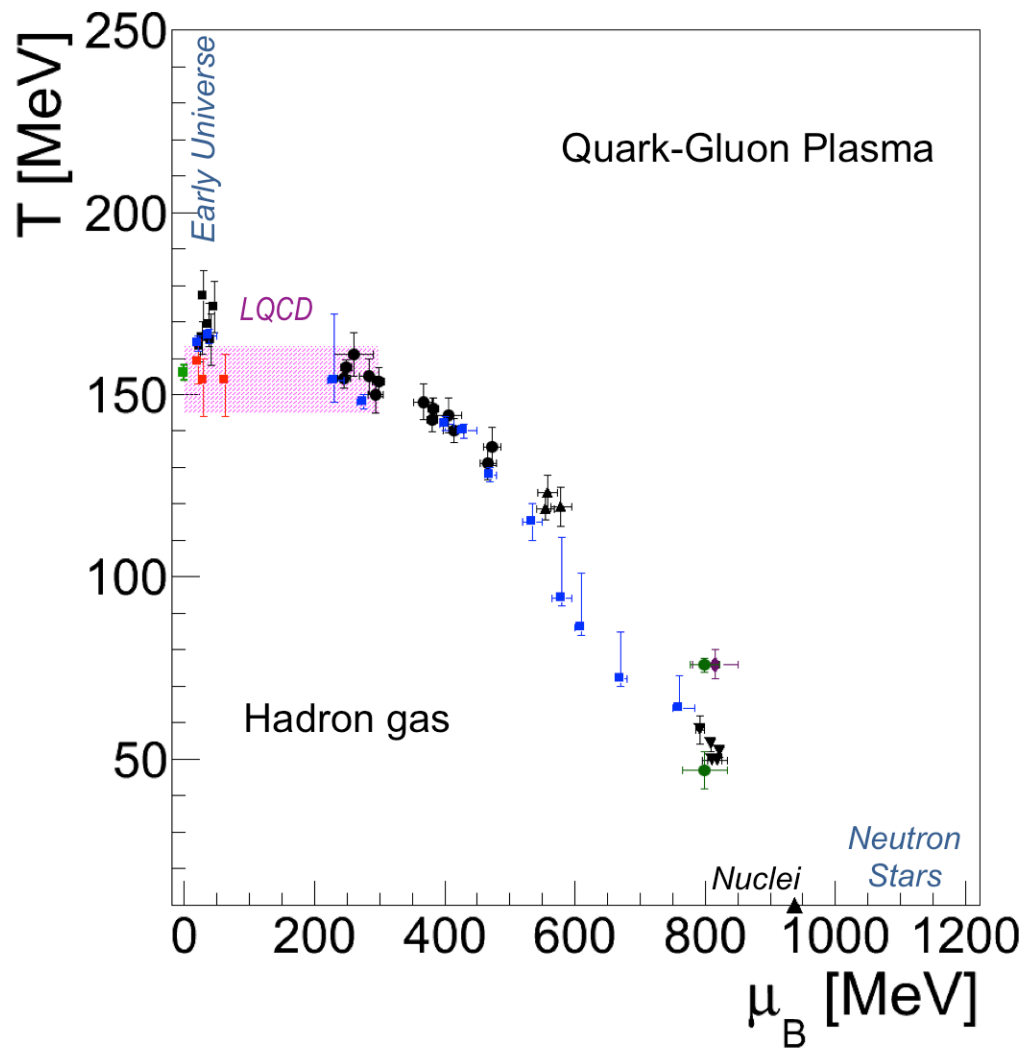
$$T = 161 \pm 4 \text{ MeV}$$

Note:
Limiting temperature first predicted
by
Hagedorn's bootstrap model (1965)



Chemical Freeze-out data

T. Galatyuk (HADES, CBM)



Errors include systematic errors (when given).

Data sources:

SHM : J. Cleymans: PRC 73 (2006) 034905,
A. Andronic PLB 673 (2009) 142

ALICE : J. Stachel, arXiv:1311.4662

STAR : PRC 79 (2009) 034909

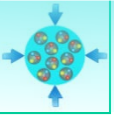
HADES : NPA 931 (2014)

FOPI : PRC 76 (2007) 052203

Lattice : $T_c(\mu_B) = 154(9) [1-0.0006(7)\mu_B^2]$ MeV

At lower energies canonical ensemble has to be used.

Equilibrium yields as signature for phase transition?



Equilibration times in hadronic matter

Naïve estimate:

3 collisions needed for equilibration (result from kinetic theory)

hadronic cross section: $\sigma = 40 \text{ mb} = 4 \text{ fm}^2$

strangeness production cross section: $\sigma = 400 \text{ } \mu\text{b} = 4 \cdot 10^{-2} \text{ fm}^2$

mean free path

$$\lambda = \frac{1}{n\sigma} = \frac{1}{0.17 \text{ fm}^{-3} \cdot 4 \text{ fm}^2} = 1.5 \text{ fm}$$

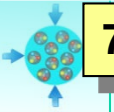
time between collisions

$$\tau = \lambda / c = 1.5 \text{ fm} / c$$

minimal equilibration time

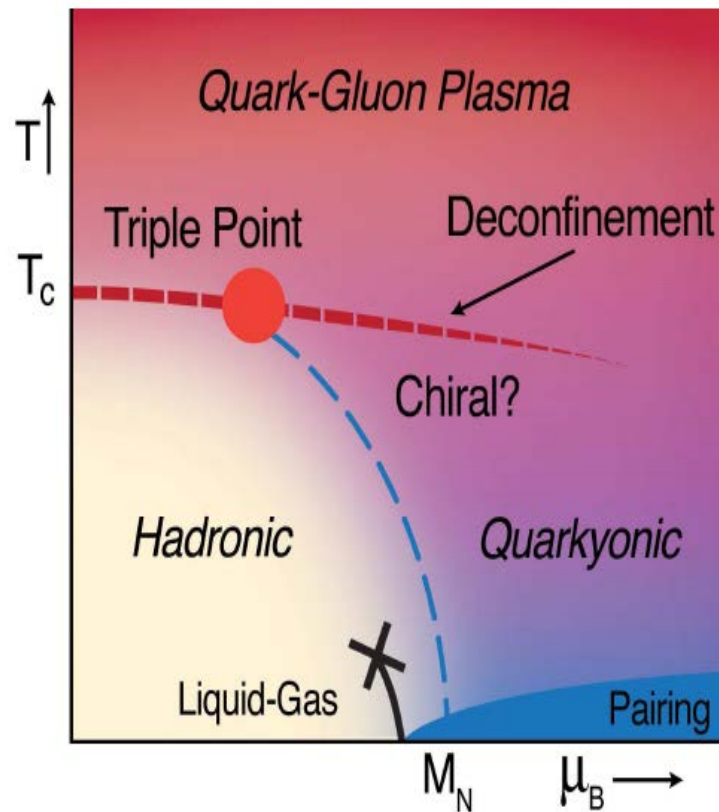
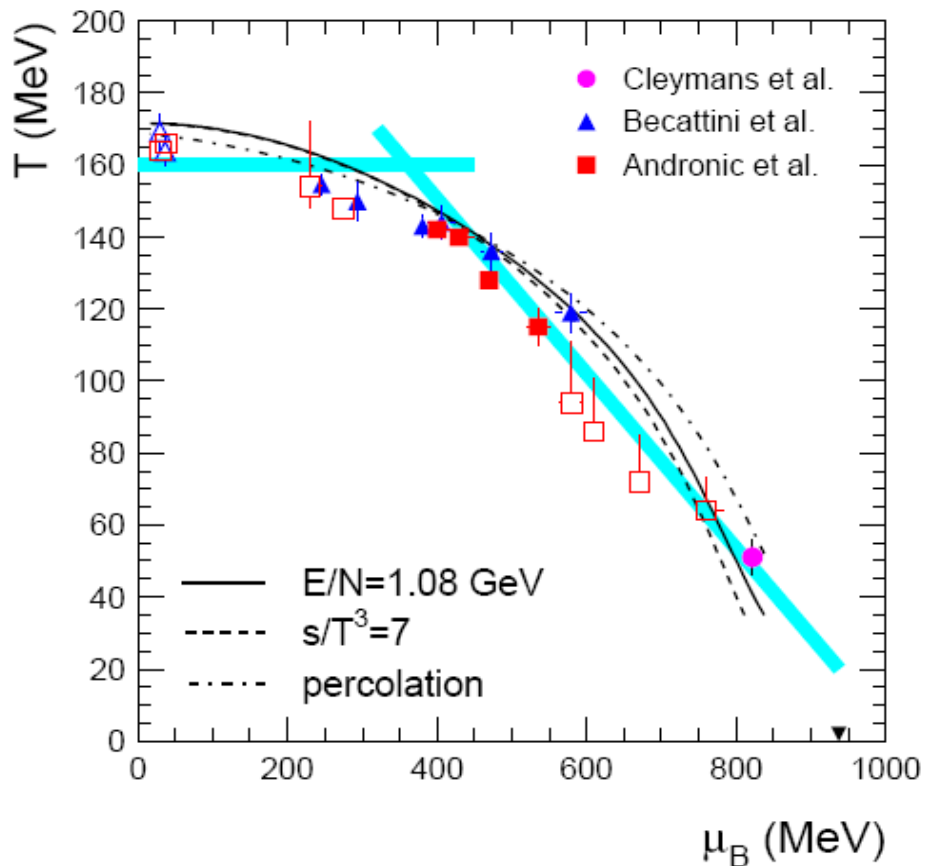
$$\tau_{eq}^{pion} = 4.5 \text{ fm} / c$$

$$\tau_{eq}^{strangeness} = 450 \text{ fm} / c$$



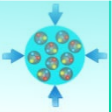
Chemical Freeze-out

A. Andronic et al., arXiv:0911.4806

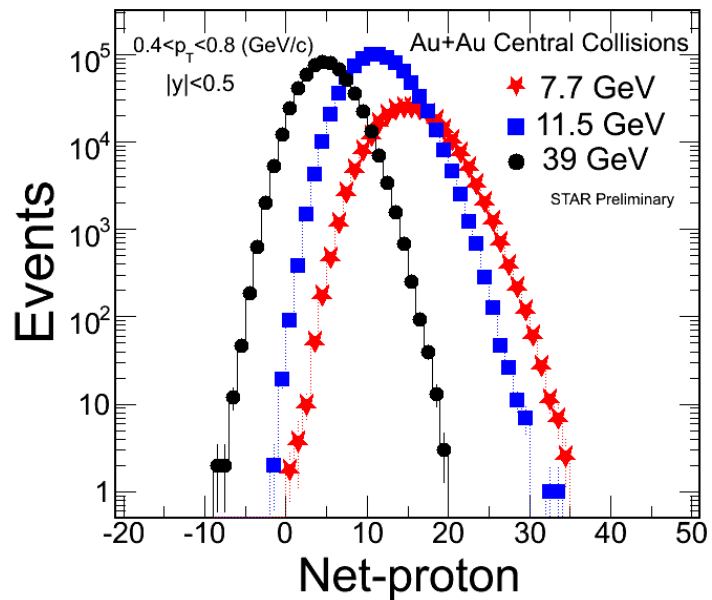
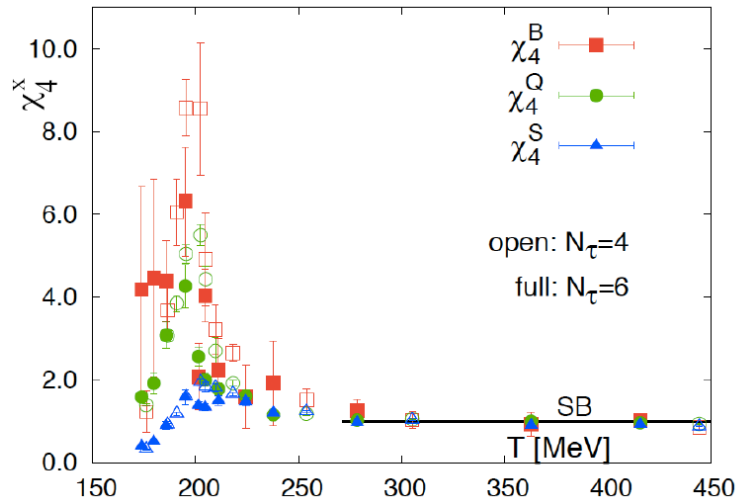


Speculation about the existence of a 1.order phase transition because of apparent thermal equilibrium.

