

Measuring the CKM angle γ

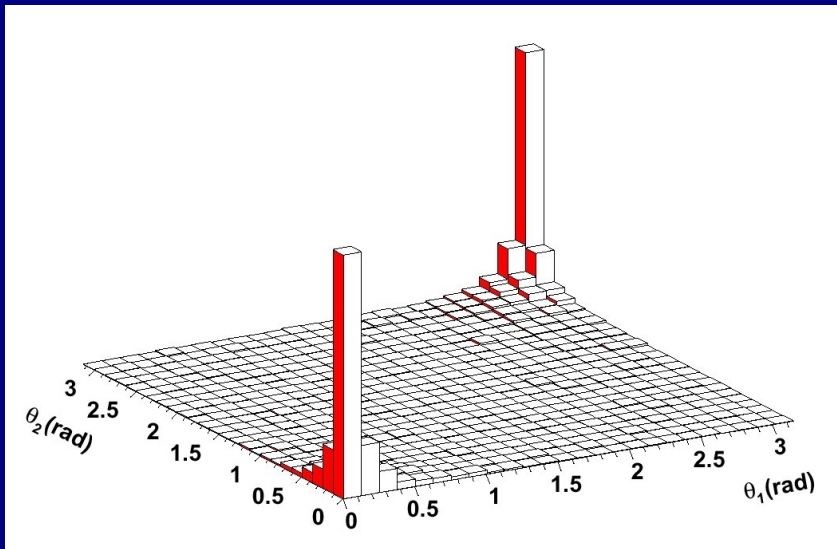
J. Blouw

Physikalisches Institut, Universitaet Heidelberg

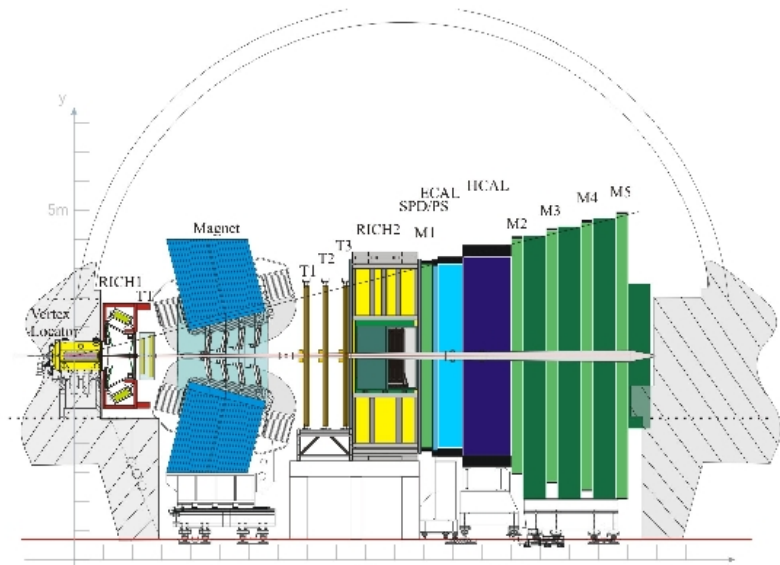
Tagungsstaette, Neckarzimmern, March 28-30, 2007



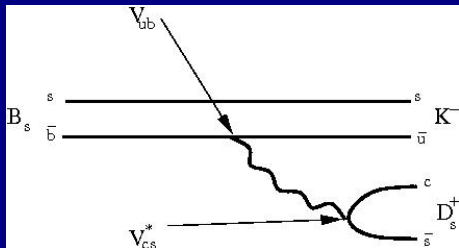
The LHCb Spectrometer



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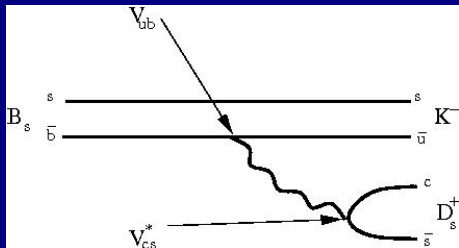
Feynmann diagram for $B_s \rightarrow D_s^+ K^-$



