

Lecture:

# Standard Model of Particle Physics

Heidelberg SS 2016

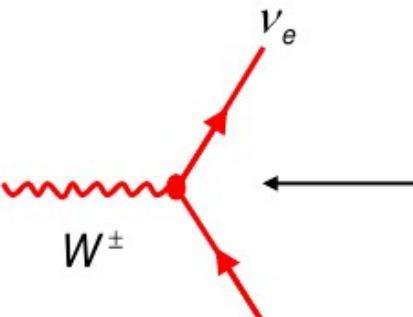
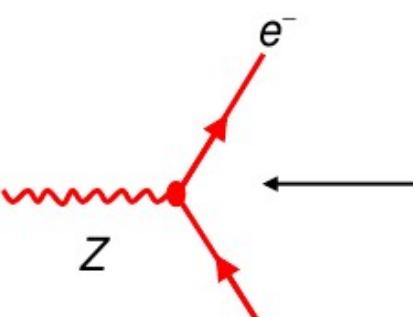
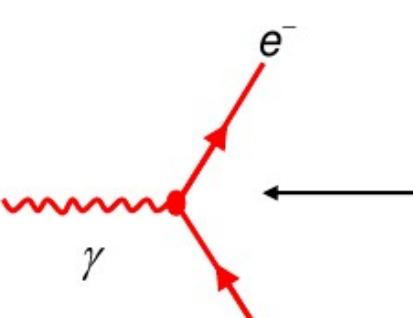
## Tests of the Standard Model at LEP

# Contents

- Introduction
- Z-Lineshape\*
- Fermion couplings and Forward-Backward Asymmetries
- Top-Mass Prediction and Discovery
- Triple Gauge Boson couplings

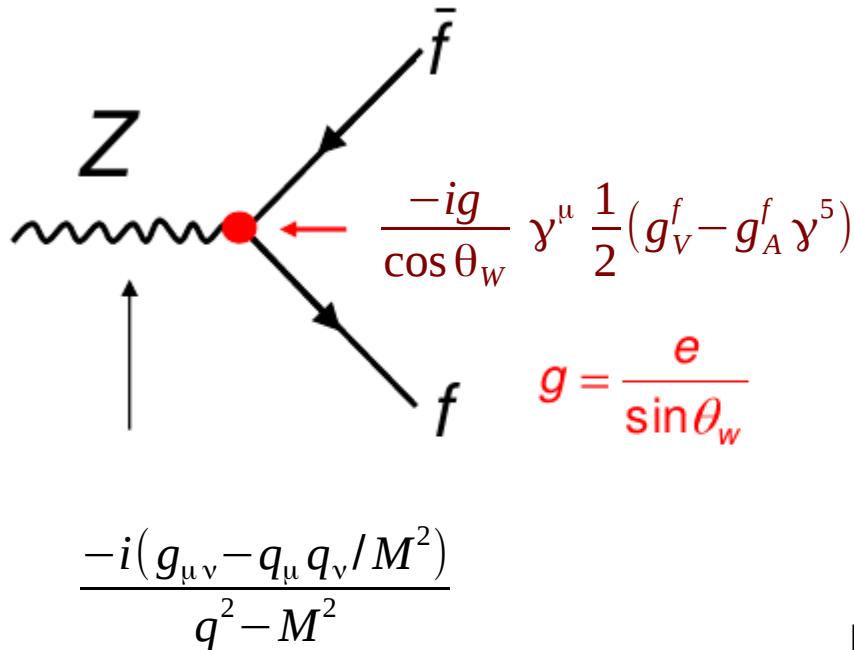
\* *Precision electroweak measurement on the Z resonance,  
Phys. Rept. 427 (2006), hep-ex/0509008.*  
<http://lepewwg.web.cern.ch/LEPEWWG/1/physrep.pdf>