Quarkyonic matter – confined objects with color - interaction



Higher Moments of Yield Distributions



- 1) Higher moments of conserved quantum numbers: **Q, S, B**, in high-energy nuclear collisions
- 2) Sensitive to critical point (ξ correlation length):

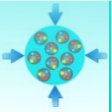
$$\langle (\delta N)^2 \rangle \approx \xi^2, \quad \langle (\delta N)^3 \rangle \approx \xi^{4.5}, \quad \langle (\delta N)^4 \rangle \approx \xi^7$$

- 3) Direct comparison with calculations at any order:

$$S\sigma \approx \frac{\chi_B^3}{\chi_B^2}, \quad K\sigma^2 \approx \frac{\chi_B^4}{\chi_B^2}$$

References:

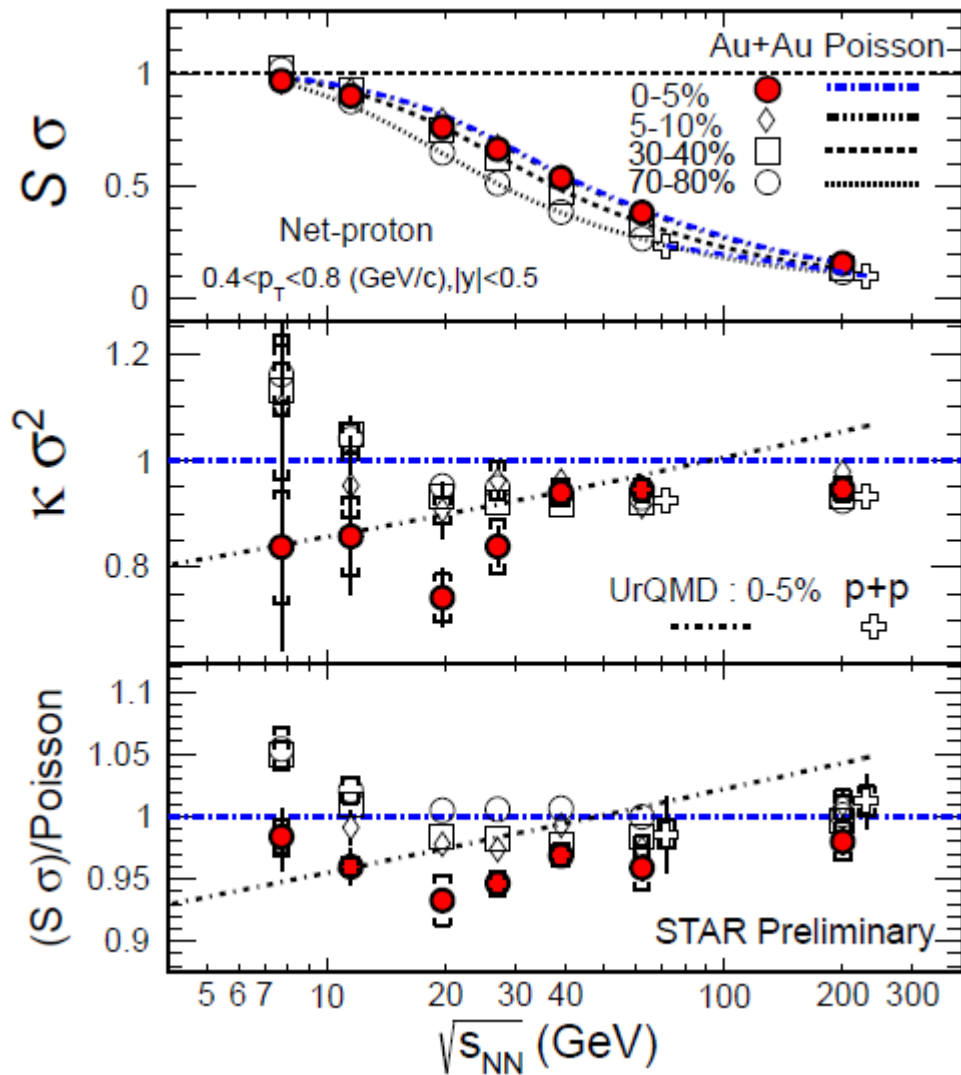
- STAR: *PRL*105, 22303(10); *ibid*, 032302(14)
- M. Stephanov: *PRL*102, 032301(09) // R.V. Gavai and S. Gupta, *PLB*696, 459(11) // F. Karsch et al, *PLB*695, 136(11) // S.Ejiri et al, *PLB*633, 275(06)
- A. Bazavov et al., *PRL*109, 192302(12) // S. Borsanyi et al., *PRL*111, 062005(13) // V. Skokov et al., *PRC*88, 034901(13)



Beam energy scan (STAR)

Xiaofeng Luo et al. (STAR), Nucl.Phys.A904 – 905 (2013) 911

Net – baryon number



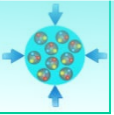
Higher order moments of $N_{p-\bar{p}}$

Skewness S

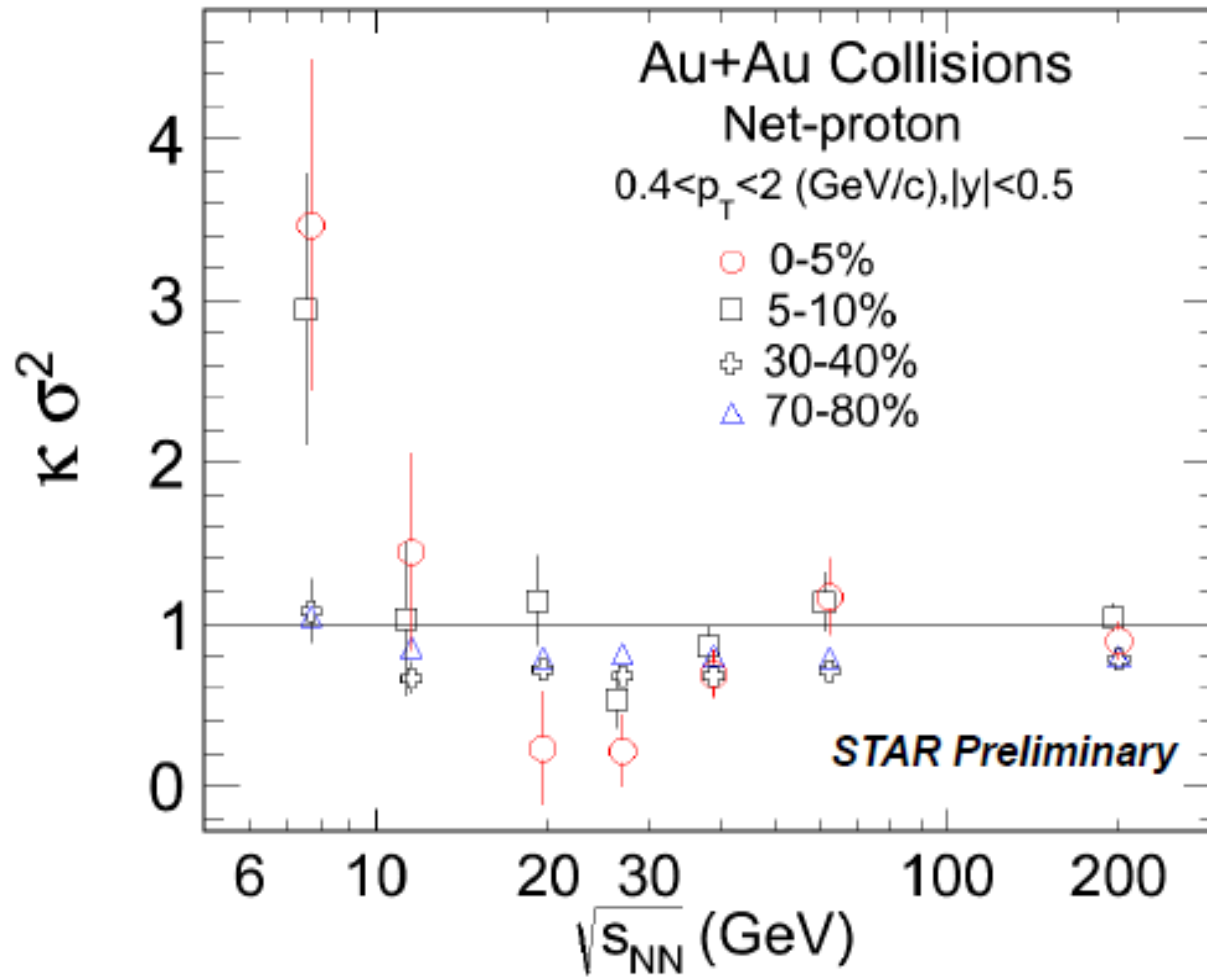
$$S = \frac{\left\langle \left(N_{p-\bar{p}} - \langle N_{p-\bar{p}} \rangle \right)^3 \right\rangle}{\left\langle \left(N_{p-\bar{p}} - \langle N_{p-\bar{p}} \rangle \right)^2 \right\rangle^{\frac{3}{2}}}$$

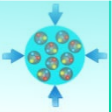
Kurtosis κ

$$\kappa = \frac{\left\langle \left(N_{p-\bar{p}} - \langle N_{p-\bar{p}} \rangle \right)^4 \right\rangle}{\left\langle \left(N_{p-\bar{p}} - \langle N_{p-\bar{p}} \rangle \right)^2 \right\rangle^2}$$