- 1 Only tree diagrams
- 2 But: problem of discrete ambiguities
- 3 Solve by using equivalent decay with B_d :
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- 5 Circumvent problems using assumption of U-spin symmetry ($s \longleftrightarrow d$)
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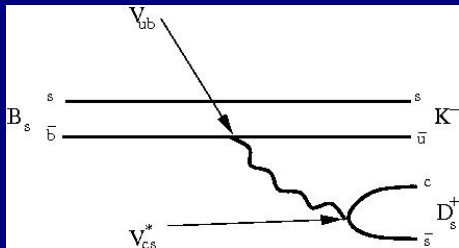
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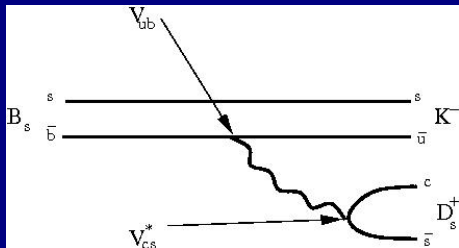
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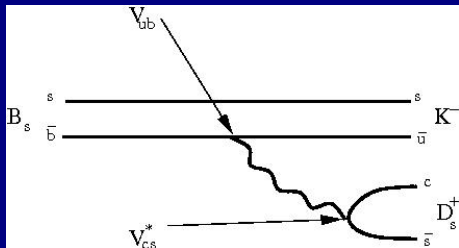
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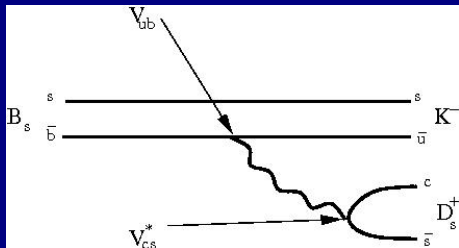
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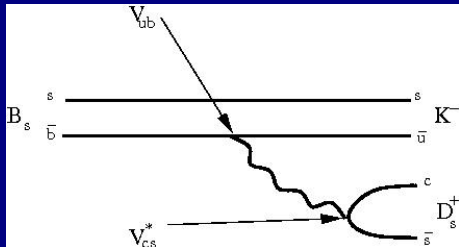
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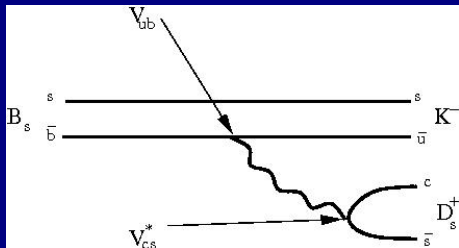
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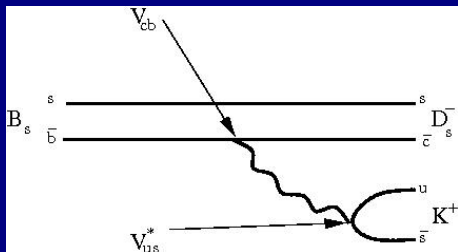
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- matrix element $V_{ub} V_{cs}^*$
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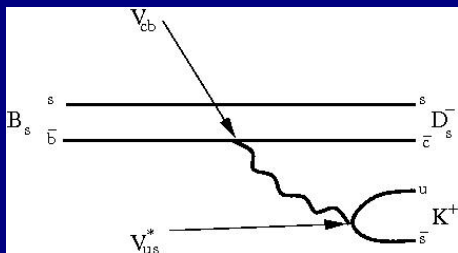
Diagram for $B_s \rightarrow D_s^- K^+$



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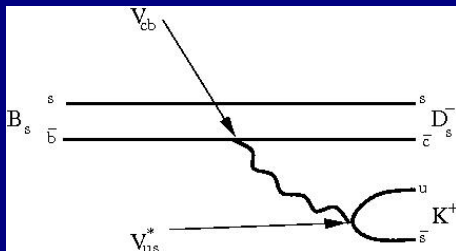
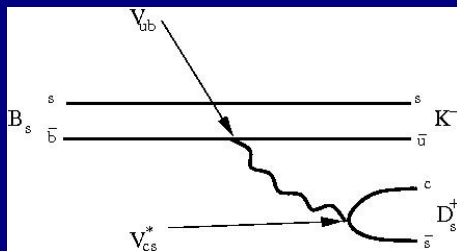
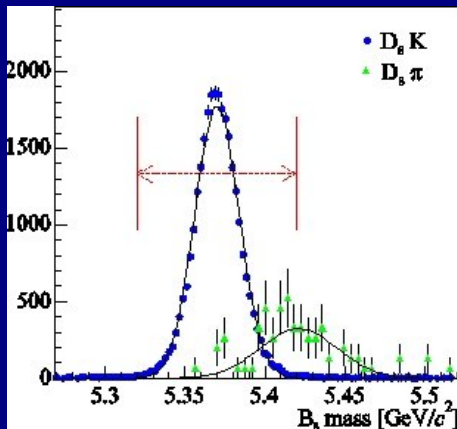


Diagram for $B_s \rightarrow D_s^+ K^-$



A Combined $B_s \rightarrow D_s^\pm K^\mp$ and $B_d \rightarrow D^\pm \pi^\mp$ Analysis



- Interference through mixing
- CP asymmetries measure $\gamma + \phi_s$
- Tree diagrams only: NO sensitivity to New Physics
- 5400 $B_s \rightarrow D_s K$ events/year at LHCb
- 82000 $B_s \rightarrow D_s \pi$ events/year