# Feynman Rules Electroweak Theory

Vertex factors	Propagator (unitary gauge)
	$-i \frac{g}{\sqrt{2}} \gamma_\mu \frac{1}{2} (1 - \gamma^5)$
	$-i \frac{g}{\cos \theta_W} \gamma_\mu \frac{1}{2} (g_V - g_A \gamma^5)$
	$-ie\gamma_\mu$

slide from U.Uwer

# SM Precision Tests



$$\sin^2 \theta_w = 1 - \frac{M_w^2}{M_Z^2}$$

Standard Model

$$g_V = T_3 - 2Q \sin^2 \theta_w \quad \text{and} \quad g_A = T_3$$

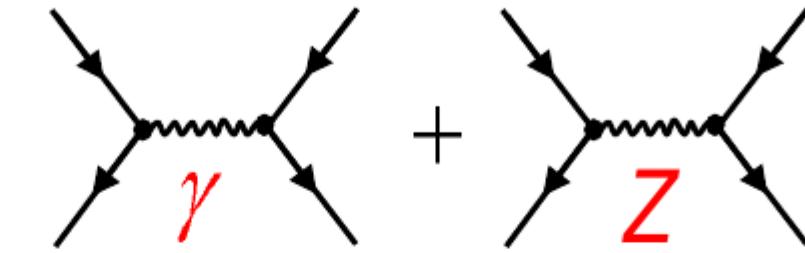
$$g_L = \frac{1}{2}(g_V + g_A) \quad g_R = \frac{1}{2}(g_V - g_A)$$

$$\frac{g_V}{g_A} = 1 - 2 \frac{Q}{T_3} \sin^2 \theta_w = 1 - 4|Q| \sin^2 \theta_w$$

	$g_V$	$g_A$
$\nu$	$\frac{1}{2}$	$\frac{1}{2}$
$\ell^-$	$-\frac{1}{2} + 2 \sin^2 \theta_w$	$-\frac{1}{2}$
$u$ -quark	$+\frac{1}{2} - \frac{4}{3} \sin^2 \theta_w$	$\frac{1}{2}$
$d$ -quark	$-\frac{1}{2} + \frac{2}{3} \sin^2 \theta_w$	$-\frac{1}{2}$

slide from U.Uwer

# LEP1 + SLC Cross Section

$$|A|^2 = \left| \begin{array}{c} \text{Diagram with } \gamma \\ \text{Diagram with } Z \end{array} \right|^2$$


for  $e^+ e^- \rightarrow \mu^+ \mu^-$

Matrix elements:

$$A_\gamma = -ie^2 (\bar{u}_\mu \gamma^\nu v_\mu) \frac{g_{\rho\nu}}{q^2} (\bar{v}_e \gamma^\rho u_e)$$

$$A_Z = -i \frac{g^2}{\cos^2 \theta_W} \left[ \bar{u}_\mu \gamma^\nu \frac{1}{2} (g_V^\mu - g_A^\mu \gamma^5) v_\mu \right] \underbrace{\frac{g_{\rho\nu} - q_\rho q_\nu / M_Z^2}{(q^2 - M_Z^2) + iM_Z \Gamma_Z}}_{\text{Z propagator considering a finite Z width (real particle)}} \left[ \bar{v}_e \gamma^\rho \frac{1}{2} (g_V^e - g_A^e \gamma^5) u_e \right]$$

Z propagator considering a finite Z width (real particle)

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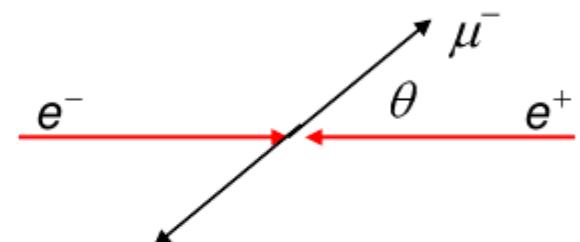
# LEP1 + SLC Cross Section

One finds for the differential cross section:

$$\frac{d\sigma}{d\cos\theta} = \frac{\pi\alpha^2}{2s} \left[ F_\gamma(\cos\theta) + F_{\gamma Z}(\cos\theta) \frac{s(s - M_Z^2)}{(s - M_Z^2)^2 + M_Z^2\Gamma_Z^2} + F_Z(\cos\theta) \frac{s^2}{(s - M_Z^2)^2 + M_Z^2\Gamma_Z^2} \right]$$

known       $\gamma$ 
 $\gamma/Z$  interference
Z

} Vanishes at  $\sqrt{s} \approx M_Z$



$$F_\gamma(\cos\theta) = Q_e^2 Q_\mu^2 (1 + \cos^2\theta) = (1 + \cos^2\theta)$$

$$F_{\gamma Z}(\cos\theta) = \frac{Q_e Q_\mu}{4 \sin^2 \theta_W \cos^2 \theta_W} [2 g_V^e g_V^\mu (1 + \cos^2\theta) + 4 g_A^e g_A^\mu \cos\theta]$$

$$F_Z(\cos\theta) = \frac{1}{16 \sin^4 \theta_W \cos^4 \theta_W} [(g_V^e)^2 + (g_A^e)^2] [(g_V^\mu)^2 + (g_A^\mu)^2] (1 + \cos^2\theta) + 8 g_V^e g_A^e g_V^\mu g_A^\mu \cos\theta]$$

