



Analysing $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ at LHCB

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INTRODUCTION

- This is mostly a walk-through of the $B^0 \to K^{*0} \mu^+ \mu^-$ analysis like it was performed in 2012 & 2013 in LHCb.
- It should show how an angular analysis with $\mathcal{O}(1000)$ events might look like and where the problems are.



VINTAGE PHYSICS (I)

- The electroweak bosons W and Z^0 were proposed in the 60ies.
- They are quite heavy with 80 ${\rm GeV}/c^2$ and 91 ${\rm GeV}/c^2$ and were first seen directly at UA1.
- However, in principle, the Z^0 should also contribute to the process $e^+~e^ \rightarrow \mu^+~\mu^-$, even at lower energies than $\sqrt{s}\sim$ 91 GeV
- Look at \sqrt{s} = 34 GeV. Simple calculation yields: Only very small effect of Z^0 in total cross-section.



VINTAGE PHYSICS (II)



Fig. 13.7 (a) The $\cos \theta$ distribution for the process $e^-e^+ \rightarrow \mu^- \mu^+$ does not follow the $1 + \cos^2 \theta$ QED prediction. (b) The discrepancy is explained by the interference of the virtual Z and γ contributions. (Compilation by R. Marshall.)

- However, if you look at the differential cross-section, you clearly see the influence of the Z^0 due to interference terms.
- You have discovered a new particle/effect/... indirectly at a centre-of-mass energy lower than the mass of the particle.
- Even if your total cross-section is according to your prediction of the (standard) model, one might seen new effects when studying angular distributions.

Essentials of the $B^0 \! \to K^{*0} \mu^+ \mu^-$ analysis aka: The "Sendung-mit-der-Maus" version



Essentials of the $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ analysis



- A particle decays into two particles, with angle α .
- Suppose we can formulate the angular distribution as:

$$\frac{d\Gamma}{d\alpha} = \frac{1}{2\pi} \left[A \cos \alpha + B \sin \alpha + C \right] \quad \alpha \in [-\pi, \pi]$$

- The angular terms are given by kinematics / spin only.
- Remember: $\frac{d\sigma}{d\Omega}(e^+e^- \to \mu^+\mu^-) = \frac{\alpha^2}{4s} \left(1 + \cos^2\theta\right)$

Essentials of the $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ analysis

$$\frac{d\Gamma}{d\alpha} = \frac{1}{2\pi} \left[A \cos \alpha + B \sin \alpha + C \right] \quad \alpha \in [-\pi, \pi]$$

- The coefficients contain the physics-information we are interested in.
- Do: Run an experiment, collect data, select your decay, plot number of events as a function of α.
- Fit the angular distribution in collision data with the pdf and extract the coefficients.
- Ask a theorist and compare prediction with experimental result.

Folding technique (I)

- Suppose you don't have enough data to fit both terms.
- Solution: Use a variable transformation ("folding"). Example:

$$\begin{array}{rcl} \frac{\mathrm{d}\Gamma}{\mathrm{d}\alpha} &=& \frac{1}{2\pi} \left[A\cos\alpha + B\sin\alpha + C \right] & \alpha \in [-\pi,\pi] \\ \alpha \to -\alpha & \mathrm{if} & \alpha < 0 \\ & \frac{\mathrm{d}\Gamma}{\mathrm{d}\alpha} &=& \frac{1}{\pi} \left[A\cos\alpha + C \right] & \alpha \in [0,\pi] \end{array}$$

• By folding we can use symmetries in the angular distribution to cancel observables without loosing sensitivity. Note: The angular terms are orthogonal.

Folding technique (II)



- Apply transformation to the pdf and to the dataset.
- Results:
 - + $A=1.03\pm0.05$ (without folding)
 - + $A=1.05\pm0.05$ (with folding)
- We have determined A!

And now the real $B^0\!\to K^{*0}\mu^+\mu^-$ analysis

 $B^0\!\to K^{*0}\mu^+\mu^-$ decay topology



Particle	mass	lifetime ($c au$)
B^0	5279 MeV/ c^2	491.1 μm
K^{*0}	892 MeV/ c^2	$pprox 3 \cdot 10^{-12} \mu \mathrm{m}$

 $B^0 \rightarrow K^{*0} \mu^+ \mu^-$: Rare, but exciting



- \mathcal{B} = $(1.05^{+0.16}_{-0.13}) \times 10^{-6}_{\text{[PDG]}}$
- Pseudoscalar \rightarrow Vector-Vector decay: Plenty of observables in the angular distribution.

