

Standard Model: Flavor mixing and CP violation

Flavor Mixing and CP Violation

1. CKM Matrix
2. Mixing of neutral mesons
3. CP violation
4. Precision Study of B mesons at LHC

1. CKM Matrix

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \cdot \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

weak eigenstates

CKM matrix

mass eigenstates

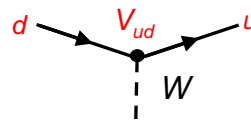
Unitarity

$$V_{CKM} V_{CKM}^+ = 1$$

Charged currents:

$$J_\mu^+ \propto (\bar{u}, \bar{c}, \bar{t}) \gamma_\mu (1 - \gamma_5) \begin{pmatrix} d' \\ s' \\ b' \end{pmatrix}$$

weak



$$= (\bar{u}, \bar{c}, \bar{t}) \gamma_\mu (1 - \gamma_5) V_{CKM} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

mass/
flavor

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1.1 Parameters of CKM matrix

Number of independent parameters:

- 18 parameter (9 complex elements)
- 5 relative quark phases (unobservable)
- 9 unitarity conditions
- =4 independent parameters: **3 angles + 1 phase**

PDG parametrization

3 Euler angles

$$\theta_{23}, \theta_{13}, \theta_{12}$$

1 Phase

$$\delta$$

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

$$\begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix}$$

where $c_{ij} = \cos\theta_{ij}$, $s_{ij} = \sin\theta_{ij}$

Magnitude of elements

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} u & d & s & b \\ c & & & \\ t & & & \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

complex in $O(\lambda^3)$

Wolfenstein Parametrization

$$\lambda, A, \rho, \eta, \lambda = 0.22$$

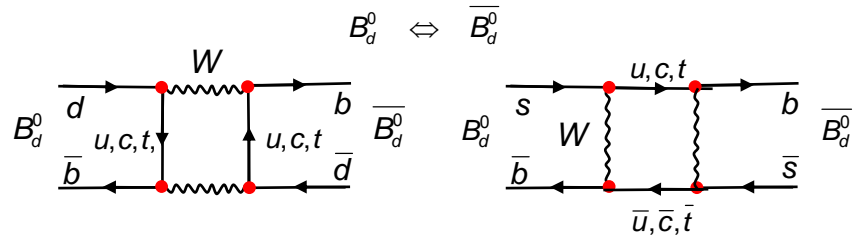
$$V_{CKM} = \begin{pmatrix} 1 - \frac{\lambda^2}{2} & \lambda & V_{ub} = |V_{ub}|e^{-i\gamma} \\ -\lambda & 1 - \frac{\lambda^2}{2} & A\lambda^3(\rho - i\eta) \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \\ V_{td} = |V_{td}|e^{-i\beta} & & \end{pmatrix} + O(\lambda^4)$$

Reflects hierarchy of elements in $O(\lambda)$

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2. Mixing of neutral mesons

The quark mixing results into several interesting “loop” effects:
Standard Model predicts oscillations of neutral mesons



Neutral mesons: $|P^0\rangle: K^0 = |d\bar{s}\rangle$ $D^0 = |\bar{u}c\rangle$ $B_d^0 = |d\bar{b}\rangle$ $B_s^0 = |s\bar{b}\rangle$
 $|\bar{P}^0\rangle: \bar{K}^0 = |\bar{d}s\rangle$ $\bar{D}^0 = |\bar{u}c\rangle$ $\bar{B}_d^0 = |\bar{d}b\rangle$ $\bar{B}_s^0 = |\bar{s}b\rangle$

discovery of mixing 1960 2007 1987 2006

2.1 Mixing phenomenology

Consider time dependent Schrödinger eq. for 2 component wave function $\begin{pmatrix} B^0 \\ \bar{B}^0 \end{pmatrix}$:

$$i \frac{d}{dt} \begin{pmatrix} B^0 \\ \bar{B}^0 \end{pmatrix} = \mathbf{H} \begin{pmatrix} B^0 \\ \bar{B}^0 \end{pmatrix} = \left(\mathbf{M} - \frac{i}{2} \mathbf{\Gamma} \right) \begin{pmatrix} B^0 \\ \bar{B}^0 \end{pmatrix} = \begin{pmatrix} m_{11} - \frac{i}{2} \Gamma_{11} & m_{12}^* - \frac{i}{2} \Gamma_{12}^* \\ m_{12} - \frac{i}{2} \Gamma_{12} & m_{22} - \frac{i}{2} \Gamma_{22} \end{pmatrix} \begin{pmatrix} B^0 \\ \bar{B}^0 \end{pmatrix}$$

Dispersive & absorptive

As the matrix H is not diagonal B^0 and \bar{B}^0 are not mass eigenstates (defined as state in which to particle propagates in time).

Diagonalizing H of finds the mass eigenstates

$$\begin{aligned} |B_L\rangle &= p |B^0\rangle + q |\bar{B}^0\rangle & \text{with } m_L, \Gamma_L & & |p|^2 + |q|^2 = 1 \\ |B_H\rangle &= p |B^0\rangle - q |\bar{B}^0\rangle & \text{with } m_H, \Gamma_H & & \text{complex coefficients} \end{aligned}$$

Free particle wave function $|B_{H,L}(t)\rangle = |B_{H,L}(0)\rangle \cdot \underbrace{e^{-im_{H,L}t} \cdot e^{-\frac{1}{2}\Gamma_{H,L}t}}_{b_{H,L}(t)}$ $\Delta m = m_H - m_L$
 $\Delta \Gamma = \Gamma_H - \Gamma_L$