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# Total Cross Section

$$\sigma_Z = \frac{4\pi\alpha^2}{3s} \frac{1}{16 \sin^4 \theta_W \cos^4 \theta_W} [(g_V^e)^2 + (g_A^e)^2] [(g_V^u)^2 + (g_A^u)^2] \frac{s^2}{(s - M_Z^2)^2 + (M_Z \Gamma_Z)^2}$$



Breit-Wigner Resonance:  
BW description is very general

$$\sigma_Z(\sqrt{s}=M_Z) = \frac{12\pi}{M_Z^2} \frac{\Gamma_e \Gamma_\mu}{\Gamma_Z^2}$$



$$\sigma(s) = 12\pi \frac{\Gamma_e \Gamma_\mu}{M_Z^2} \cdot \frac{s}{(s - M_Z^2)^2 + M_Z^2 \Gamma_Z^2}$$

With partial and total widths:

$$\Gamma_f = \frac{\alpha M_Z}{12 \sin^2 \theta_W \cos^2 \theta_W} (g_V^f)^2 + (g_A^f)^2$$

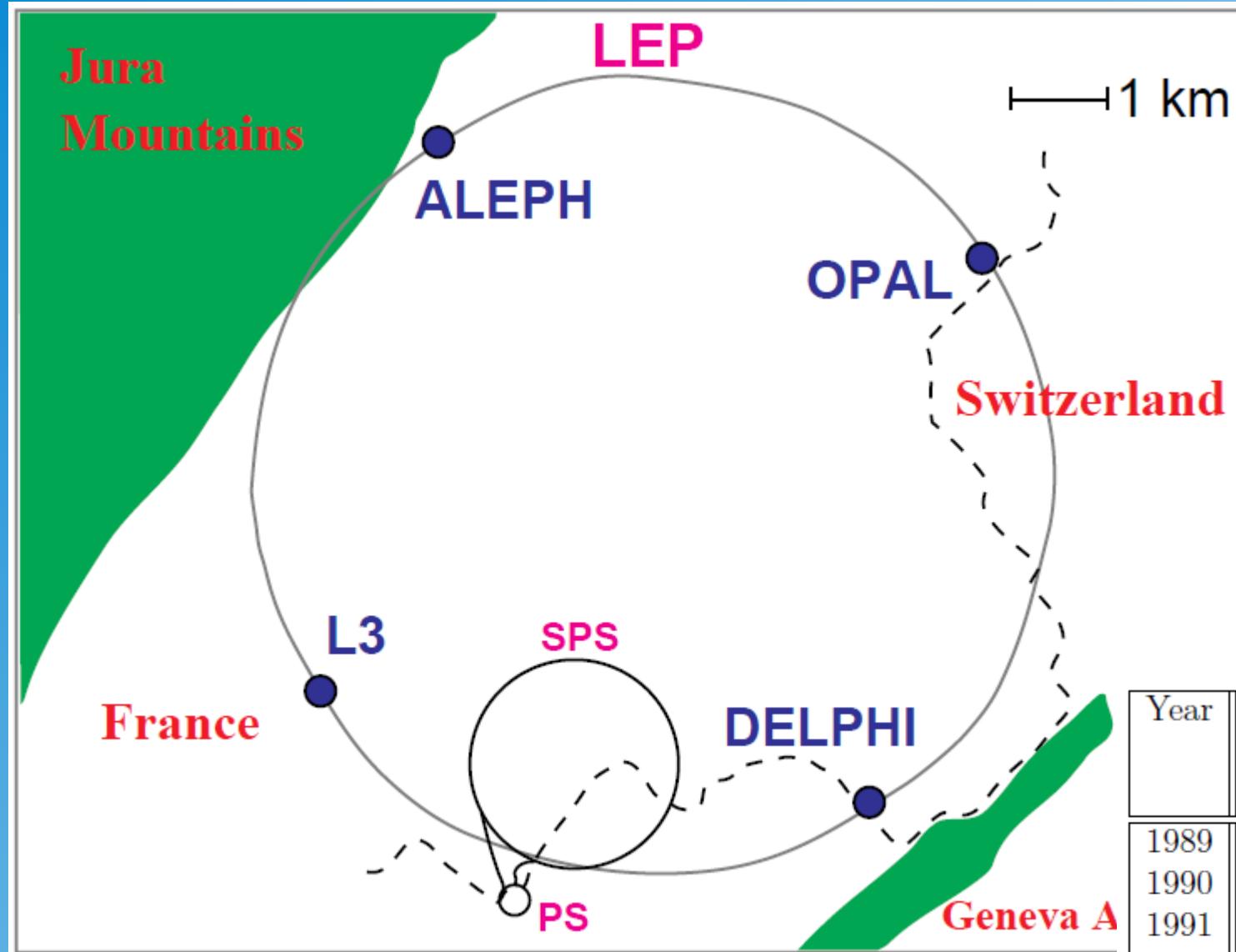
$$\Gamma_Z = \sum_i \Gamma_i \quad BR(Z \rightarrow ii) = \frac{\Gamma_i}{\Gamma_Z}$$