$B^0 \rightarrow K^{*0} \mu^+ \mu^-$ angular distribution (I)



- Decay can be fully described by three angles ($\theta_\ell, \theta_K, \phi$) and the dimuon invariant mass (square) q^2 .



$B^0 \rightarrow K^{*0} \mu^+ \mu^-$ angular distribution (II)

$$\begin{aligned} \frac{\mathrm{d}^4(\Gamma+\bar{\Gamma})}{\mathrm{d}\cos\theta_\ell\,\mathrm{d}\cos\theta_K\,\mathrm{d}\phi\,\mathrm{d}q^2} &= \frac{9}{32\pi} \left[\frac{3}{4} (1-F_L) \sin^2\theta_K + F_L \cos^2\theta_K + \right. \\ &\left. \frac{1}{4} (1-F_L) \sin^2\theta_K \cos 2\theta_\ell - F_L \cos^2\theta_K \cos 2\theta_\ell + \right. \\ &\left. S_3 \sin^2\theta_K \sin^2\theta_\ell \cos 2\phi + S_4 \sin 2\theta_K \sin 2\theta_\ell \cos \phi + \right. \\ &\left. S_5 \sin 2\theta_K \sin \theta_\ell \cos \phi + S_6 \sin^2\theta_K \cos \theta_\ell + \right. \\ &\left. S_7 \sin 2\theta_K \sin \theta_\ell \sin \phi + \right. \\ &\left. S_8 \sin 2\theta_K \sin 2\theta_\ell \sin \phi + S_9 \sin^2\theta_K \sin^2\theta_\ell \sin 2\phi \right] \end{aligned}$$

- The F_L, S_i depend on q^2 and contain the information we are interested in.
- The angular terms are... the angular terms.
- Note that this formula adds $B^0 \to K^{*0} \mu^+ \mu^-$ and $\overline{B}{}^0 \to \overline{K}{}^{*0} \mu^+ \mu^$ i.e. it's a \mathcal{CP} average.

$B^0 \rightarrow K^{*0} \mu^+ \mu^-$ angular distribution (II)

- This is the full angular distribution of $B^0 \to K^{*0} \mu^+ \mu^-$, neglecting lepton masses (and scalar and tensor contributions).
- There are 8 independent, ${\cal CP}$ averaged observables that all can be measured experimentally.
- Could in principle also measure CP asymmetric observables, but then could not profit from adding the datasets.



$B^0 \rightarrow K^{*0} \mu^+ \mu^-$ Angular distribution (III)

- In 2011, LHCb reconstructed \approx 900 $B^0 \to K^{*0} \mu^+ \mu^-$ events: Not enough for full angular fit.
- Apply "folding" technique: $\phi \rightarrow \phi + \pi$ for $\phi < 0$. This cancels four terms in the total angular distribution.
- And leaves:

$$\begin{split} \frac{\mathrm{d}^4(\Gamma+\bar{\Gamma})}{\mathrm{d}\cos\theta_\ell\,\mathrm{d}\cos\theta_K\,\mathrm{d}\phi\,\mathrm{d}q^2} = & \frac{9}{32\pi} \left[\frac{3}{4} (1-F_L) \sin^2\theta_K + F_L \cos^2\theta_K + \frac{1}{4} (1-F_L) \sin^2\theta_K \cos 2\theta_\ell \right. \\ & - F_L \cos^2\theta_K \cos 2\theta_\ell + \\ & S_3 \sin^2\theta_K \sin^2\theta_\ell \cos 2\phi + \\ & S_6 \sin^2\theta_K \cos \theta_\ell + \\ & S_9 \sin^2\theta_K \sin^2\theta_\ell \sin 2\phi \, \big] \end{split}$$

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• This expression was fitted to the 1 fb⁻¹ of LHCb data at $\sqrt{s} = 7$ TeV in 2011.