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Time development of B^0 and \bar{B}^0

Time development of the flavor eigenstates given by the linear combination B_L/B_H

$$|B^0\rangle = \frac{1}{2p}(|B_L\rangle + |B_H\rangle) \quad |\bar{B}^0\rangle = \frac{1}{2q}(|B_L\rangle - |B_H\rangle)$$

$$\begin{aligned} |\psi_{B^0}(t)\rangle &= \frac{|B_L(t)\rangle + |B_H(t)\rangle}{2p} = \frac{1}{2p} \left(b_L(t) \cdot (p|B^0\rangle + q|\bar{B}^0\rangle) + b_H(t) \cdot (p|B^0\rangle - q|\bar{B}^0\rangle) \right) \\ &= f_+(t) \cdot |B^0\rangle + \frac{q}{p} f_-(t) \cdot |\bar{B}^0\rangle \quad \text{with} \quad f_{\pm}(t) = \frac{1}{2} \cdot \left[e^{-im_H t} e^{-\Gamma_H t/2} \pm e^{-im_L t} e^{-\Gamma_L t/2} \right] \end{aligned}$$

$$|\psi_{\bar{B}^0}(t)\rangle = f_+(t) \cdot |\bar{B}^0\rangle + \frac{p}{q} f_-(t) \cdot |B^0\rangle$$

$$B^0 \quad \begin{aligned} P(B^0(0) \rightarrow B^0(t)) &= |f_+(t)|^2 \\ P(B^0(0) \rightarrow \bar{B}^0(t)) &= \left| \frac{q}{p} \right|^2 |f_-(t)|^2 \end{aligned}$$

$$\bar{B}^0 \quad \begin{aligned} P(\bar{B}^0(0) \rightarrow \bar{B}^0(t)) &= |f_+(t)|^2 \\ P(\bar{B}^0(0) \rightarrow B^0(t)) &= \left| \frac{p}{q} \right|^2 |f_-(t)|^2 \end{aligned}$$

Oscillation frequency

$$P(B^0 \rightarrow B^0) = P(\bar{B}^0 \rightarrow \bar{B}^0) = \frac{1}{4} \left[e^{-\Gamma_L t} + e^{-\Gamma_H t} + 2e^{-(\Gamma_L + \Gamma_H)t/2} \cos \Delta m t \right]$$

CPT

$$P(B^0 \rightarrow \bar{B}^0) = \frac{1}{4} \left| \frac{q}{p} \right|^2 \left[e^{-\Gamma_L t} + e^{-\Gamma_H t} - 2e^{-(\Gamma_L + \Gamma_H)t/2} \cos \Delta m t \right]$$

$$P(\bar{B}^0 \rightarrow B^0) = \frac{1}{4} \left| \frac{p}{q} \right|^2 \left[e^{-\Gamma_L t} + e^{-\Gamma_H t} - 2e^{-(\Gamma_L + \Gamma_H)t/2} \cos \Delta m t \right]$$

CP- violation in mixing:

$$P(B^0 \rightarrow \bar{B}^0) \neq P(\bar{B}^0 \rightarrow B^0) \Rightarrow \left| \frac{q}{p} \right| \neq 1$$

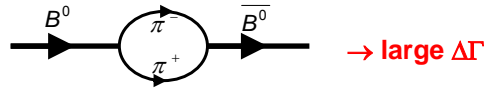
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2.2 Standard Model prediction for B^0 mixing

Mixing mechanisms:

- Mixing through decay:

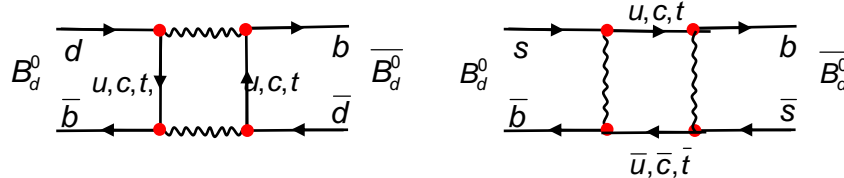
„long distant, on-shell states“



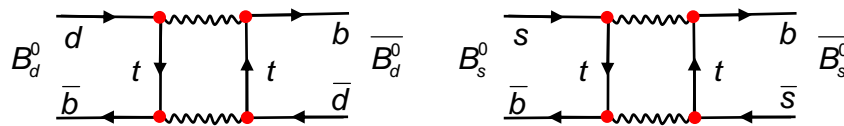
For B mesons there are many possible hadronic decays $\rightarrow \Gamma$ is large in addition decays like $B \rightarrow \pi\pi$ are suppressed

$$\Rightarrow y = \frac{\Delta\Gamma}{2\Gamma} \text{ is small} = \begin{cases} \approx 0 \text{ for } B_d^0 \\ \approx O(0.1) \text{ for } B_s^0 \end{cases} \Rightarrow \text{don't expect mixing via decay}$$

- Mixing through oscillation \rightarrow large Δm



- Standard Model result \rightarrow Significant contribution only from top loop



$$\Delta m \sim m_t^2 |V_{tb} V_{td}|^2 \sim m_t^2 \cdot O(\lambda^6) \quad \Delta m \sim m_t^2 |V_{tb} V_{ts}|^2 \sim m_t^2 \cdot O(\lambda^4)$$

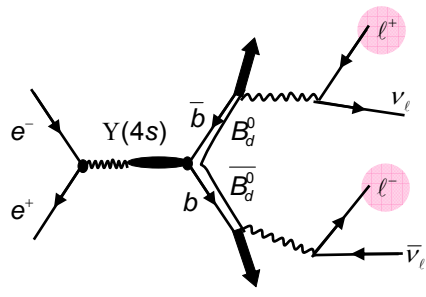
Large $\Delta m_{s,d}$: $\Delta m_s \sim 1/\lambda^2 \Delta m_d \rightarrow B_s$ osc. is about 35 times faster than B_d osc.