Cross sections and widths  
can be calculated within the  
Standard Model if all  
parameters are known

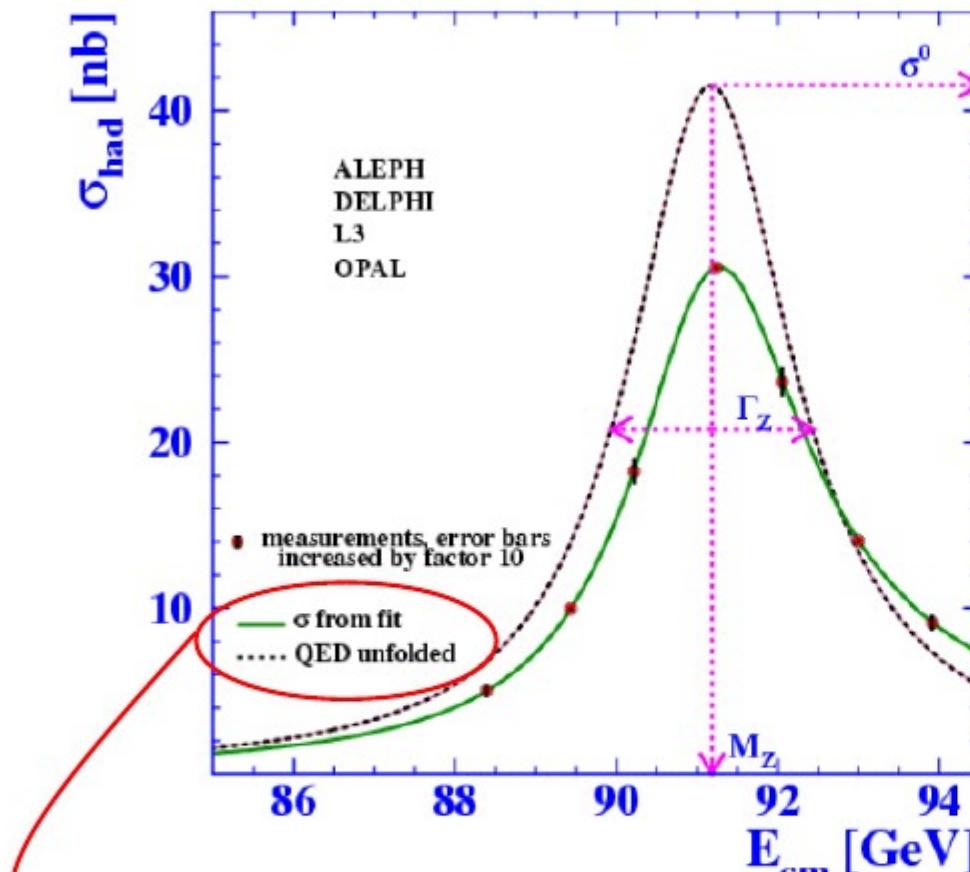
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# Large Electron Positron Collider