- Select signal events with a multivariate classifier (BDT): Based on kinematic quantities (IP, pointing angle, $p_{\rm T}$) and particle identification for μ , π , K
- Dominated by $B^0\to J/\psi\,K^{*0}$ and $B^0\to\psi(2S)K^{*0}$ in two regions of $q^2\colon$ Cut out.



EXPERIMENTAL ASPECTS (II)



- Peaking background due to misidentification of particles. e.g. $B^0_s \to \phi \mu^+ \mu^-$, where $K \to \pi$.
- Evaluate $m_{K\pi}$ mass under hypothesis that the π is actually a K. Does it peak in the ϕ region?
- Other peaking backgrounds like $B^0 \to J\!/\!\psi\,K^{*0}$, where $\pi \to \mu$ and $\mu \to \pi$



EXPERIMENTAL ASPECTS (III)



- Remember: We want to measure an angular distribution and extract physics parameters.
- We need to be sure, the angular distribution reflects the physics.
- Acceptance of detector distorts angular distribution. Need event-by-event correction, determined on simulation.
- Need to have a simulation describing collision data: Correct for particle ID and efficiency (tracking, trigger, ...)-differences in simulation and collision data.

S-wave / Background



• $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ is contaminated with S-wave $K\pi$ contributions, stemming from non-resonant decays or higher $K_{(i)}^{(*)}$ states.

- Ideally one would fit for this contribution. However, this adds many terms in the angular distribution.
- Instead: Estimate the S-wave contribution and check with simulation how large the effect on the results is. Add to systematic uncertainty.

Distribution of events in q^2 (I)

- Told you that F_L, S_i depend on q^2 .
- Need to parametrize / bin in q^2 to understand dependence.
- This analysis uses 6 q^2 bins. The binning scheme was copied from the analysis of the Belle collaboration.
- See later for a possible unbinned way (in a slightly different context).



DISTRIBUTION OF EVENTS IN q^2 (II)





EXAMPLE OF ANGULAR DISTRIBUTION



Results

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DIFFERENTIAL BRANCHING FRACTION



- Note that the theoretical uncertainty is larger than the experimental one.
- This is / was a major showstopper for discovering smallish effects of new physics.
- However, new lattice results can reduce the uncertainty for high q^2 .

COMPARISON WITH OTHER EXPERIMENTS



More observables

- Angular distribution has 8 independent observables in total. Have only measured 4 of them due to folding. Want to measure the remaining ones as well.
- Could now go on and devise other foldings to extract the remaining S_4, S_6, S_7 and S_8 .
- Or we can try something slightly different...



Esses and Pees

- While all S_i observables can be predicted theoretically, they have large theoretical uncertainties.
- We can do a basis-transformation:
 - Old basis: F_L , S_3-S_9 (8 imes large theo. uncertainty)
 - New basis: F_L , $\frac{d\mathcal{B}}{dq^2}$, $P_1, P_2, P_3, P_4', P_5', P_6'$ (2 × large theo. uncertainty, 6 × small theo. uncertainty)

$$\begin{split} P_4' &= \frac{S_4}{\sqrt{F_L(1-F_L)}} \quad P_5' = \frac{S_5}{\sqrt{F_L(1-F_L)}} \quad P_6' = \frac{S_7}{\sqrt{F_L(1-F_L)}} \text{ [sic!]} \\ P_8' &= \frac{S_8}{\sqrt{F_L(1-F_L)}} \text{ (not fully independent)} \end{split}$$

- Replace the S_i observables with the $P_i^{(\prime)}$ observables and determine their values on collision data.

$B^0 \rightarrow K^{*0} \mu^+ \mu^-$ Folded Angular distribution

- The first folding gave us with one transformation 4 observables.
- To extract the other observables, more effort is needed.
- Example: Extracting P'_5 :

$$\begin{array}{ll} \phi \rightarrow -\phi & \mbox{for} & \phi < 0 \\ \theta_\ell \rightarrow \pi - \theta_\ell & \mbox{for} & \theta_\ell > \pi/2 \end{array}$$

• Similar foldings for P'_4, P'_6, P'_8 .