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2.3 Discovery of B^0 mixing

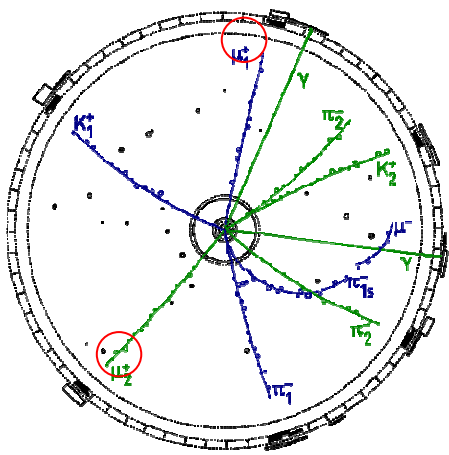
ARGUS 1987

First e^+e^- B factory at DESY:
 at $\sqrt{s} = 10.58$ GeV :
 $e^+e^- \rightarrow Y(4S) \rightarrow B^0\bar{B}^0$ } $\sigma(B\bar{B}) \approx 1\text{nb}$



Unmixed: $B^0\bar{B}^0 \rightarrow l^+l^-$

Mixed: $B^0B^0 \rightarrow l^+l^+$
 $\bar{B}^0\bar{B}^0 \rightarrow l^-l^-$ } Same charge



$B^0 \rightarrow D^{*-}\mu^+\nu_\mu$ $B^0 \rightarrow D^{*-}\mu^+\nu_\mu$

$\downarrow D^0\pi_s^-$ $\downarrow D^-\pi^0$

$\downarrow K^+\pi^-$ $\downarrow K^+\pi^-\pi^-$

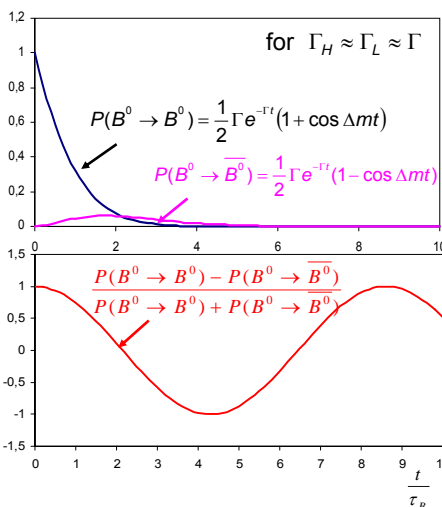
Experimental Status of B meson mixing

for $\Gamma_H \approx \Gamma_L \approx \Gamma$

$P(B^0 \rightarrow B^0) = \frac{1}{2}\Gamma e^{-\Gamma t}(1 + \cos \Delta m t)$

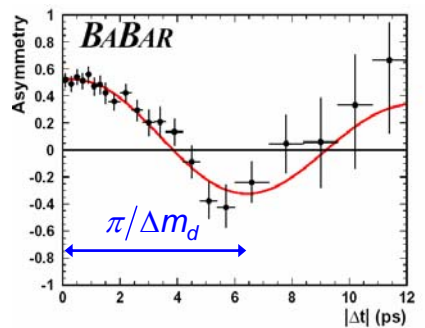
$P(B^0 \rightarrow \bar{B}^0) = \frac{1}{2}\Gamma e^{-\Gamma t}(1 - \cos \Delta m t)$

$\frac{P(B^0 \rightarrow B^0) - P(B^0 \rightarrow \bar{B}^0)}{P(B^0 \rightarrow B^0) + P(B^0 \rightarrow \bar{B}^0)}$