Time-dependent Asymmetries

$$\mathcal{A}_{\text{CP}}(\text{D}_s^+ \text{K}^-) = \frac{\text{B}_s \rightarrow \text{D}_s \text{K}^-(t) - \bar{\text{B}}_s \rightarrow \text{D}_s \text{K}^-(t)}{\text{B}_s \rightarrow \text{D}_s \text{K}^-(t) + \bar{\text{B}}_s \rightarrow \text{D}_s \text{K}^-(t)}$$

dependence:

$$\mathcal{A}_{\text{CP}}(\text{D}_s^+ \text{K}^-) = \frac{C_s \cos \Delta m_s t + S_s \sin \Delta m_s t}{\cosh(\Delta \Gamma_s t/2) - A_{\Delta \Gamma_s} \sinh(\Delta \Gamma_s t/2)}$$

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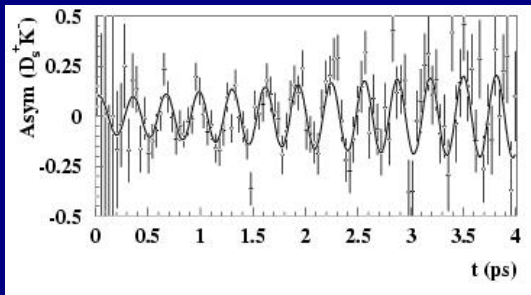
$$S_s(\bar{S}_s) \sim \sin(\phi_s + \gamma \pm \delta_s)$$

$$A_{\Delta \Gamma_s} \sim -\cos(\phi_s + \gamma \pm \delta_s)$$



LHCb Simulated Results

From ~ 5 years of LHCb data:

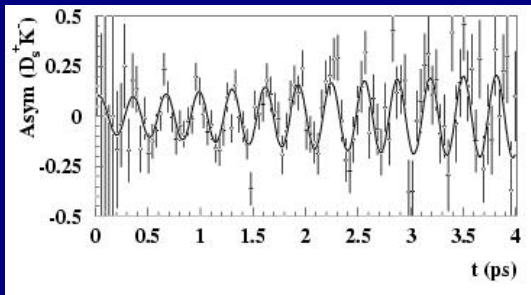


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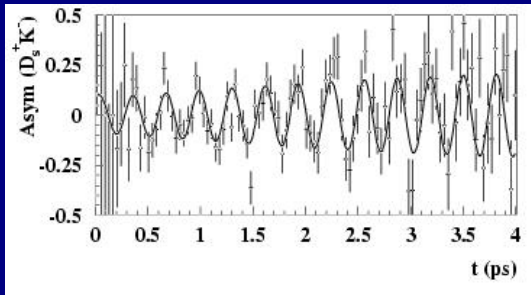


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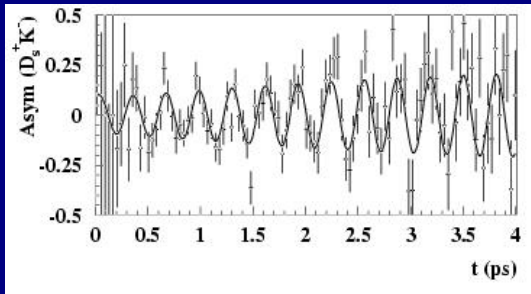


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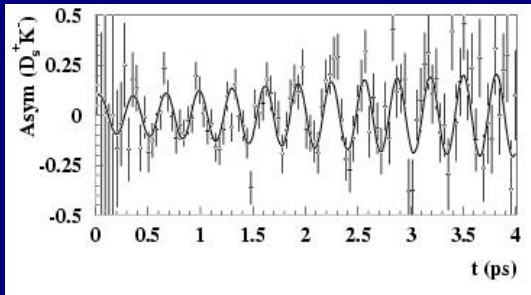


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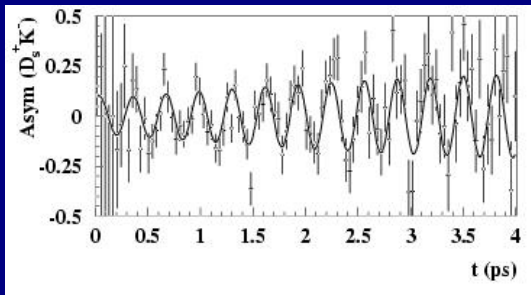


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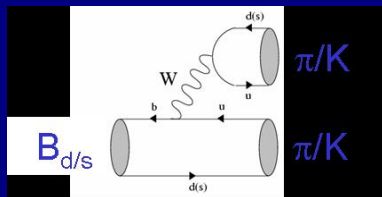
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γ from $B \rightarrow h^+ h^-$