$B^0 \rightarrow K^{*0} \mu^+ \mu^-$ folded angular distribution

• The folding for P_5' leads to:

$$\begin{split} \frac{\mathrm{d}^4(\Gamma+\bar{\Gamma})}{\mathrm{d}\cos\theta_\ell\,\mathrm{d}\cos\theta_K\,\mathrm{d}\phi\,\mathrm{d}q^2} = & \frac{9}{8\pi} \left[\frac{3}{4} (1-F_L) \sin^2\theta_K + F_L \cos^2\theta_K + \right. \\ & \left. \frac{1}{4} (1-F_L) \sin^2\theta_K \cos 2\theta_\ell - F_L \cos^2\theta_K \cos 2\theta_\ell + \right. \\ & \left. \frac{1}{2} S_3 \sin^2\theta_K \sin^2\theta_\ell \cos 2\phi_+ \right. \\ & \left. \sqrt{F_L (1-F_L} P_5' \sin 2\theta_K \sin \theta_\ell \cos \phi_{-} \right] \end{split}$$

- Only three observables left after the folding. Now we can fit the distribution.
- Only one of them we are interested in, the other two are "nuisance parameters".
- Selection, corrections, etc. all are the same as for the "first" analysis.

EXAMPLE OF ANGULAR DISTRIBUTION



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P_4' and P_5'



- Analysis is performed in the same six bins of q^2 as the first analysis.
- Good agreement for P_4' for the full q^2 range.
- Disagreement for P_5' for low q^2 .
- Discrepancy in third bin is about 4 standard deviations. The chance of this happening in one bin out of 24 is about 0.5%.

P_6' and P_8'



- Good agreement for P_6' for the full q^2 range.
- Good agreement for P_8' for the full q^2 range.

STATISTICAL UNCERTAINTIES



• For some bins the likelihood looked was perfectly parabolic, for some not. Evaluate statistical uncertainty using "Feldmann-Cousins".

• FC:

- For each possible value of *x*, generate toys (with: removing events and correcting for acceptance).
- Order them according to $R = \frac{\mathcal{L}(x|\mu)}{\mathcal{L}(x|\mu_{best})}$, where μ_{best} is the value of μ that maximises $\mathcal{L}(x|\mu)$.

- Determine 68% CL.
- Construct band and read off interval.

Measuring the zero-crossing point of $A_{FB}(I)$



- Zero-crossing point of A_{FB} is a very clean measurement, as the form factors cancel (to first order).
- $A_{FB} = \frac{\text{Forward}-\text{Backward}}{\text{Forward}+\text{Backward}}$. "Forward" = $\cos \theta_{\ell} > 0$
- Zero-crossing point was extracted using "unbinned counting" technique: Make a 2D unbinned likelihood fit to (q^2 , mass) for "forward" and "backward" events (with respect to $\cos \theta_{\ell}$).

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Measuring the zero-crossing point of A_{FB} (II)



• Extract
$$A_{FB} = \frac{N_F \cdot PDF_F(q^2) - N_B \cdot PDF_B(q^2)}{N_F \cdot PDF_F(q^2) + N_B \cdot PDF_B(q^2)}$$

- Standard Model theory predicts zero-crossing in 4.0 - 4.3 $\,{\rm GeV}^2/c^4$ (central values)

[JHEP 1201 (2012) 107][Eur. Phys. J. C41 (2005), 173][Eur. Phys. J. C47 (2006) 625]

• LHCb result: $4.9\pm0.9\,{
m GeV^2}/c^4$

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Yes, we did some crosschecks



- Surely, if there is a discrepancy in P_5^\prime , there is also one in $S_5.$
- Measure S_5 with a "counting" experiment (similar to zero-crossing point) and with an angular fit and compare results.
- Can define S_5 as an asymmetry between two type of events: $S_5=\frac{\#\text{type1}-\#\text{type2}}{\#\text{type1}+\#\text{type2}}$
- There is excellent agreement between fitting and counting.

Yes, we did more crosschecks...

- Cut very hard in selection until essentially no background is left. No effect.
- Apply selection, data-simulation corrections, acceptance correction to $B^0 \to J/\psi \, K^{*0}$. The values come out as predicted.
- Evaluate many systematic effects: Background angular distribution, signal mass distribution, removing events at large angles, neglecting acceptance correction, ...
- None had a seizable effect.