$A = \frac{\text{unmixed} - \text{mixed}}{\text{unmixed} + \text{mixed}}$

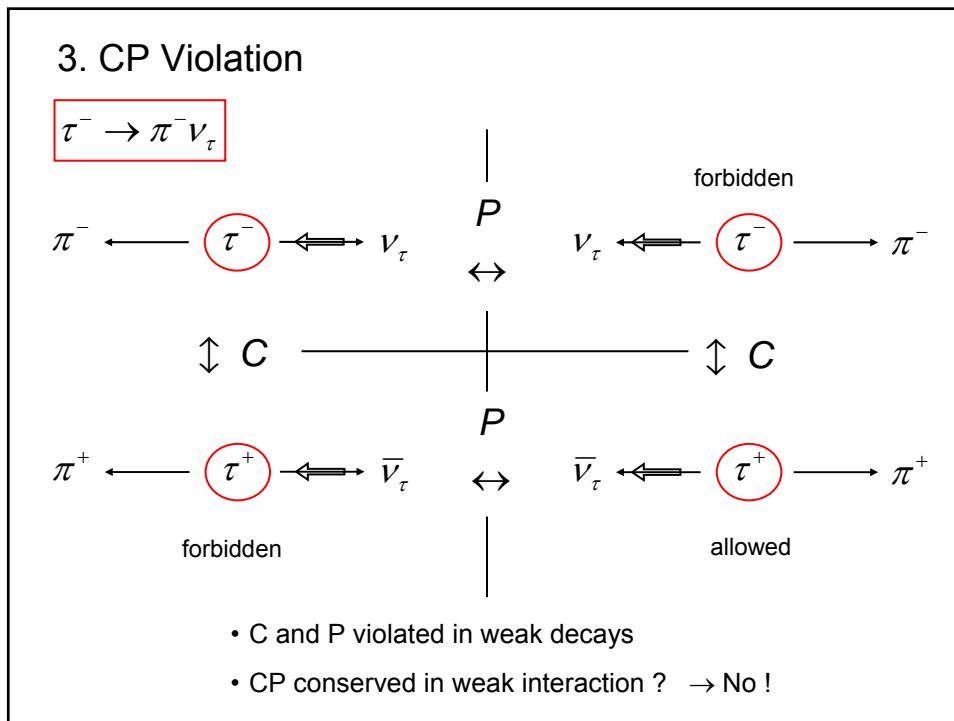
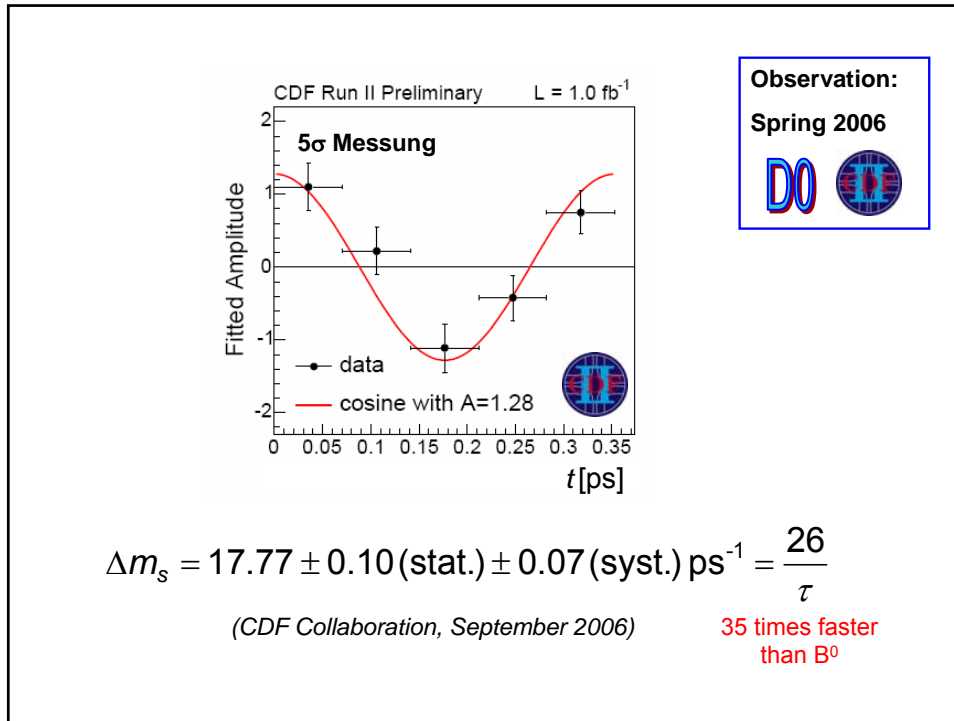
BABAR



$\Delta m_d = 0.506 \pm 0.006 \pm 0.004 \text{ ps}^{-1}$

$\approx \frac{0.774}{\tau_B}$

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3.1 Discovery of CP Violation in Kaon Decays

Observation of two neutral kaons K_L (long) and K_S (short) with different lifetimes:

$$\tau(K_L^0) = (51.7 \pm 0.4) \text{ ns} \gg \tau(K_S^0) = (0.089 \pm 0.001) \text{ ns}$$

$$K_L^0 \rightarrow 3\pi$$

$$CP = -1$$

$$K_S^0 \rightarrow 2\pi$$

$$CP = +1$$

$$K^0 = |d\bar{s}\rangle$$

$$\bar{K}^0 = |\bar{d}s\rangle$$

Interpretation: (neglecting possible CP violation)

$$|K_L\rangle = |K_2\rangle = \frac{1}{\sqrt{2}}(|K^0\rangle - |\bar{K}^0\rangle)$$

$$|K_S\rangle = |K_1\rangle = \frac{1}{\sqrt{2}}(|K^0\rangle + |\bar{K}^0\rangle)$$

$$CP|K_2\rangle = -|K_2\rangle$$

$$CP|K_1\rangle = +|K_1\rangle$$

Phase convention:

$$CP|K^0\rangle = |\bar{K}^0\rangle$$

$$CP|\bar{K}^0\rangle = |K^0\rangle$$

Large differences between lifetimes

$$\Delta m = (0.5303 \pm 0.0009) \cdot 10^{10} \text{ } \hbar\text{s}^{-1}$$

$$= (3.49 \pm 0.006) \cdot 10^{-12} \text{ MeV}$$

$$\Delta\Gamma = -11.182 \cdot 10^9 \text{ } \hbar\text{s}^{-1}$$

If no CPV:

$$|K_L\rangle = \frac{1}{\sqrt{2}}(|K^0\rangle - |\bar{K}^0\rangle) \quad CP = -1$$

should always decay into 3π :

$$CP(|3\pi\rangle) = -1$$

and never into 2π $CP(|2\pi\rangle) = +1$

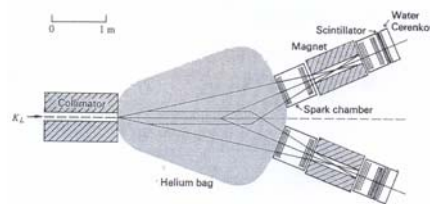
Explanation:

$$|K_L\rangle = \frac{1}{\sqrt{1+|\varepsilon|^2}}(|K_2\rangle - \varepsilon|K_1\rangle)$$

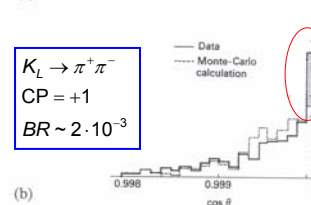
\uparrow $CP = -1$ $CP = +1$

Not a CP eigenstate: CP violation !