Excitation function of fluctuation

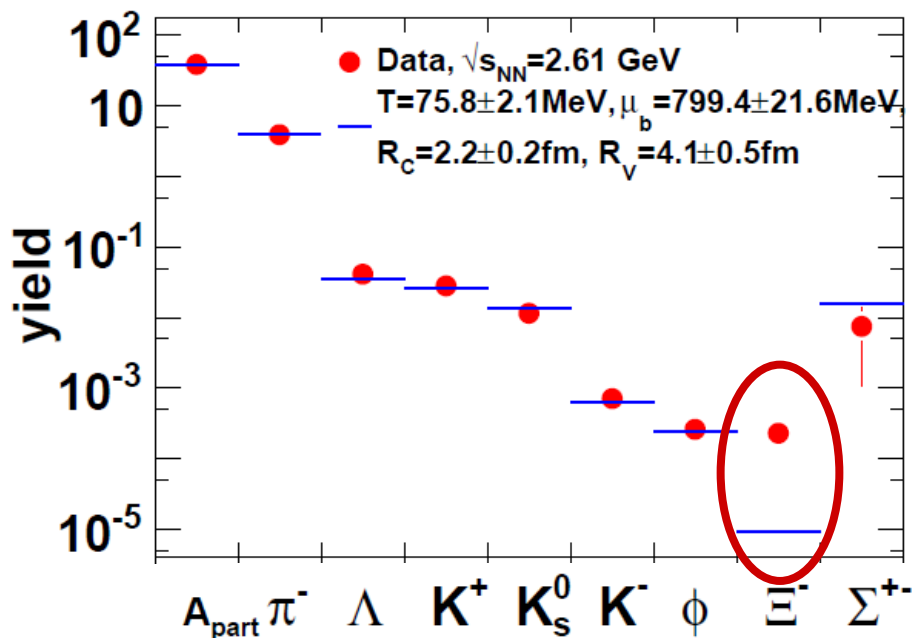




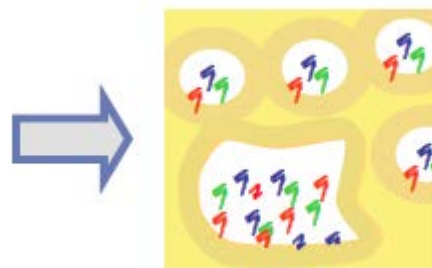
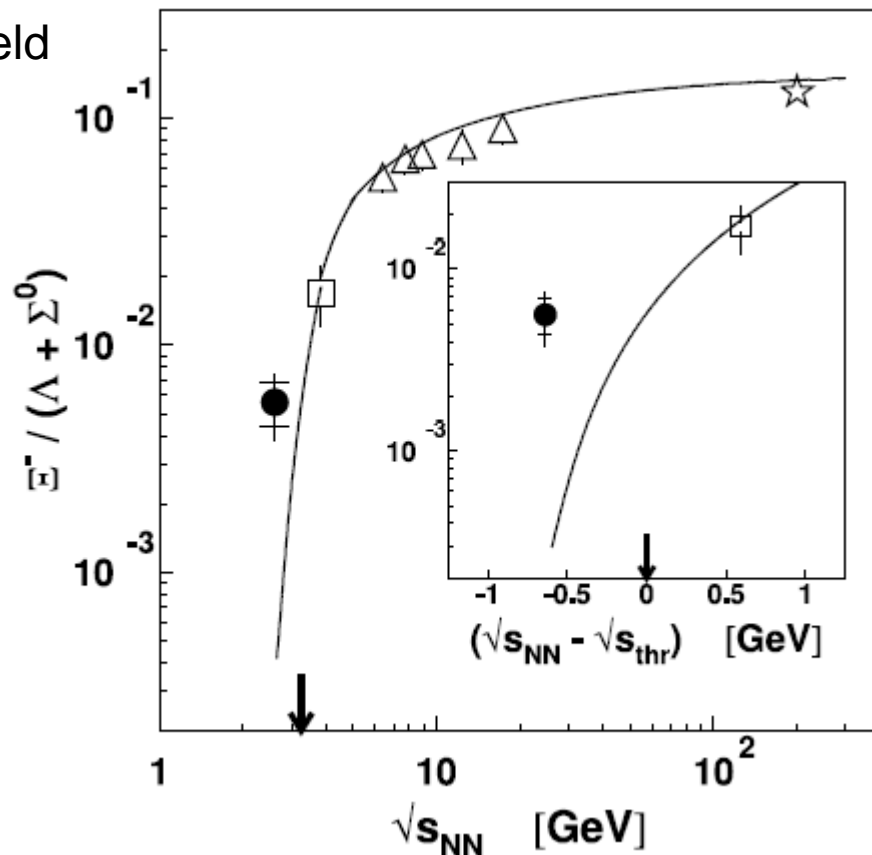
HADES: Sub-threshold Ξ^- production

Ar+KCl reactions at 1.76A GeV

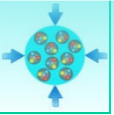
- Ξ^- yield by appr. factor 25 higher than thermal yield
- strangeness exchange reactions like



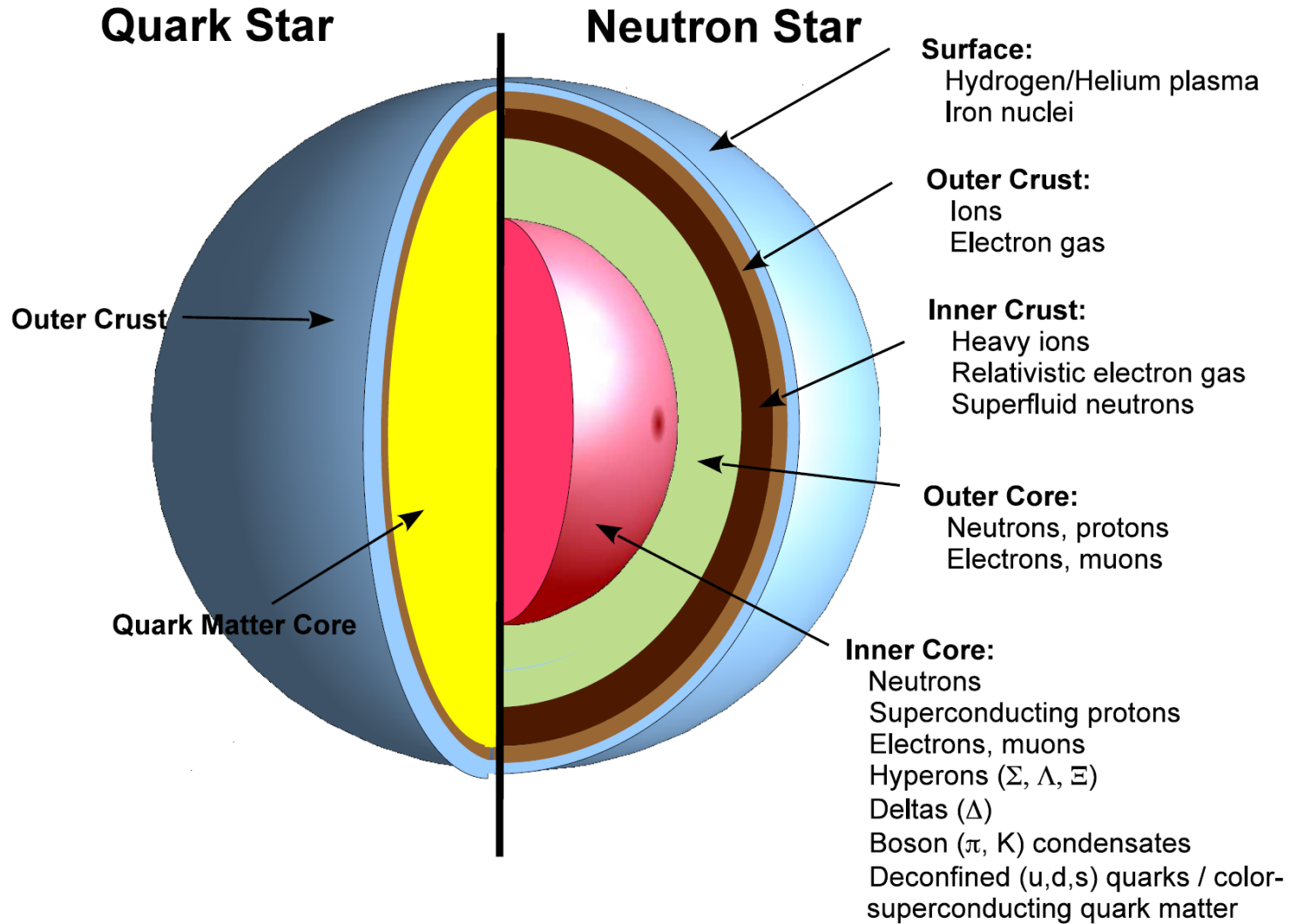
G. Agakishiev et al. (HADES), PRL103, 132301, (2009)



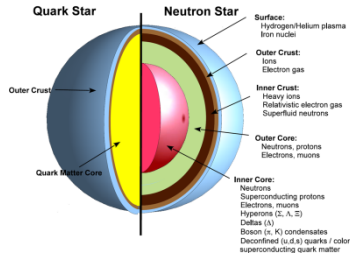
**trapping of
strange quarks
in bubbles ?**



The structure of neutron stars

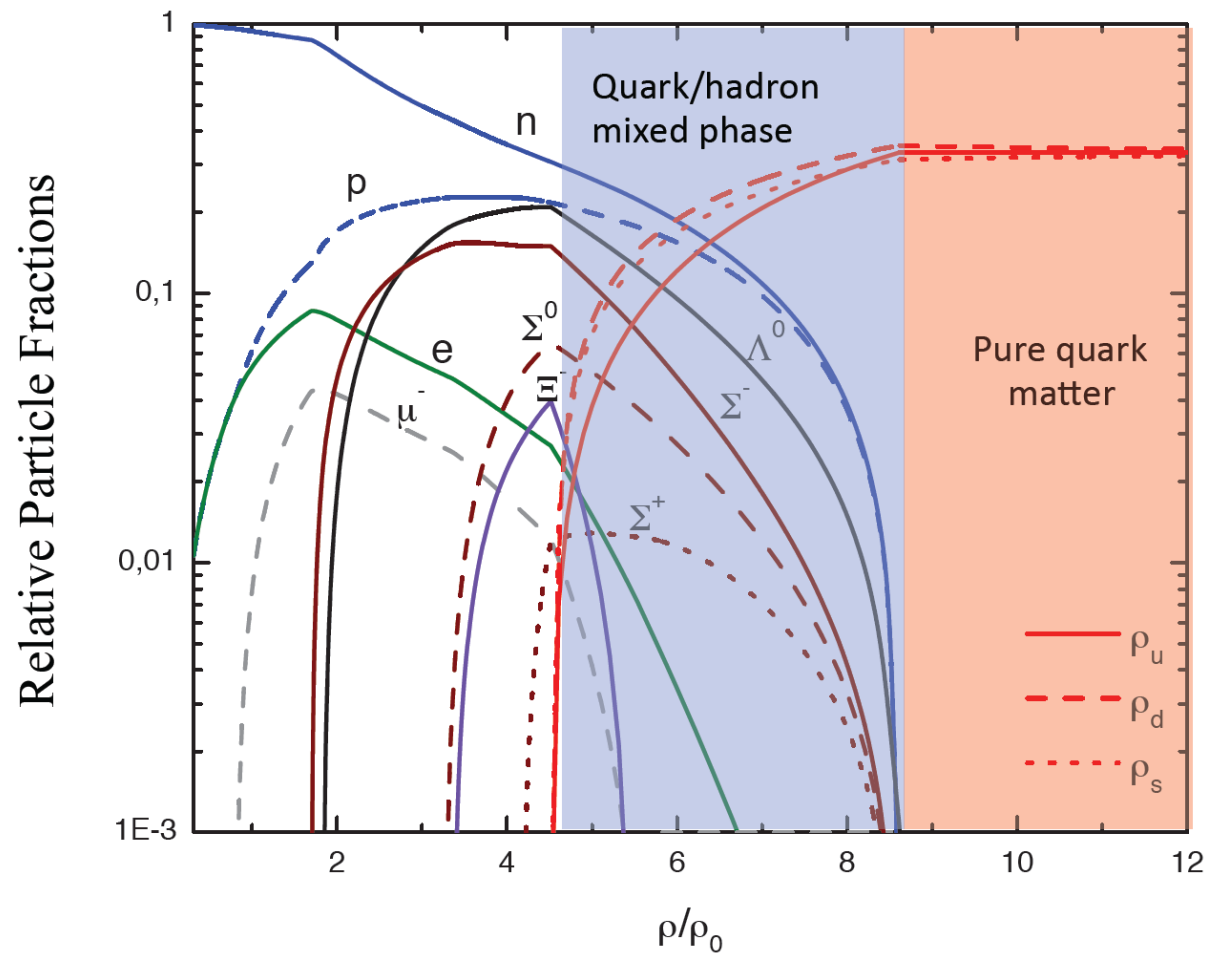
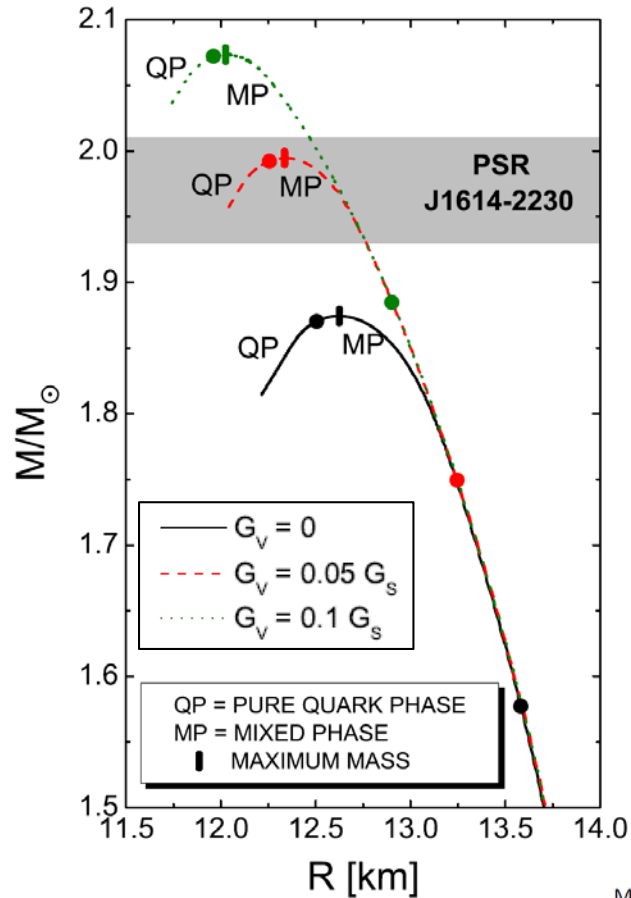