WHAT IS IT? POSSIBLE ANSWERS:

- A statistical fluctuation. The chance of one bin fluctuating that much (assuming all bins independent) is 0.5%.
- A peaking background nobody could think of. Something else, nobody could think of...

- An underestimation of the theoretical uncertainty.
- If you dare to believe: New physics.

The future!

- Everything I showed so far was performed on data from 2011.
- We have 2 fb⁻¹ more to analyse, giving in total \approx 3000 events.
- What can we do with them?
- Goal would be to do a full angular analysis without folding.
- None of these studies is public yet, cannot show too much...



Full angular analysis

- In principle would like to fit all observables at once to get the values and the correlation matrix.
- Would also like to have a different (finer) binning scheme, to take steep shapes better into account.
- And would like to disentangle B^0 and \overline{B}^0 .
- Would also like to have sunny weather every day.
- Realistic seems a full angular analysis with the same binning scheme or again folding with a finer binning scheme. But not both.
- It might also be possible to gain back the correlation matrix from toy studies. This would allow folding (=more stable) fits and provide the same information as the full analysis.





- $S_i = f_i(A_{\perp}^L, A_{\parallel}^L, A_0^L, A_{\perp}^R, A_{\parallel}^R, A_0^R)$. Can we measure the amplitudes directly?
- Need to parametrize q^2 dependence: $lpha+eta q^2+rac{\gamma}{q^2}.$
- Can in the end still build observables out of the amplitudes.
- Looks quite promising at the moment, but will be restricted to $q^2=1-6~{
 m GeV^2}/c^4$ (as q^2 parametrisation does not hold anywhere else).

Moment analysis

- All angular terms are orthonormal.
- Basic linear algebra tells you: $g = \sum_i c_i g_i$ with $\langle g_i || g_j
 angle = \delta_{ij}$
- $\Rightarrow c_i = \langle g || g_i \rangle$
- → To extract the angular coefficients, one can multiply distributions with each other.
- Looks quite promising at the moment, but study is only in an early stage.
- A nice thing about the moment analysis: The S-wave terms are orthogonal to all other (P-wave) terms, so they don't need special treatment.
- However, still need to care about acceptance correction.

OTHER EW PENGUINS





- There are other electroweak penguin decays which are sensitive to the same underlying physics: $B_s^0 \rightarrow \phi \mu^+ \mu^-$, $\Lambda_b^0 \rightarrow \Lambda \mu^+ \mu^-$, ...
- Less events than for $B^0
 ightarrow K^{*0} \mu^+ \mu^-$, angular analysis difficult.
- Isn't it fascinating that all branching fractions we measure are at the low end of the prediction?



SUMMARY

- Presented the 2012 & 2013 analyses of $B^0 \rightarrow K^{*0} \mu^+ \mu^-.$
- Have seen some "interesting" effects in the 2011 data.
- Looking forward to analysing the 2011+2012 data.
- Atlas & CMS can analyse this decay as well...



fin



• Only angle $heta_\ell$ and q^2 for description of decay:

 $B^+ \rightarrow K^+ \mu^+ \mu^-$

$$\frac{1}{\Gamma} \frac{\mathrm{d}\Gamma}{\mathrm{d}\cos\theta_{\ell}} = \frac{3}{4} (1 - F_H) \sin^2\theta_{\ell} + \frac{1}{2} F_H + A_{FB} \cos\theta_{\ell} \quad (1)$$

- Branching fraction smaller than for $B^0 \to K^{*0} \mu^+ \mu^-$, but cleaner. About 1200 events to analyse in 1 fb⁻¹.
- Good agreement with Standard Model, including resonance at high- q^2 (compatible with $\psi(4160)$).

 $B^+ \rightarrow K^+ \mu^+ \mu^-$



 $B^0_s \to \phi \mu^+ \mu^-$



- Very similar to $B^0 \rightarrow K^{*0} \mu^+ \mu^-$, however, less B^0_s produced than B^0 . Only \sim 175 signal events in 1 fb⁻¹.
- Decay is not self-tagging, as $\phi
 ightarrow K^+K^-$.
- Need to restrict to observables invariant under $B^0_s \leftrightarrow \overline{B}^0_s$: F_L , $S_{3,4,7}$, $A_{5,6,8,9}$.
- Only projections in one angles fitted, not full 3D-fit.
- Angular observables show good agreement with SM.