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- 4 $A_{\text{dir}}, A_{\text{mix}}$ depend on ϕ_s, ϕ_d & γ
- 5 and on ratio of penguin to tree amplitudes: $d e^{i\theta}$
- 6 with U-spin symmetry: $d_{\pi\pi} = d_{KK}, \theta_{\pi\pi} = \theta_{KK}$
- 7 ϕ_s from $B_s \rightarrow J/\psi\phi$ and ϕ_d from $B_d \rightarrow J/\psi K_s$
- 8 4 measurements, 3 unknowns \implies extract $\gamma, \sigma_\gamma = 5^\circ$

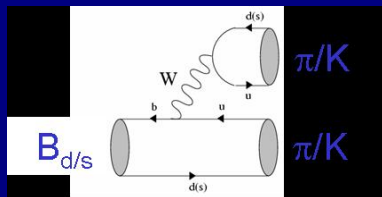
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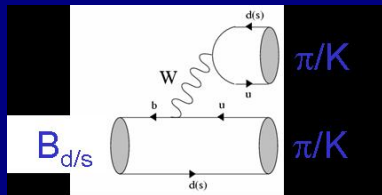
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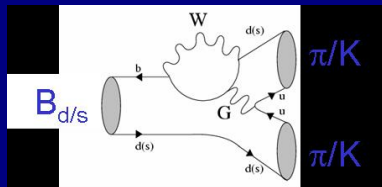
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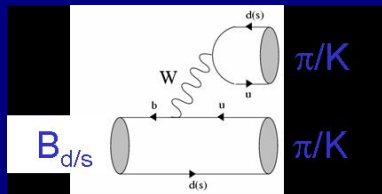
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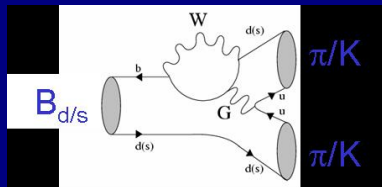
$$A_{CP}(t) = A_{\text{dir}} \cos(\Delta m t) + A_{\text{mix}} \sin(\Delta m t)$$

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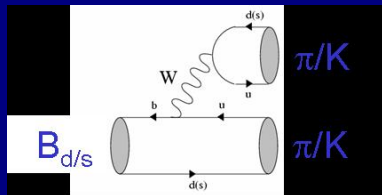
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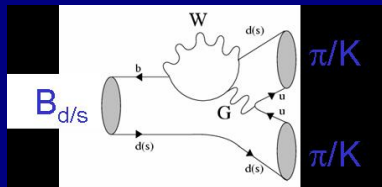
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- 4 $A_{\text{dir}}, A_{\text{mix}}$ depend on ϕ_s, ϕ_d & γ
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Penguin diagram:



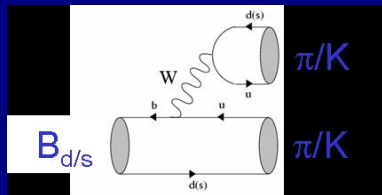
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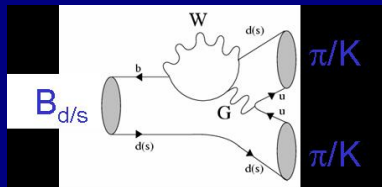
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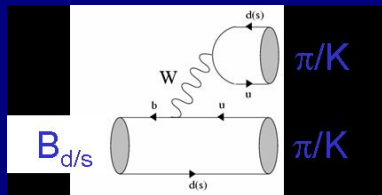
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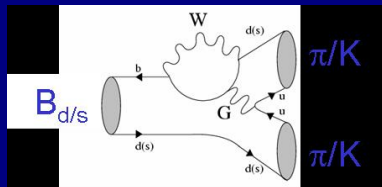
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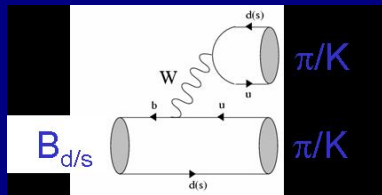
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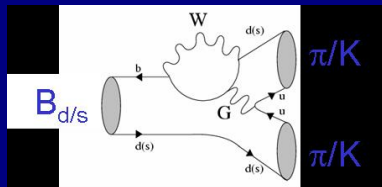
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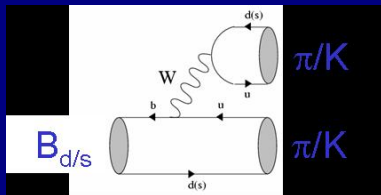
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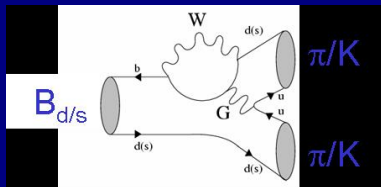
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