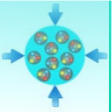
Equation – of – State of neutron stars



Equation-of-state: Non-local SU(3) NJL with vector coupling

M. Orsaria, H. Rodrigues, F. Weber, Phys.Rev. D87 (2013) 023001

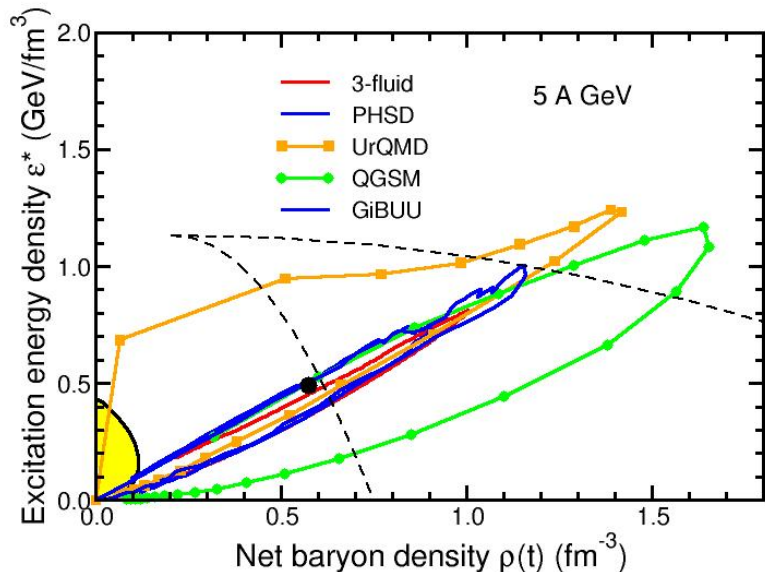




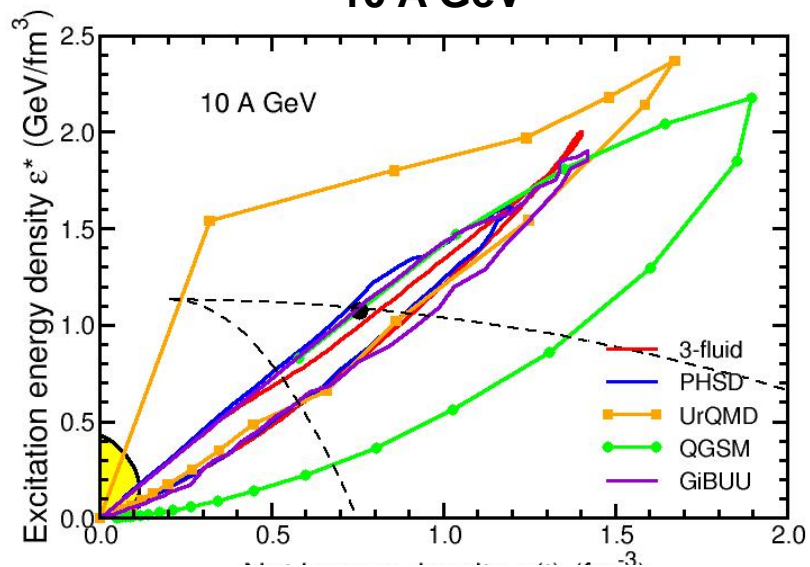
Baryon density in HI - collisions

I.C. Arsene et al., Phys. Rev. C 75, 24902 (2007)