[JHEP 1307 (2013) 084]

 $B^0_s\!\to \phi\mu^+\mu^-$



However the branching fraction is significantly lower than the SM prediction.



[PLB B725 (2013) 25]

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 $\Lambda_h^0 \to \Lambda \mu^+ \mu^-$



- Even less signal than for $B_s^0 \rightarrow \phi \mu^+ \mu^-$, \sim 80 events in 1 fb⁻¹.
- Still most precise measurement of branching fraction.
- Basically no events at low q^2 (but very large uncertainties).

 $B^+ \rightarrow \pi^+ \mu^+ \mu^-$



- b
 ightarrow d process, suppressed by $|V_{td}/V_{ts}|^2$ compared to b
 ightarrow s
- LHCb observed \sim 25 signal candidates in 1 fb $^{-1}$..
- Measured branching fraction of: $(2.3\pm0.6\pm0.1)\cdot10^{-8}$, in good agreement with Standard Model.

More penguins

- $B^0 \rightarrow K^{*0} e^+ e^-$: Interesting at low q^2 , where muon mass cannot be neglected anymore.
- More EW penguin measurements: \mathcal{CP} asymmetry and isospin asymmetry in $B^0 \rightarrow K^{*0} \mu^+ \mu^-$, $B^+ \rightarrow K^+ \mu^+ \mu^-$.
- None of the other modes (except isospin asymmetry) shows such a large deviation.
- However, none of the other modes has the same sensitivity to " P_5' -physics" as $B^0 \to K^{*0} \mu^+ \mu^-.$



BDT INPUT VARIABLES

- the B^0 pointing to the primary vertex, flight-distance and IP χ^2 with respect to the primary vertex, p_T and vertex quality (χ^2);
- the K^{*0} and dimuon flight-distance and IP χ² with respect to the primary vertex (associated to the B⁰), p_T and vertex quality (χ²);
- the impact parameter χ^2 and the $\Delta LL(K \pi)$ and $\Delta LL(\mu \pi)$ of the four final state particles.



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Possible interpretations (I)



- Matias et al. did a combined fit of observables of $B^0 \to K^{*0} \mu^+ \mu^-$, $B^0_s \to \mu^+ \mu^-$, $B^0 \to K^{*0} \gamma$ to extract the Wilson coefficients.
- Split Wilson coefficients in $\mathcal{C}_i^{(\prime)} = \mathcal{C}_{i,SM}^{(\prime)} + \mathcal{C}_{i,NP}^{(\prime)}$
- Determine best fit point and confidence intervals.
- Looks like a clear case for NP...

Possible interpretations (II)



- Straub et al. did a combined fit of observables of $B^0 \to K^{*0} \mu^+ \mu^-$, $B^+ \to K^+ \mu^+ \mu^-$, $B^0 \to \mu^+ \mu^-$, $B^0 \to K^{*0} \gamma$. They also included results from other experiments besides LHCb.
- The trend is the same as for Matias et al., however the picture is a bit less clear.

Possible interpretations (III)



- Van Dyk et al. did a Bayesian analysis using observables of $B^0 \rightarrow K^{*0}\mu^+\mu^-$, $B^+ \rightarrow K^+\mu^+\mu^-$, $B^0_s \rightarrow \mu^+\mu^-$, $B^0 \rightarrow K^{*0}\gamma$ (and other information) where the QCD-uncertainties were allowed to float (using a prior).
- They conclude: "In the absence of substantial improvements in the handling of subleading contributions to the $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ amplitudes and given the statistical evaluation, we are therefore forced to conclude that the SM interpretation of the data is more economical than a New Physics hypothesis."

 $A_T^{(2)}$ and $A_T^{(Re)}$





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$$S_3 = \frac{1}{2}(1 - F_L)A_T^{(2)}$$

• $A_{FB} = \frac{3}{4}(1 - F_L)A_T^{(Re)}$

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Likelihood for P'_5 , bin 3



• (Profile) likelihood for P_5^\prime in bin 3.