Christenson, Cronin, Fitch, Turlay, 1964



(a)



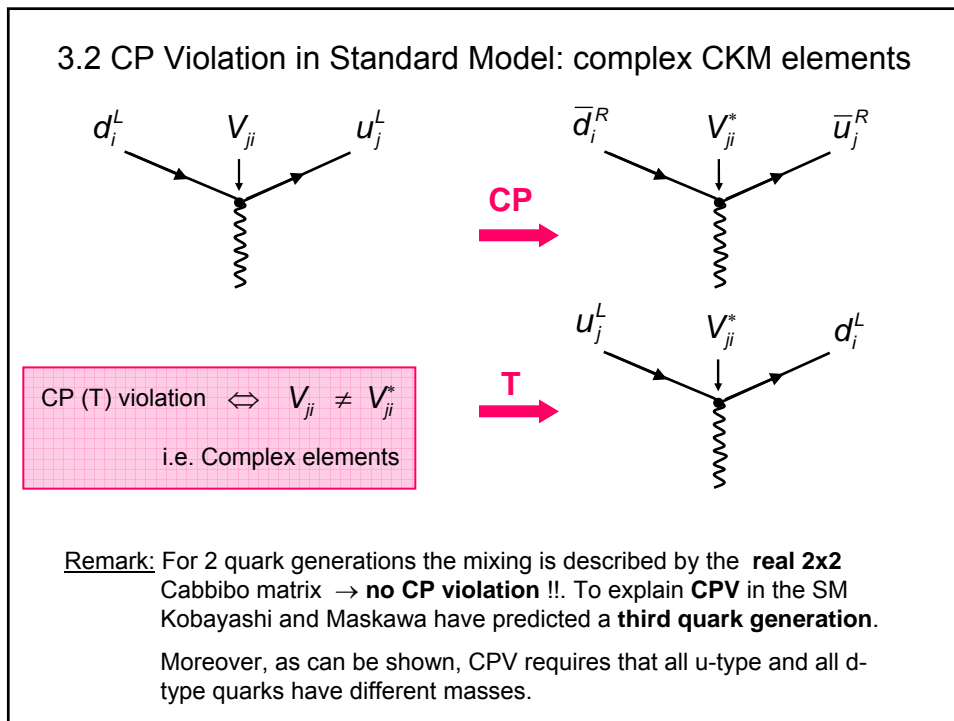
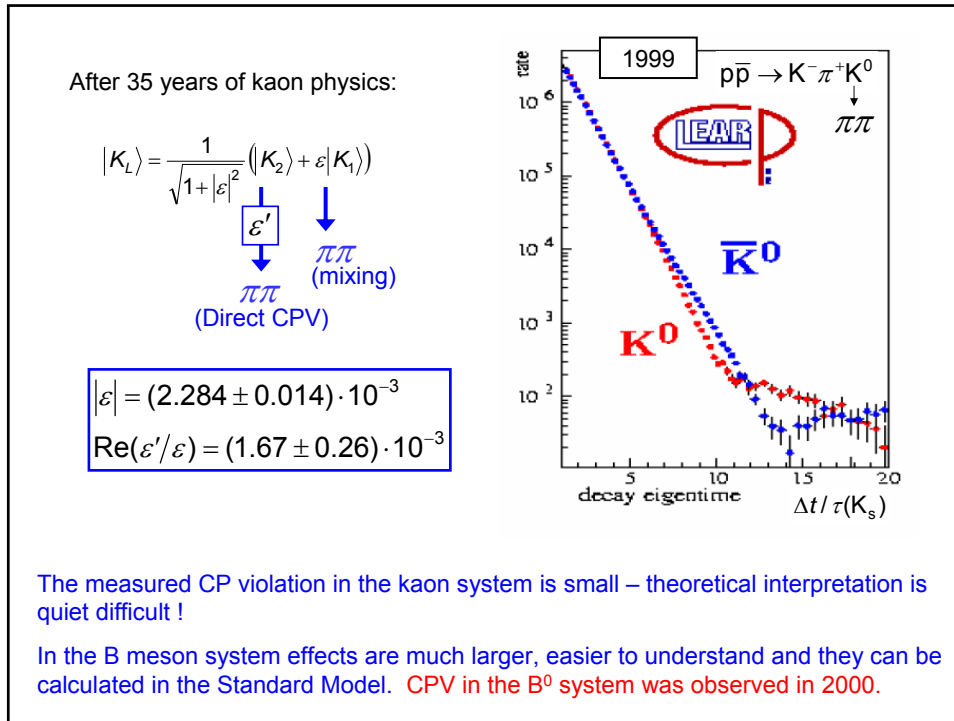
(b)

$$K_L \rightarrow \pi^+ \pi^-$$

$$CP = +1$$

$$BR \sim 2 \cdot 10^{-3}$$

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Unitarity Triangle

Unitary CKM matrix: $\mathbf{V}\mathbf{V}^\dagger = \mathbf{1}$ → 6 “triangle” relations in complex plane:

$$V = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$
 $V_{td}V_{ud}^* + V_{ts}V_{us}^* + V_{tb}V_{ub}^* = 0$

Important for \mathbf{B}_d and \mathbf{B}_s decays
 Real “triangles” only in case of CP violation: Tip / triangle area defines amount/strength of CPV!