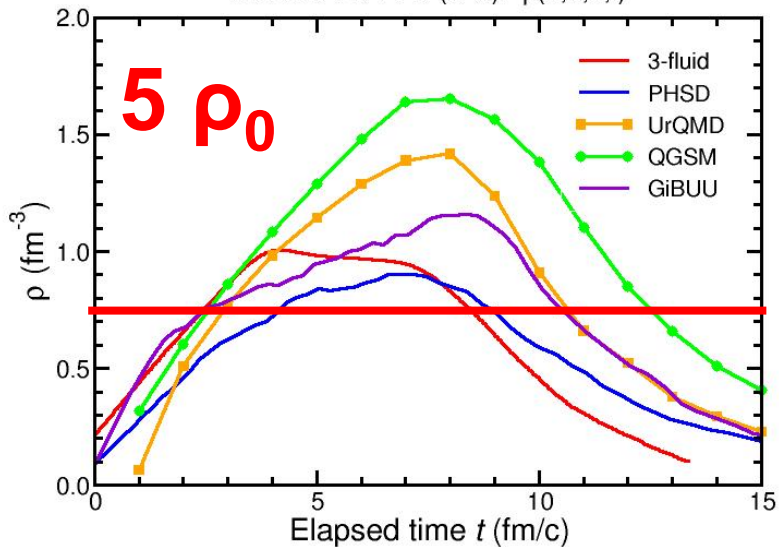
5 A GeV



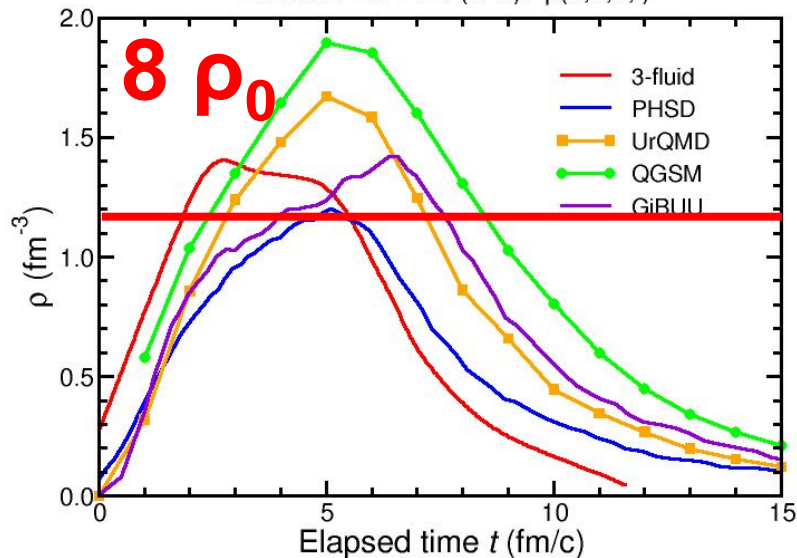
10 A GeV

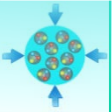


5 A GeV Au + Au (b=0): $\rho(0,0,0,t)$

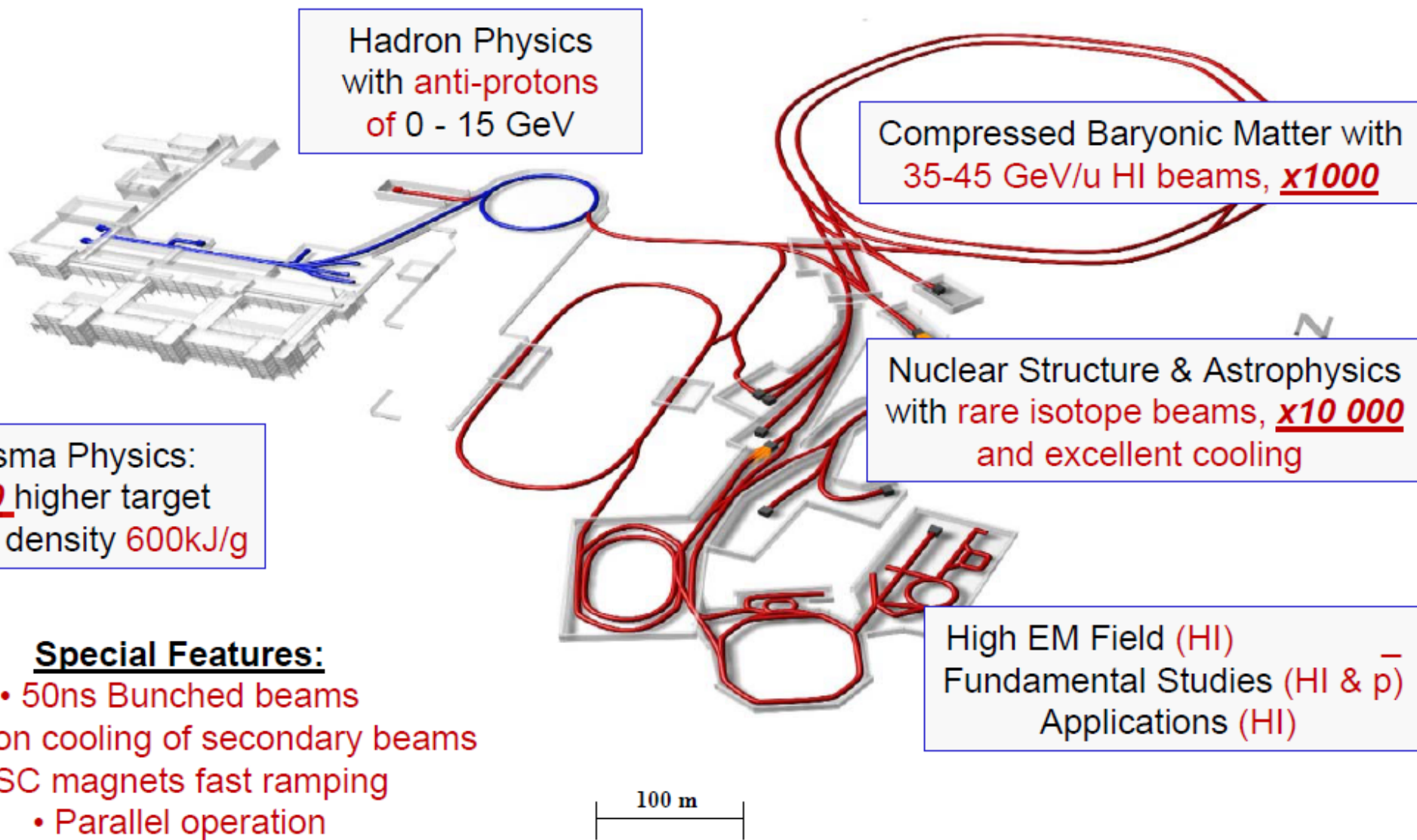


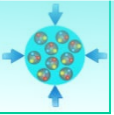
10 A GeV Au + Au (b=0): $\rho(0,0,0,t)$



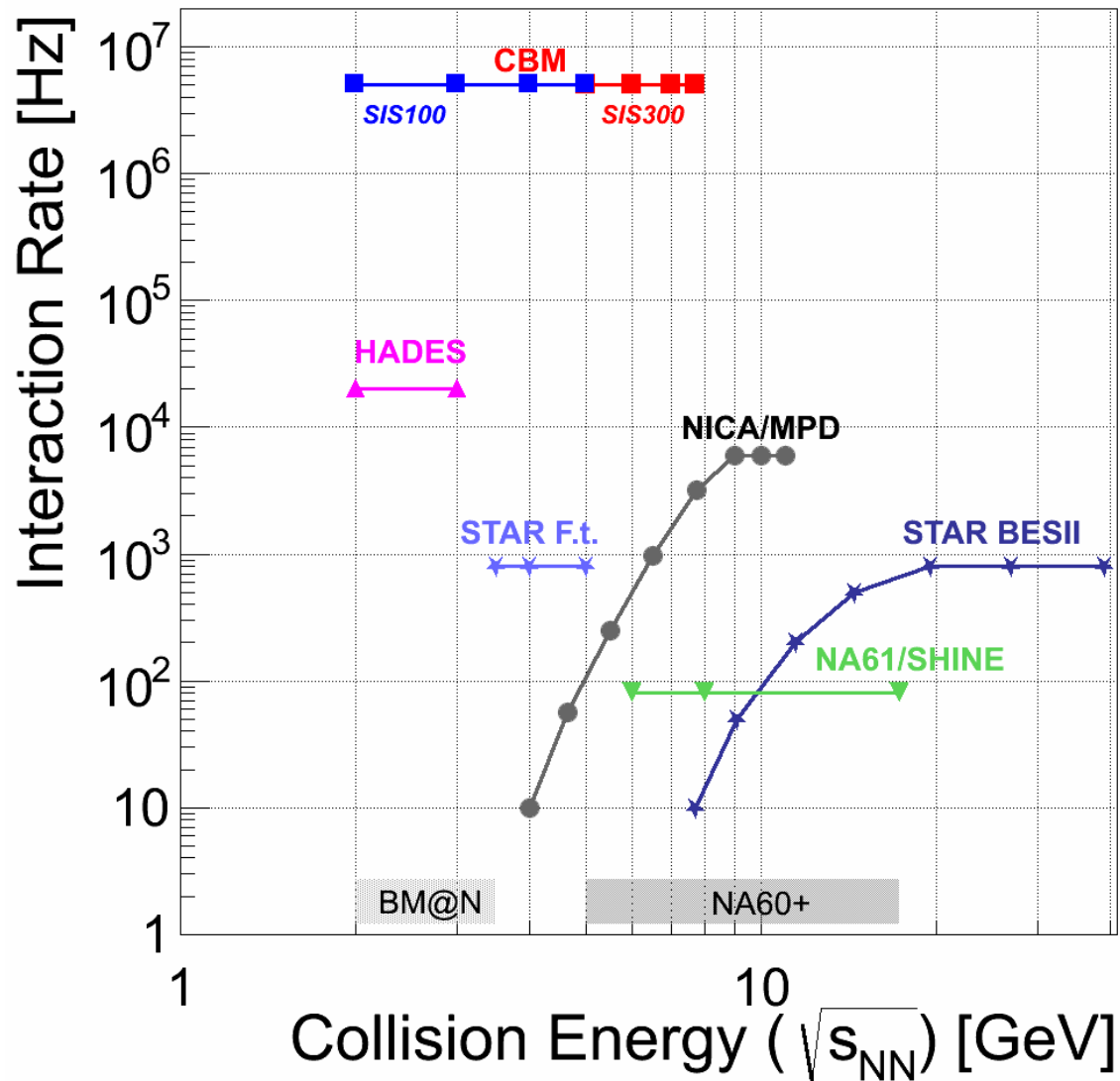


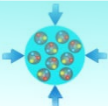
FAIR project (since 2001)





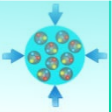
Experiments exploring dense QCD matter





CBM – Experimental Challenges

- $10^5 - 10^7$ Au+Au reactions/sec
- determination of (displaced) vertices ($\sigma \approx 50 \mu\text{m}$)
- identification of leptons and hadrons
- fast and radiation hard detectors
- free-streaming readout electronics
- high speed data acquisition and high performance computer farm for online event selection
- 4-D event reconstruction



CBM – Detector Concept

Different detector setups for muon & electron measurements:

0) Core elements

- dipole magnet
- STS – silicon tracking system
- PSD – projectile spectator detector
- TOF – MRPC time-of-flight detector
- DAQ – data acquisition
- FLES – first level event selection

1) Muon setup

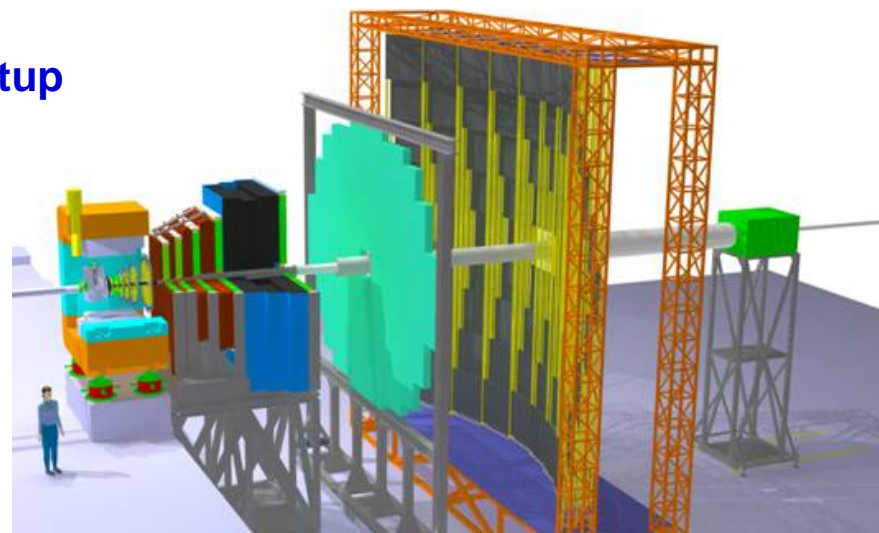
- MUCH – Muon detection system (active absorber)
- TRD – tracking station

2) Electron/Hadron setup

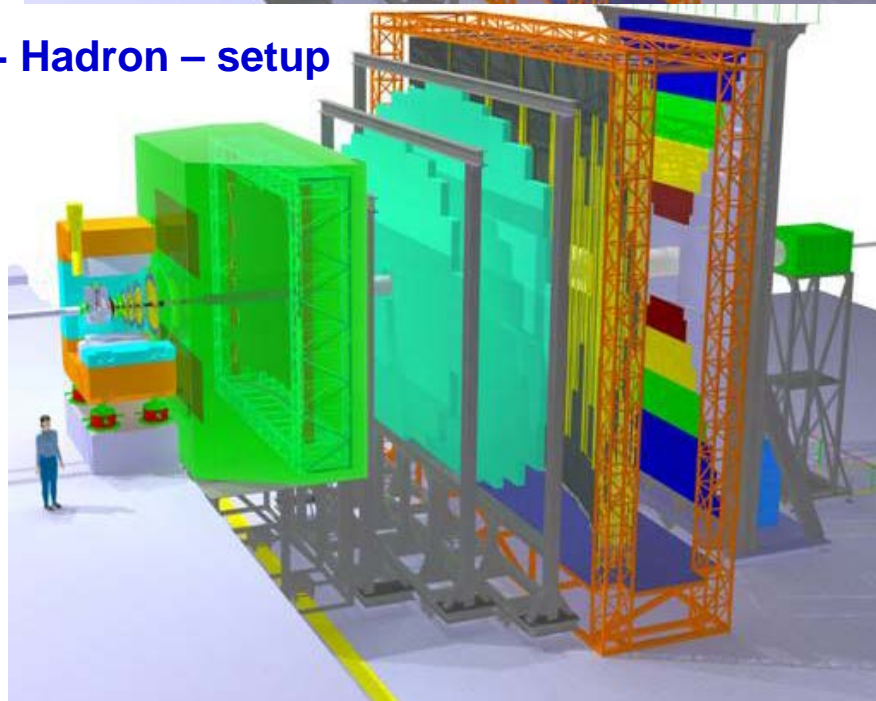
- MVD – Micro vertex detector
- TRD – Transition radiation detector
- ECAL – Electromagnetic calorimeter

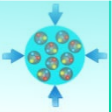
All core components designed with self triggered FEE and free running DAQ for 10 MHz interaction rate.

1) Muon – setup

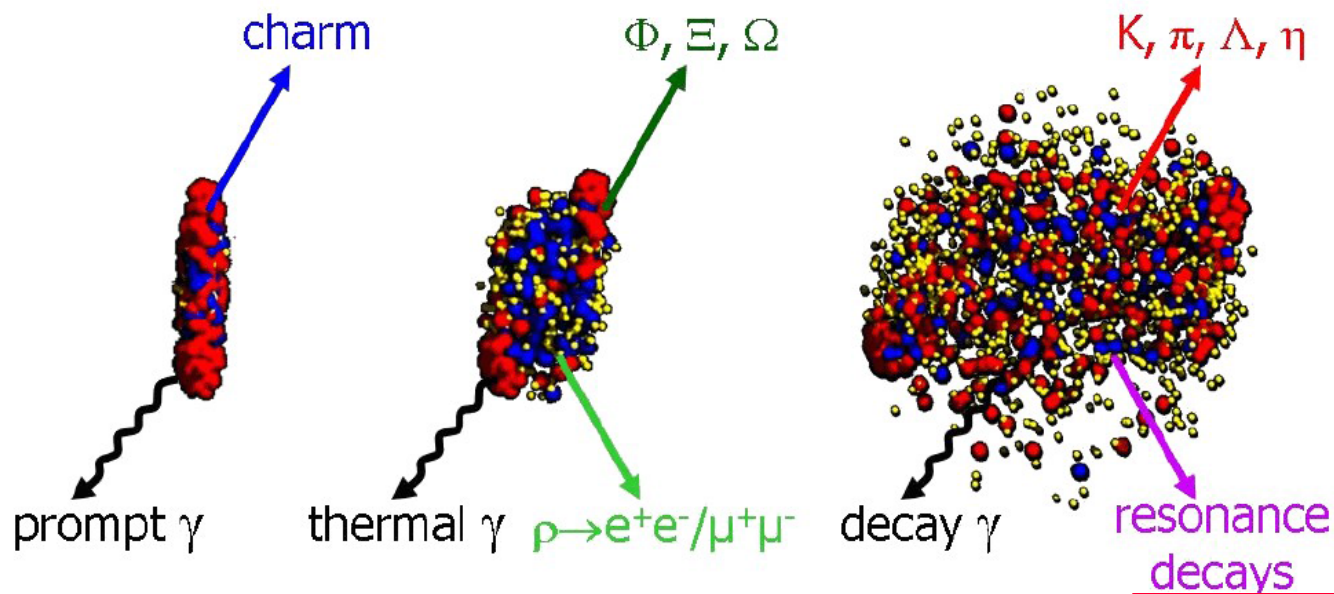


2) Electron + Hadron – setup





Observables in HI – collisions



**Hard probes
(initial state)**

**Penetrating probes
(integrate over collision history)**

**Relicts
(produced in dense phase,
sub – NN – threshold processes
are sensitive to medium properties)**

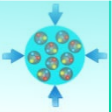
**Freeze-out
(final state particles)**

Thermalized (?) hadrons

Direct multi-strange hyperon production:

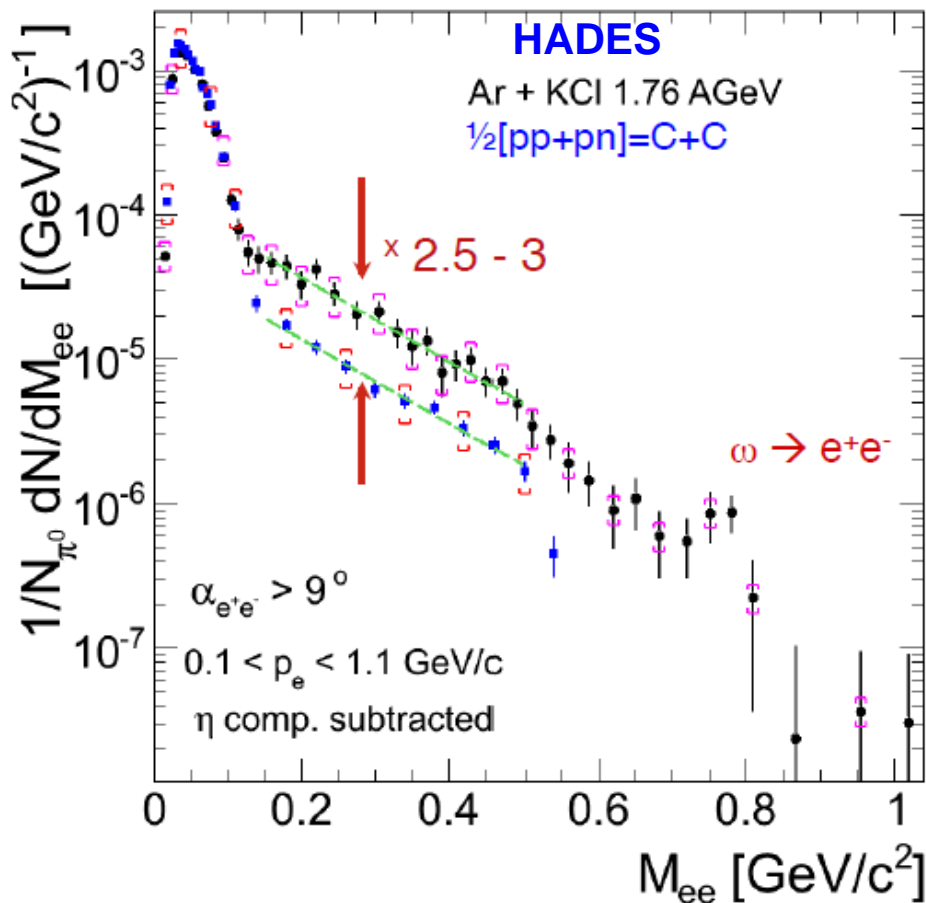
$$pp \rightarrow \Xi^- K^+ K^+ p \quad (E_{\text{thr}} = 3.7 \text{ GeV})$$

$$pp \rightarrow \Omega^- K^+ K^+ K^0 p \quad (E_{\text{thr}} = 7.0 \text{ GeV})$$

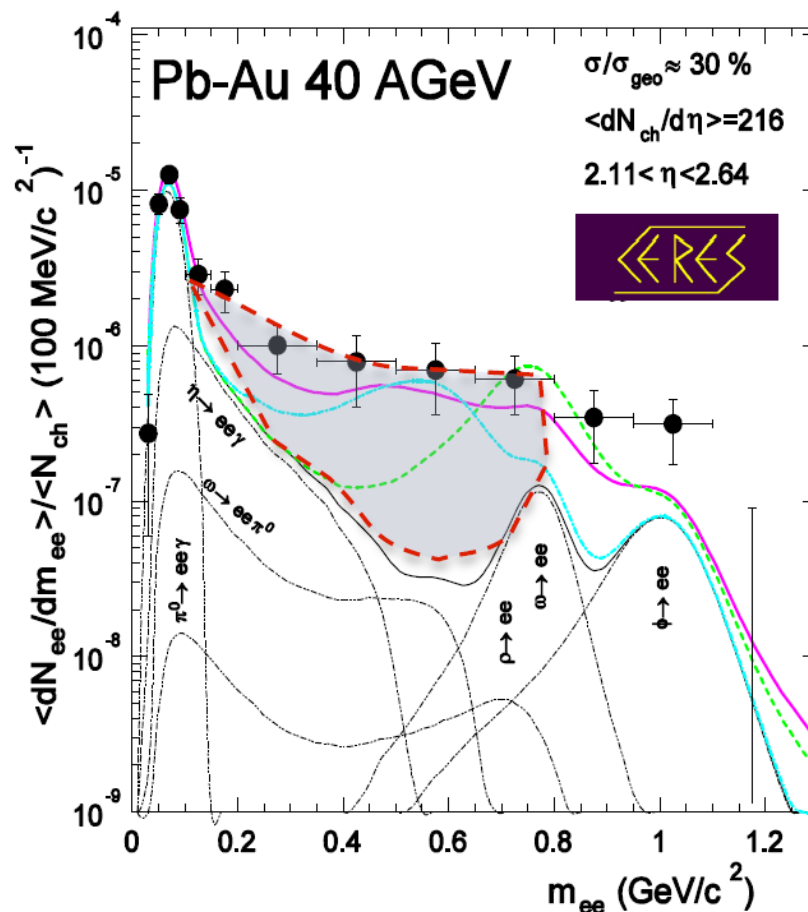


In – medium properties of light vector mesons

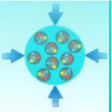
G. Agakishiev et al., Phys. Rev. C 84 (2011) 014902



D. Adamova et al., Phys. Rev. Lett. 91 (2003) 042301

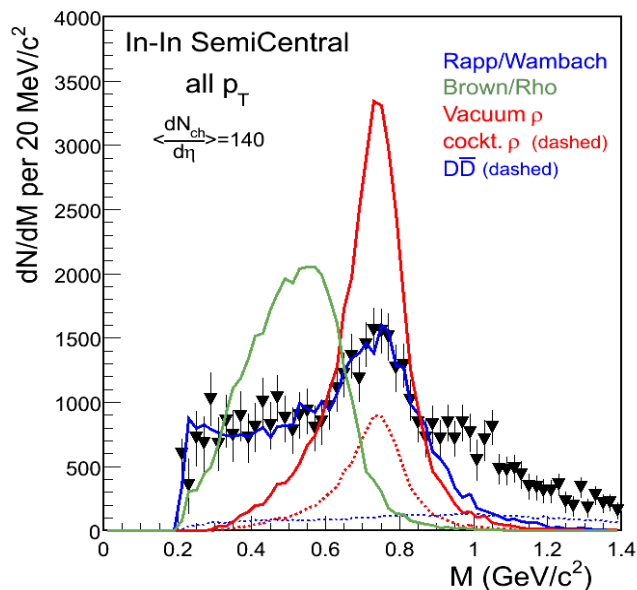


No data available in SIS100 / SIS300 energy range



Phase transition observables (?)

R. Arnaldi et al. (NA60), PRL 100 (2008) 022302

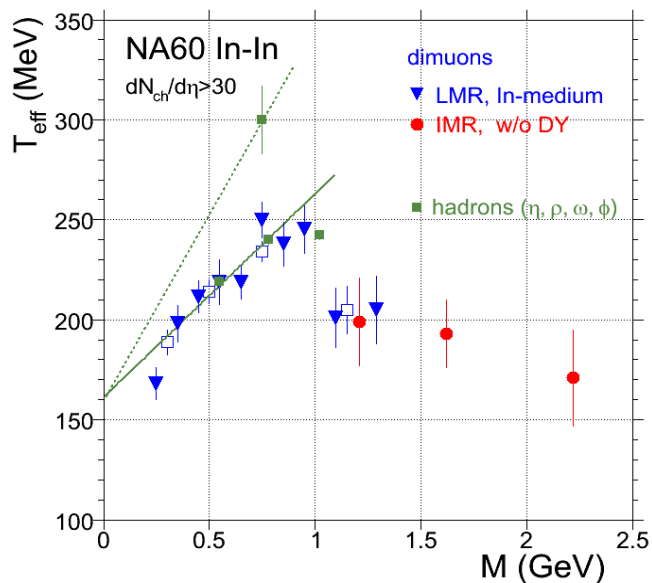


NA60

In + In collisions at 158 AGeV (SPS)

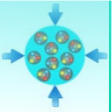


Clean measurement of ρ – meson spectral function.

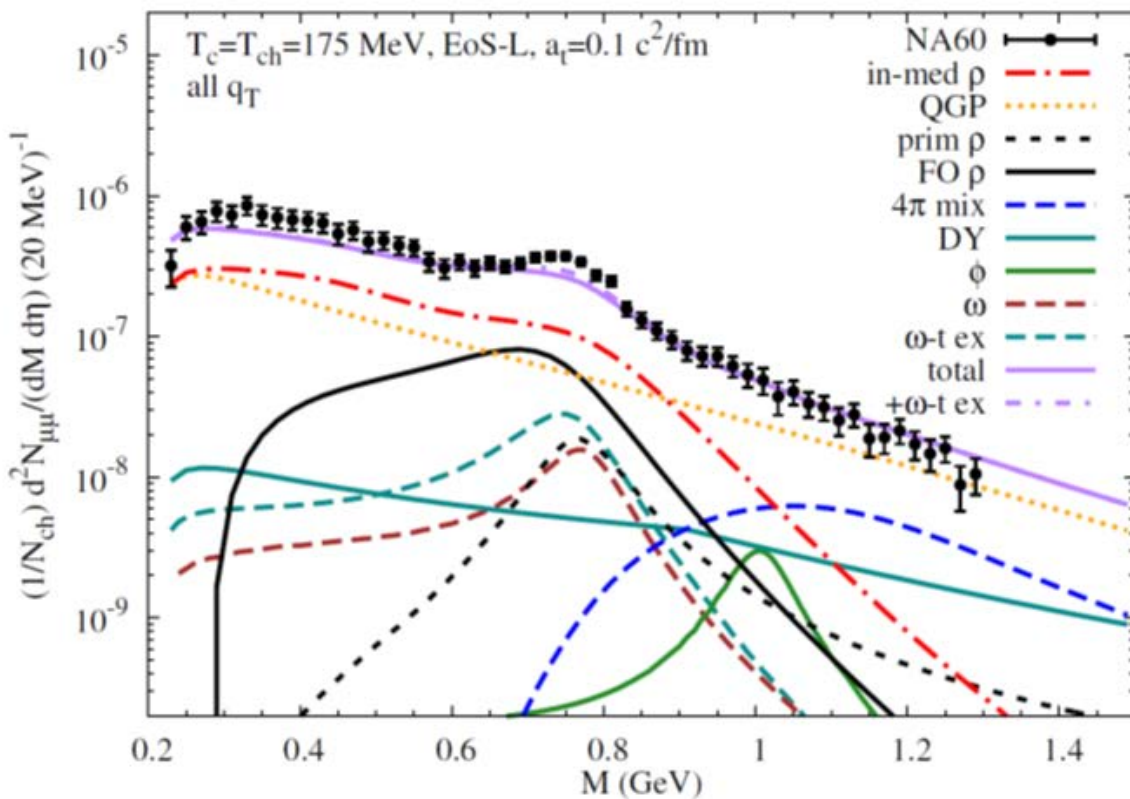


Slope parameter of transverse momentum spectra in agreement with hadrons up to $M \sim 1$ GeV

Spectra above 1 GeV are conjectured to originate from partonic source



Theoretical interpretation of Dilepton Spectrum



Experiment:

R. Arnaldi et al. [NA60 Coll.],
Phys. Rev. Lett. 96, (2006) 162302,

Theory:

R. Rapp, J. Wambach and H. van Hees, in
arXiv:0901.3289 hep-ph

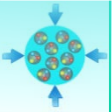
Signatures:

In – medium modification of hadrons

in 1 – 2 GeV range:

temperature of source

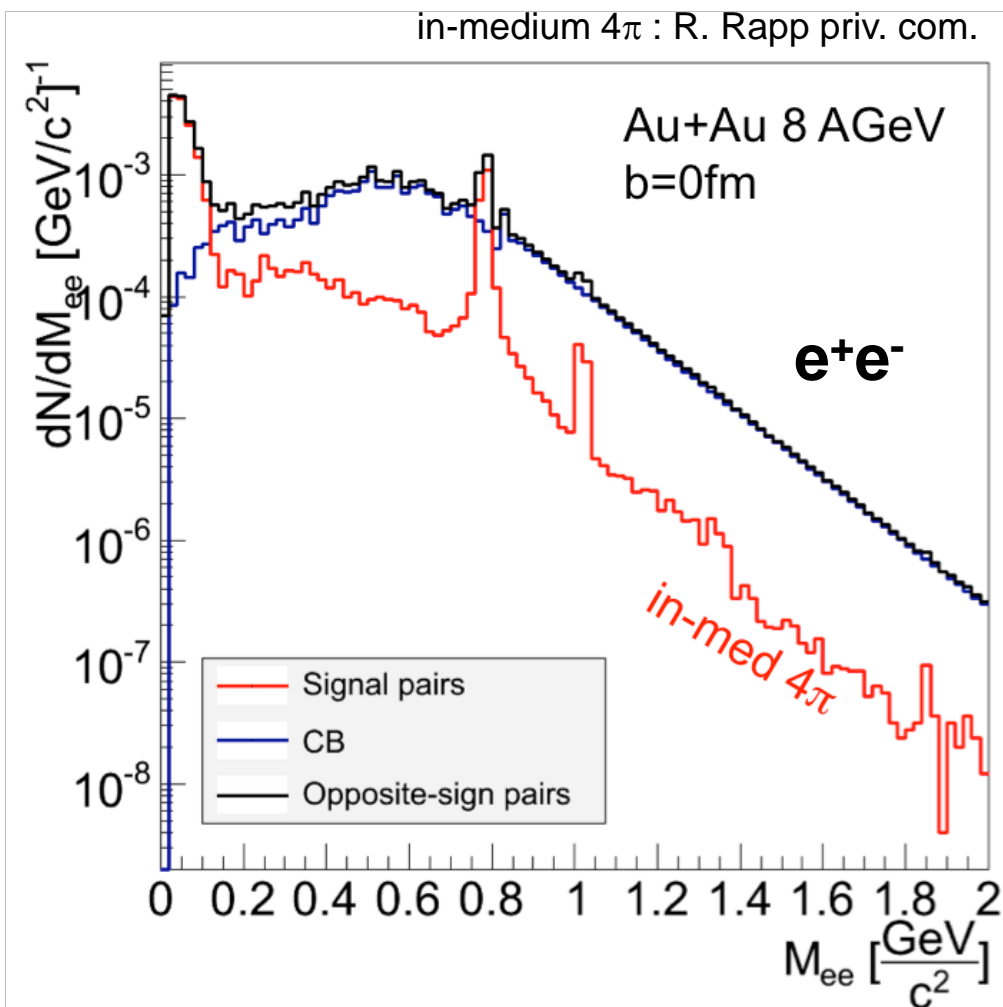
**$\rho - a_1$ mixing
(chiral symmetry restoration)**