Strength of CPV characterized by Jarlskog invariant (area) $J = \text{Im} (V_{ij} V_{kl} V_{il}^* V_{kj}^*)$
 In SM: $J = \text{Im}[V_{us} V_{cb} V_{ub}^* V_{cs}^*] = A^2 \lambda^6 \eta (1 - \lambda^2/2) + O(\lambda^{10}) \sim 10^{-5}$

Rescaled unitarity condition $V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$

$$\begin{pmatrix} V_{ud} & V_{us} & |V_{ub}|e^{-i\gamma} \\ V_{cd} & V_{cs} & V_{cb} \\ |V_{td}|e^{-i\beta} & V_{ts} & V_{tb} \end{pmatrix}$$

$\alpha \equiv \arg \left[-\frac{V_{td}V_{tb}^*}{V_{ud}V_{ub}^*} \right]$
 $\beta \equiv \arg \left[-\frac{V_{cd}V_{cb}^*}{V_{td}V_{tb}^*} \right]$
 $\gamma \equiv \arg \left[-\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*} \right]$

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3.3 Observation of CP Violation

→ Phase measurement
→ Interference experiment

$B \rightarrow f$

$|A|^2 = A_1^2 + A_2^2 + 2A_1A_2 \cos(\phi_{CP} + \delta)$

$\bar{B} \rightarrow \bar{f}$

$|\bar{A}|^2 = A_1^2 + A_2^2 + 2A_1A_2 \cos(\phi_{CP} - \delta)$

Weak and CP invariant phase difference

Need two phase differences between A_1 and A_2 : Weak difference which changes sign under CP and another phase difference (strong) which is unchanged.

“3 Ways” of CP violation in meson decays

a) Direct CP violation

$A(B \rightarrow f) = |A| e^{i\phi} e^{i\delta}$

$\left| \frac{A_f}{\bar{A}_f} \right| \neq 1$

$P(\bar{B} \rightarrow \bar{f}) \neq P(B \rightarrow f)$

b) CP violation in mixing

$\left| \frac{q}{p} \right| \neq 1$

$P(B^0 \rightarrow \bar{B}^0) \neq P(\bar{B}^0 \rightarrow B^0)$

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c) CP violation through interference of mixed and unmixed amplitudes

$\Gamma(B_{t=0}^0 \rightarrow f)(t) \neq \Gamma(\bar{B}_{t=0}^0 \rightarrow f)(t)$

Asymmetrie modulated by $\sim \sin \Delta m t$

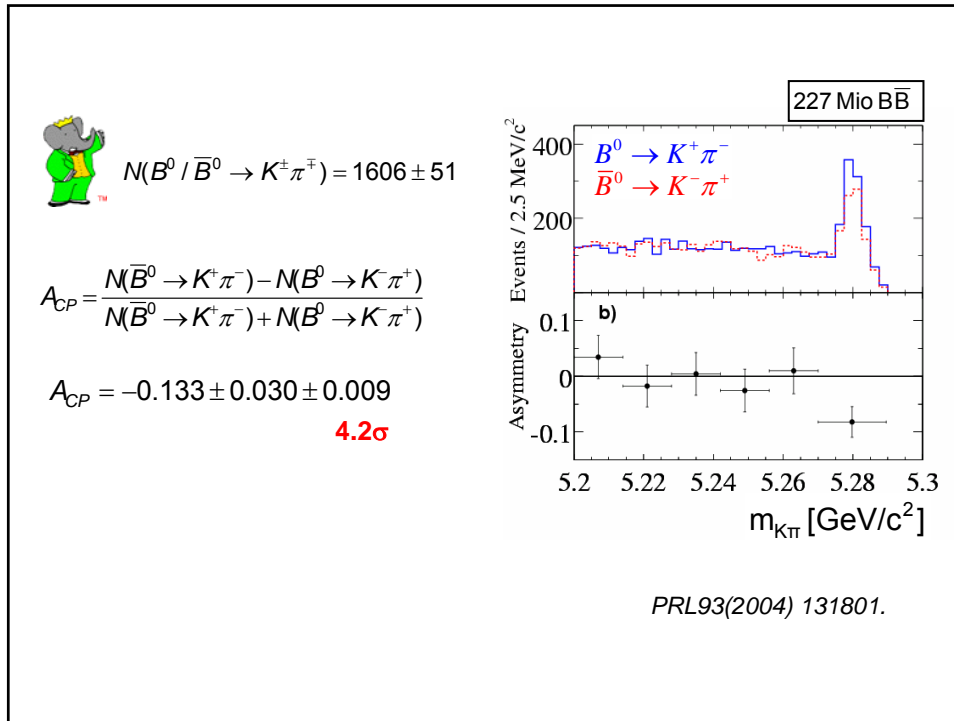
Combinations of the 3 ways are possible!

ad a) Direct CP violation (B system)

CP Asymmetrie $|\bar{A}|^2 - |A|^2 = 4|A_1||A_2| \sin \varphi \sin \delta$

Strong phase difference

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b) CP (T) violation in mixing

T violation
↔

$$\left| \frac{q}{p} \right| \neq 1 \quad P(B^0 \rightarrow \bar{B}^0) \neq P(\bar{B}^0 \rightarrow B^0)$$

Skipped.