Exploring restoration of chiral symmetry

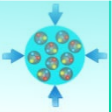
At SIS100 beam energies:

M_{inv} between 1 and 2 GeV/c^2 dominated by in-medium 4π
 $\rightarrow \rho$ - a_1 chiral mixing



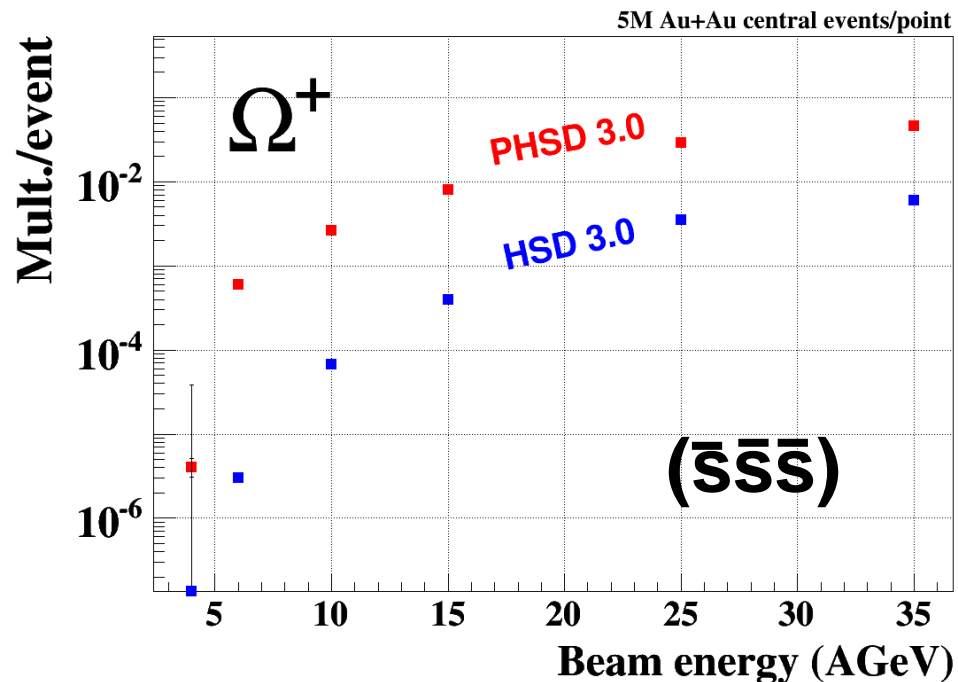
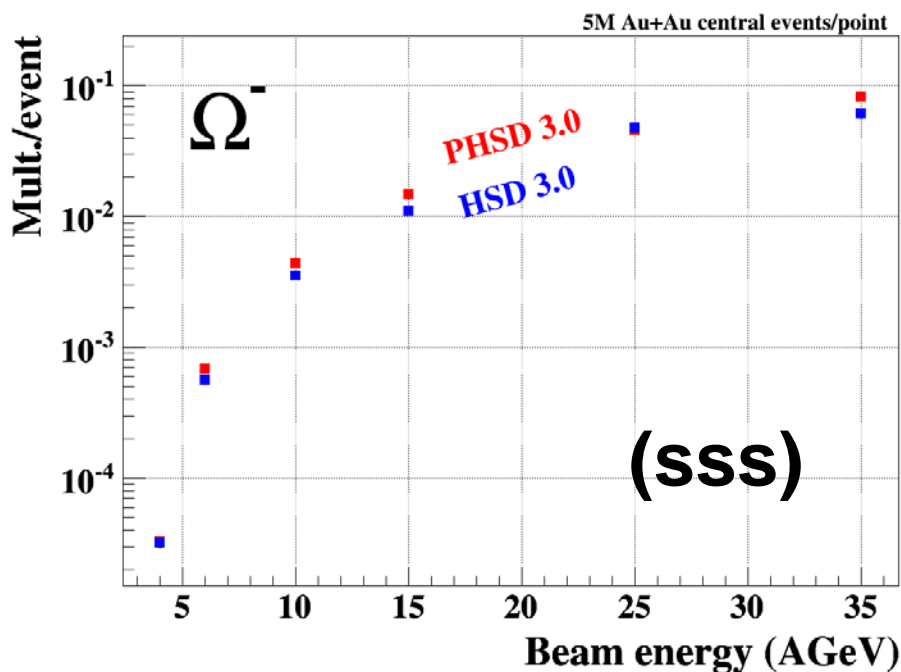
Correlated charm, Drell-Yan and QGP contributions decrease with decreasing beam energy

SIS100 energy range is well suited to search for signals for chiral symmetry restoration



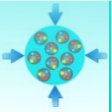
Strangeness

I. Vassiliev, E. Bratkovskaya (preliminary)



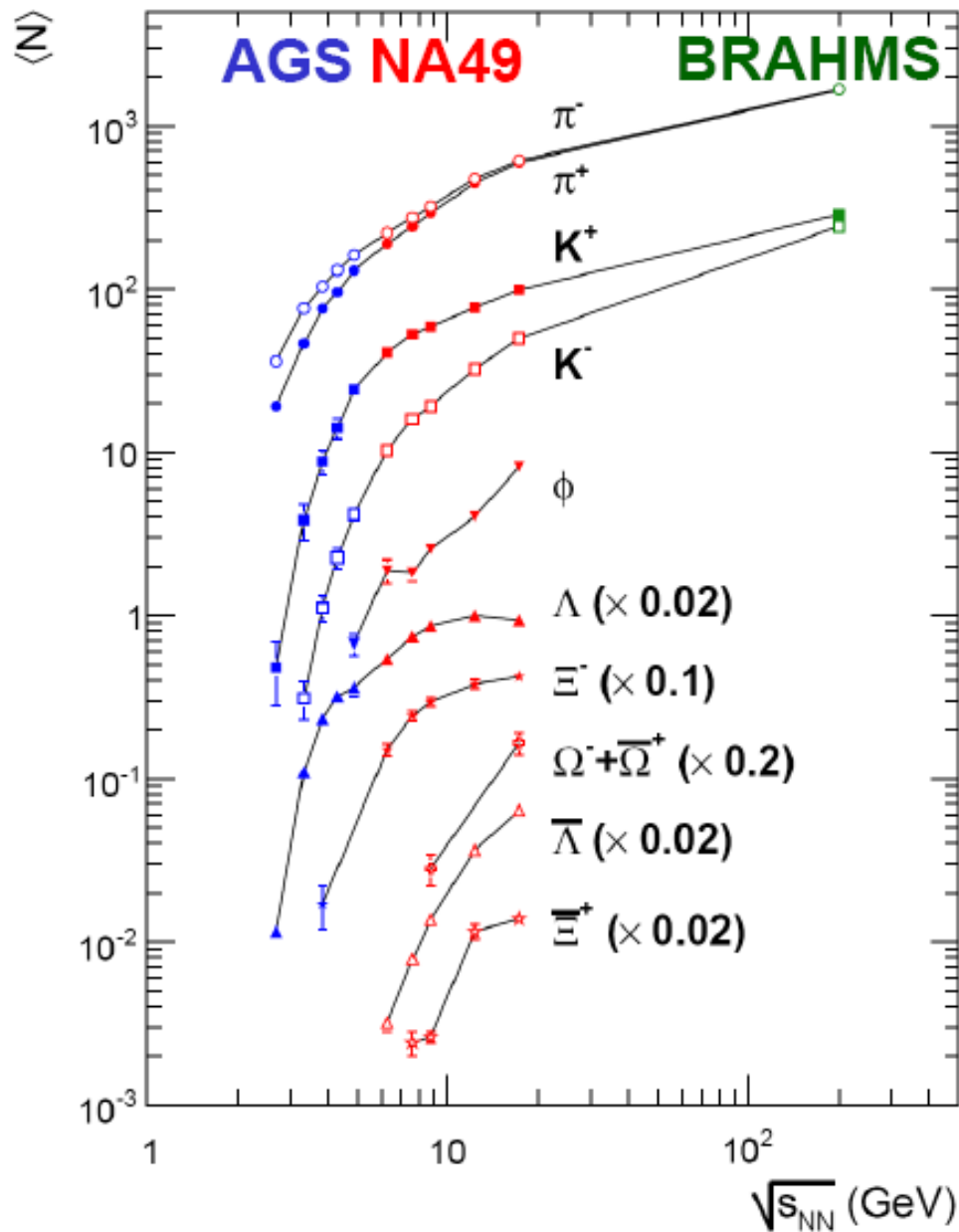
HSD: Hadronic transport code

PHSD: Hadronic transport code with partonic phase ($\epsilon > 1 \text{ GeV}/\text{fm}^3$)

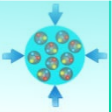


Excitation function of particle production

Central Au+Au collisions
(4π yields)

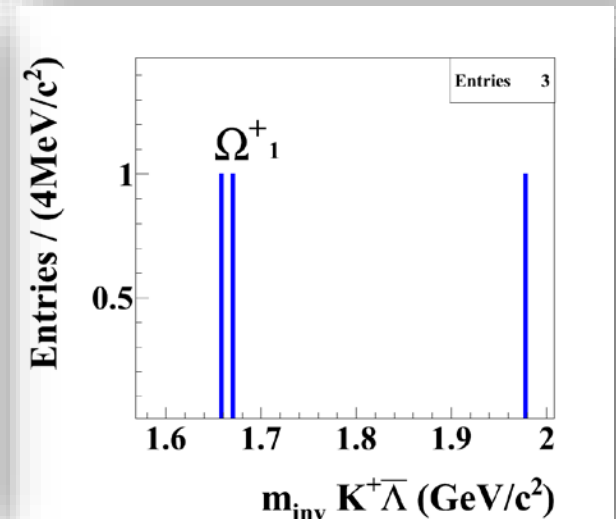
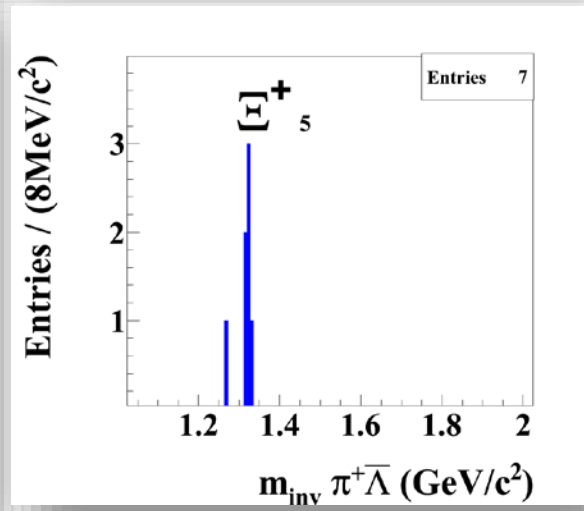
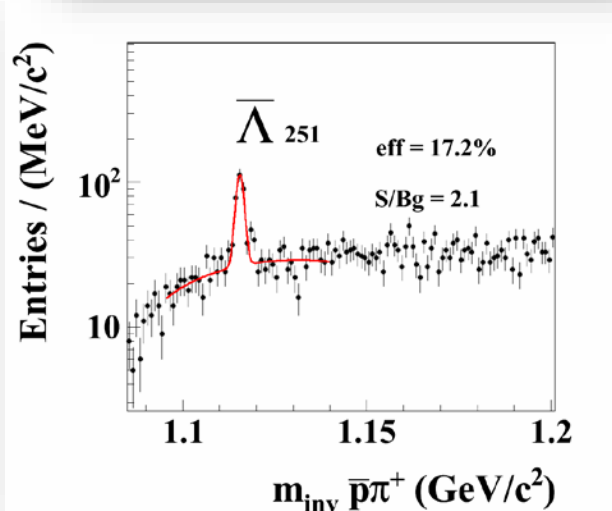
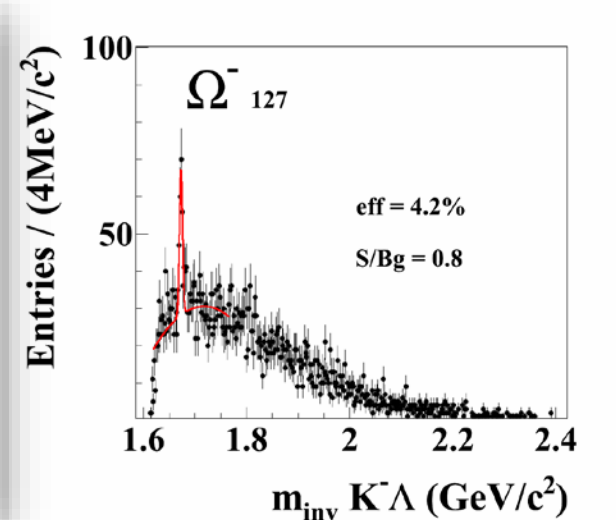
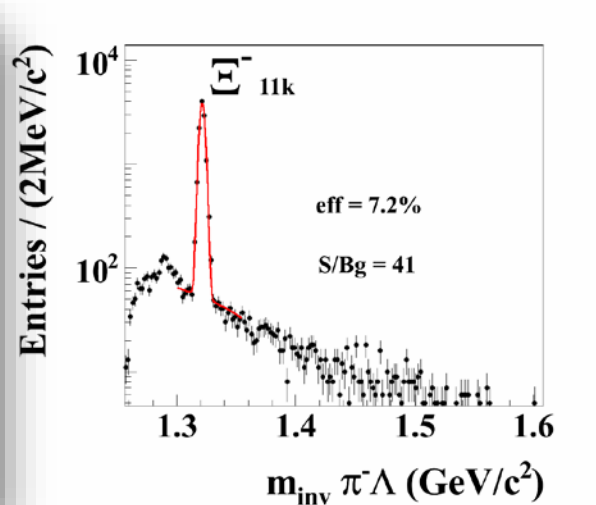
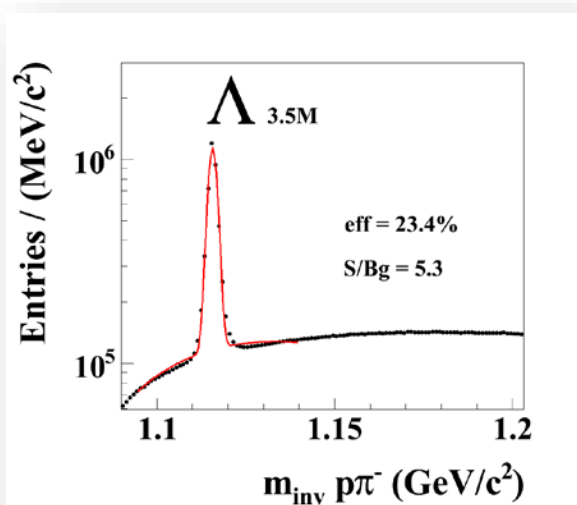


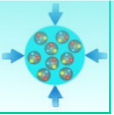
C. Blume, CBM symposium HZDR (2011)



Au + Au at 8 AGeV, 10^6 central events

Hyperon yields in CBM

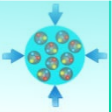




Hyperons rates in CBM

- Expected reconstructed yields for 4 weeks/energy min. bias Au+Au with 10^7 beam ions/s (100 kHz events/s):

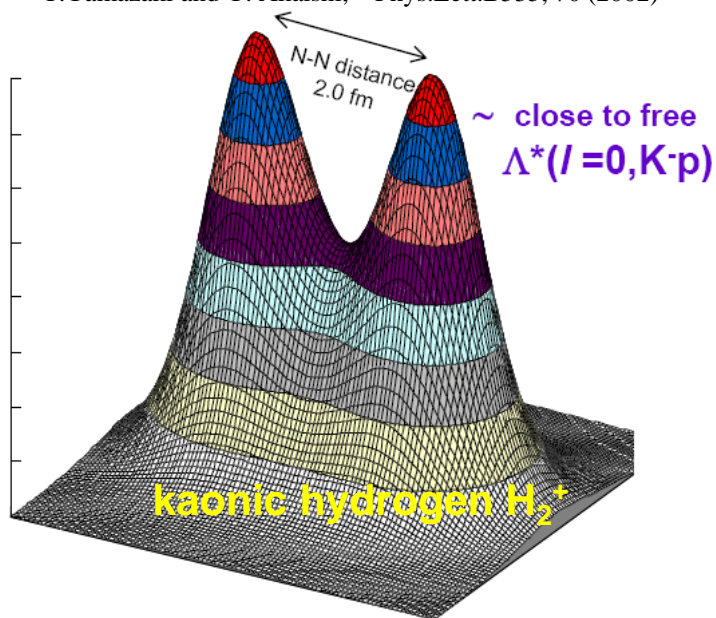
A GeV	Λ	$\bar{\Lambda}$	Ξ^-	Ξ^+	Ω^-	Ω^+
4	$8.1 \cdot 10^{10}$	$3.0 \cdot 10^5$	$6.6 \cdot 10^7$	$6.0 \cdot 10^4$	$3.6 \cdot 10^5$	$1.2 \cdot 10^3$
6	$1.6 \cdot 10^{11}$	$5.0 \cdot 10^6$	$3.4 \cdot 10^8$	$1.8 \cdot 10^5$	$2.4 \cdot 10^6$	$1.2 \cdot 10^4$
8	$2.1 \cdot 10^{11}$	$1.5 \cdot 10^7$	$6.6 \cdot 10^8$	$3.0 \cdot 10^5$	$7.6 \cdot 10^6$	$6.0 \cdot 10^4$
10	$2.4 \cdot 10^{11}$	$3.8 \cdot 10^7$	$9.6 \cdot 10^8$	$2.0 \cdot 10^6$	$1.3 \cdot 10^7$	$1.5 \cdot 10^5$



Strange baryon bound states

Kaonic molecules

T.Yamazaki and Y. Akaishi, Phys. Rev. C76 (2007) 045201
 Y. Akaishi, T.Yamazaki, Phys.Rev.C65, 044005 (2002)
 T.Yamazaki and Y. Akaishi, Phys.Lett.B535, 70 (2002)



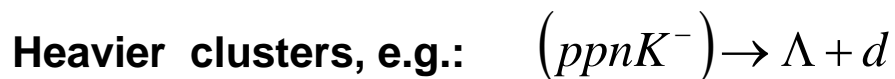
$$\Psi = \phi_a + \phi_b$$

Decay by strong interaction



FINUDA M=2255±9 MeV, Γ=64±14 MeV

DISTO M=2265±2 MeV, Γ=118±8 MeV



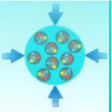
Hypernuclei



Decay by weak interaction

Production in HI – collisions?
 Recently: STAR, ALICE

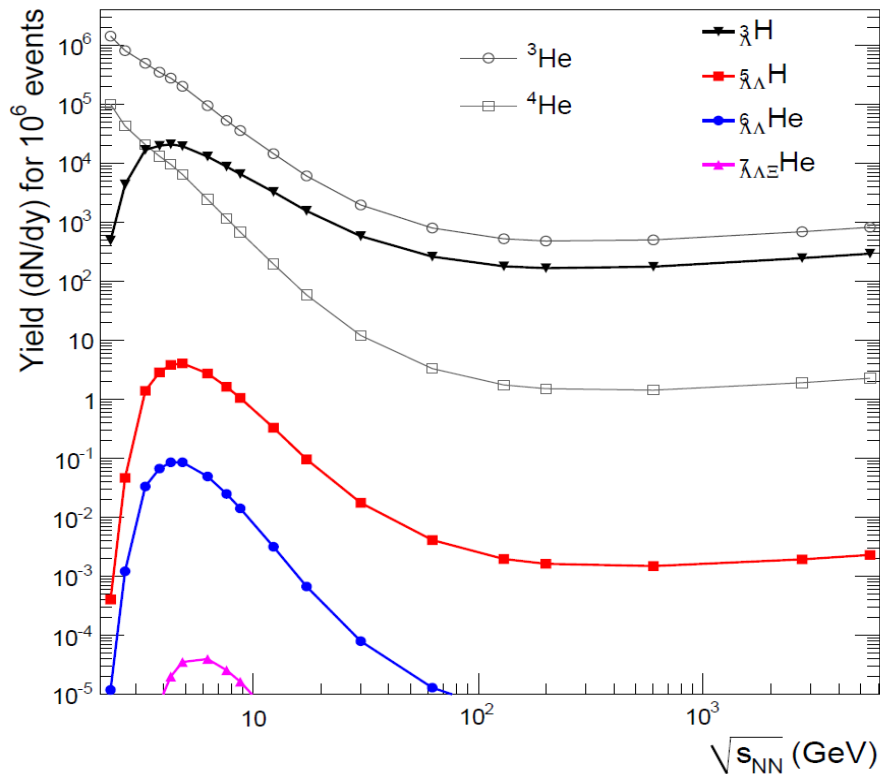
Double strange hypernuclei?



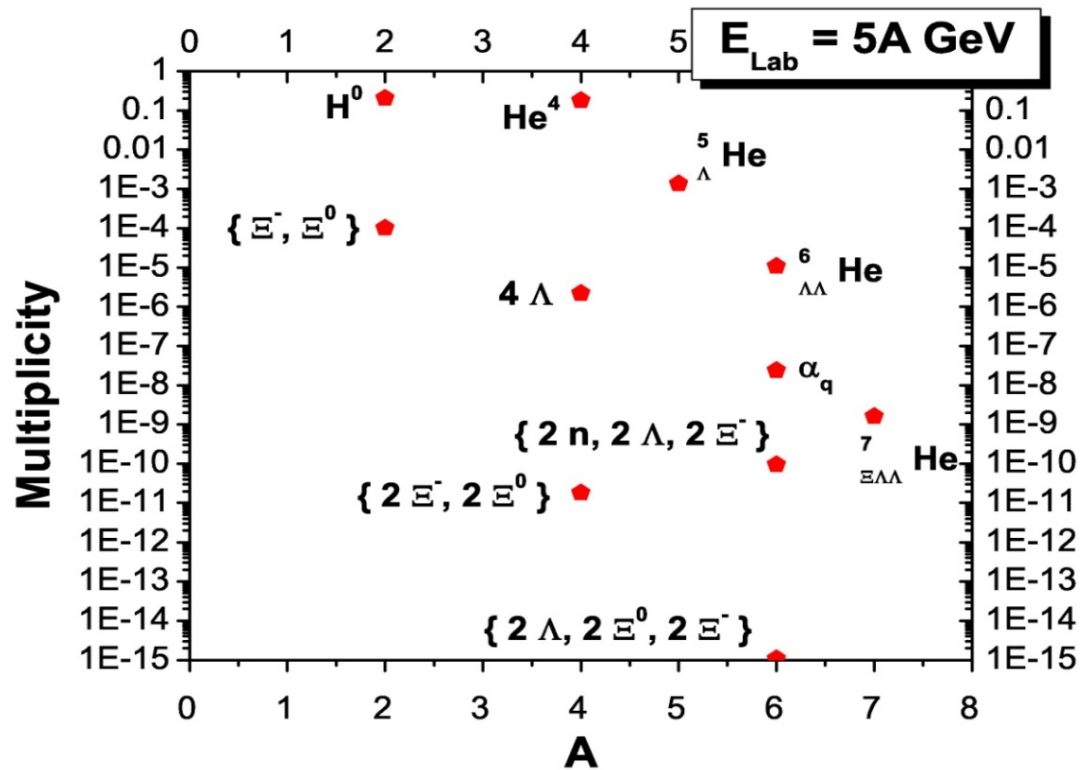
Strange baryonic bound states

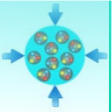
- Single and double strange hypernuclei in heavy ion collisions
- Search for strange matter in the form of strange dibaryons and heavy multi-strange short-lived objects.

A. Andronic, P. Braun-Munzinger, J. Stachel, H. Stöcker, Phys. Lett. B697 (2011) 203



H. Stöcker et al., Nucl. Phys. A 827 (2009) 624c





Conclusion

Future: exploring the QCD phase structure with rare probes