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c) CP violation in interference between mixing and decay

$B^0 \rightarrow J/\psi K_S$

$\xrightarrow{\text{CP}}$

$\bar{B}^0 \rightarrow J/\psi K_S$

$\frac{q}{p} e^{i\pi/2} \sim e^{i2\beta} e^{i\pi/2}$

$\frac{p}{q} e^{i\pi/2} \sim e^{-i2\beta} e^{i\pi/2}$

$$|B^0 \rightarrow J/\psi K_S\rangle = A(f_+(t) + \lambda_{CP} f_-(t))$$

$$|\bar{B}^0 \rightarrow J/\psi K_S\rangle = \bar{A} \left(f_+(t) + \frac{1}{\lambda_{CP}} f_-(t) \right)$$

$$\lambda_{CP} \equiv \frac{q}{p} \cdot \frac{\bar{A}}{A}$$

SM prediction of λ_{CP} for $B^0 \rightarrow J/\psi K_S$ $\eta_{CP} = -1$

B^0 mixing

q/p

B^0 decay

$A \propto V_{cb} V_{cs}^*$

K^0 mixing

q_K / p_K

Same for all $ck\bar{K}^0$ channels

$$\lambda_{CP} = \frac{q}{p} \frac{\bar{A}}{A} = \frac{V_{tb}^* V_{td} V_{cb} V_{cs}^* V_{cs} V_{cd}^*}{V_{tb} V_{td}^* V_{cb}^* V_{cs} V_{cs}^* V_{cd}} = - \frac{V_{tb}^* V_{td} V_{cb} V_{cd}^*}{V_{tb} V_{td}^* V_{cb}^* V_{cd}} \approx -e^{-2i\beta}$$

Beside V_{td} all other CKM elements are real

$V_{td} \approx |V_{td}| e^{-i\beta}$

\Rightarrow

$|\lambda_{CP}| = 1$
 $\text{Im}(\lambda_{CP}) = \sin(2\beta)$

no direct CPV, no CPV in mixing

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Calculation of the time-dependent CP asymmetry

$$\Gamma(B^0 \rightarrow f_{CP})(t) \propto \frac{e^{-\Delta t/\tau_{B^0}}}{(1+|\lambda_{CP}|^2)} \times \left[\frac{1+|\lambda_{CP}|^2}{2} - \text{Im}(\lambda_{CP})\sin(\Delta m_d t) + \frac{1-|\lambda_{CP}|^2}{2} \cos(\Delta m_d t) \right]$$

$$\neq$$

$$\Gamma(\bar{B}^0 \rightarrow f_{CP})(t) \propto \frac{e^{-\Delta t/\tau_{B^0}}}{(1+|\lambda_{CP}|^2)} \times \left[\frac{1+|\lambda_{CP}|^2}{2} + \text{Im}(\lambda_{CP})\sin(\Delta m_d t) - \frac{1-|\lambda_{CP}|^2}{2} \cos(\Delta m_d t) \right]$$

$$A_{CP}(t) = \frac{\Gamma(\bar{B}^0(t) \rightarrow f_{CP}) - \Gamma(B^0(t) \rightarrow f_{CP})}{\Gamma(B^0(t) \rightarrow f_{CP}) + \Gamma(\bar{B}^0(t) \rightarrow f_{CP})} = [S_f \sin(\Delta m_d t) - \underbrace{C_f \cos(\Delta m_d t)}_{\text{negligible}}]$$

Time resolved

$$S_f = \frac{2\text{Im} \lambda_{CP}}{1+|\lambda_{CP}|^2} \quad C_f = \frac{1-|\lambda_{CP}|^2}{1+|\lambda_{CP}|^2}$$

Interference
= $\sin 2\beta$ for $B^0 \rightarrow J/\psi K_S$

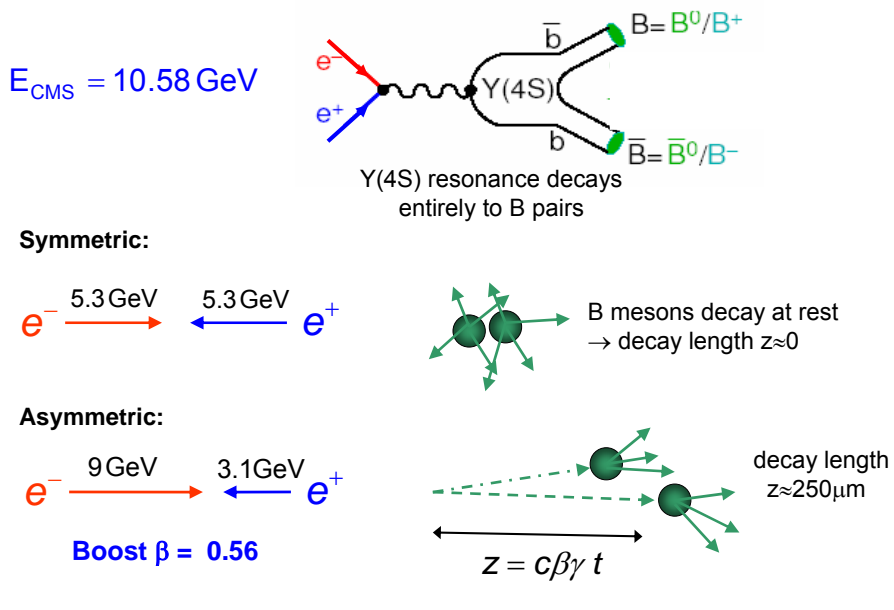
indicates direct CP violation
if $|q/p| \neq 1$

To measure CP violation in B_d system:

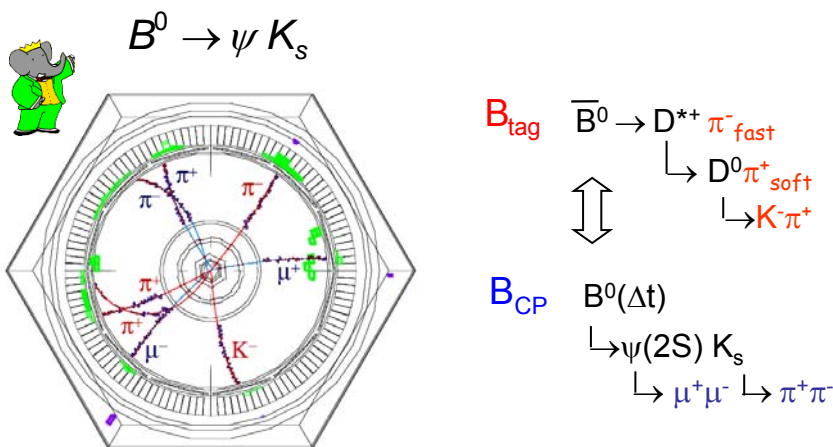
- Need many B (several 100×10^9)
- Need to know the flavor of the B at $t=0$
- Need to reconstruct the decay length to measure t

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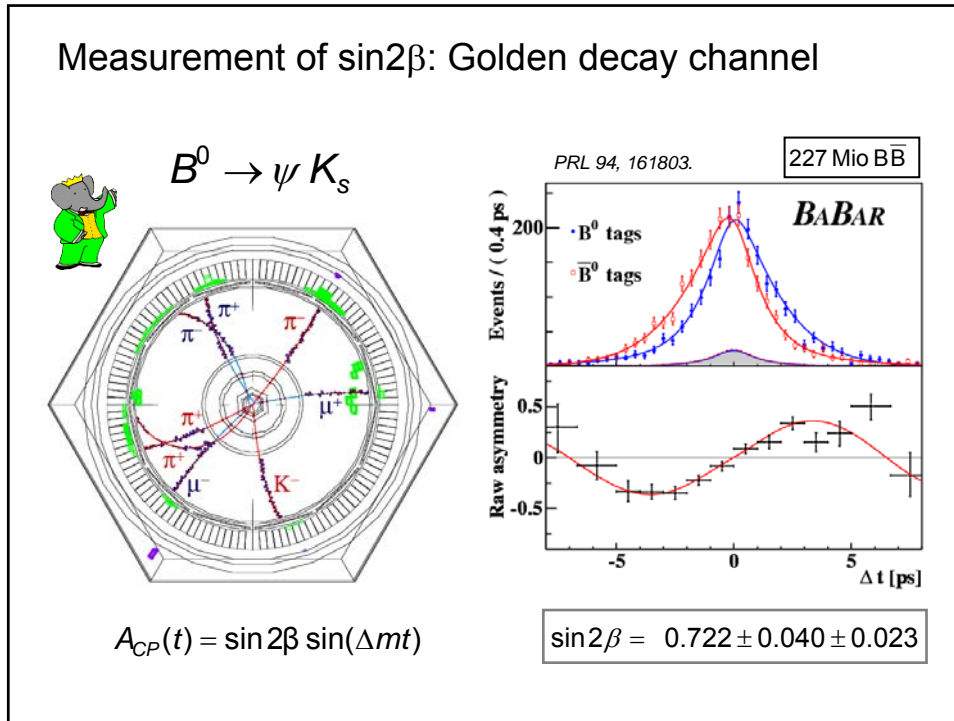
3.4 Measurement of $\sin 2\beta$: Asymmetric $e^+ e^- B$ factory



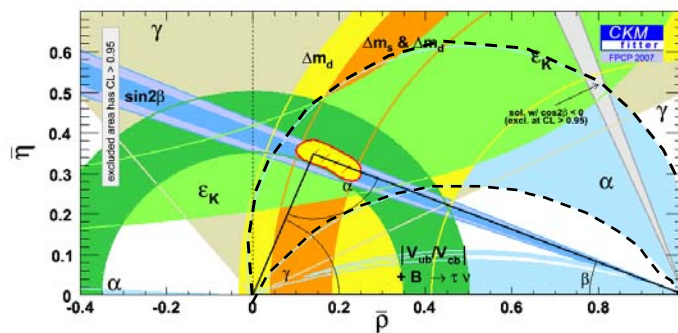
Measurement of $\sin 2\beta$: Golden decay channel



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3.5 Experimental status of the Unitarity Triangle



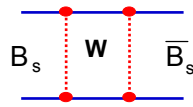
Standard Model CKM mechanism confirmed

1. Large CP Violation in B decays
2. Large direct CP violation observed
3. CPV parameter related to magnitude of non-CP observables

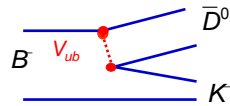
Standard Model: Flavor mixing and CP violation

4. Precision study of B mesons at LHC**b**

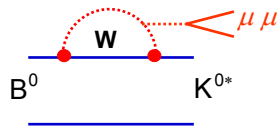
At LHC there are about 10^{12} BB pairs produced per year
 → study of very rare B decays (branching ratios $\sim 10^{-9}$) possible.



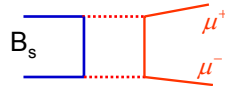
CP Violation in $B_s \rightarrow J/\psi \phi$
 ⇒ Mixing phase $\phi_s = -2\beta_s$



CP Violation in $B^+ \rightarrow DK^+$
 ⇒ CKM angle γ (tree)



FCNC penguin $B^0 \rightarrow K^* \mu \mu$
 ⇒ $\mu \mu$ angular distribution



FCNC $B_s \rightarrow \mu \mu$
 ⇒ branching ratio

New particles can appear as virtual particles in the loop corrections and can lead to additional quantum corrections which modify the observables.