Year	Centre-of-mass energy range [GeV]	Integrated luminosity [ $\text{pb}^{-1}$ ]
1989	88.2 – 94.2	1.7
1990	88.2 – 94.2	8.6
1991	88.5 – 93.7	18.9
1992	91.3	28.6
1993	89.4, 91.2, 93.0	40.0
1994	91.2	64.5
1995	89.4, 91.3, 93.0	39.8

# Measurement of the Z-lineshape



Z Resonance curve:

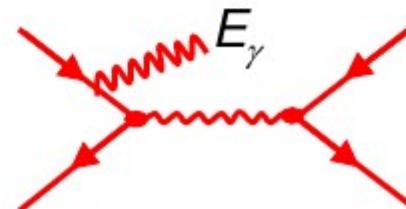
$$\sigma(s) = 12\pi \frac{\Gamma_e \Gamma_\mu}{M_Z^2} \cdot \frac{s}{(s - M_Z^2)^2 + M_Z^2 \Gamma_Z^2}$$

Peak:  $\sigma_0 = \frac{12\pi}{M_Z^2} \frac{\Gamma_e \Gamma_\mu}{\Gamma_Z^2}$

- Resonance position  $\rightarrow M_Z$
- Height  $\rightarrow \Gamma_e \Gamma_\mu$
- Width  $\rightarrow \Gamma_Z$

Initial state Bremsstrahlung corrections

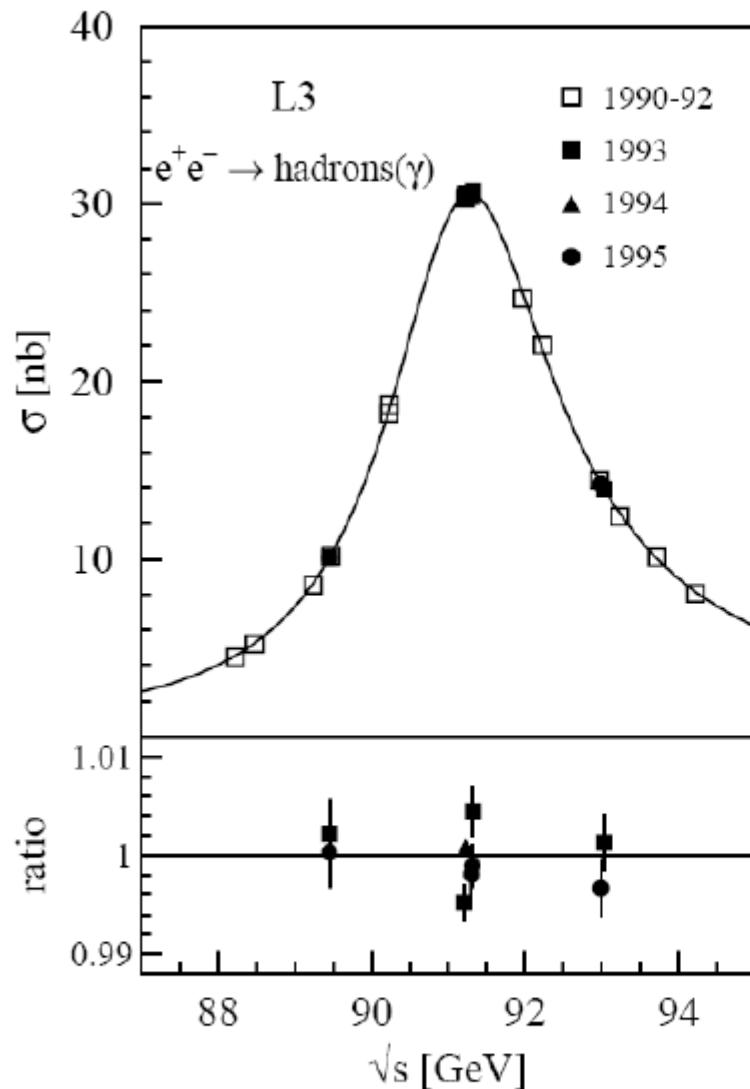
$$\sigma_{ff(\gamma)} = \int_{4m_f^2/s}^1 G(z) \sigma_{ff}^0(zs) dz \quad z = 1 - \frac{2E_\gamma}{\sqrt{s}}$$



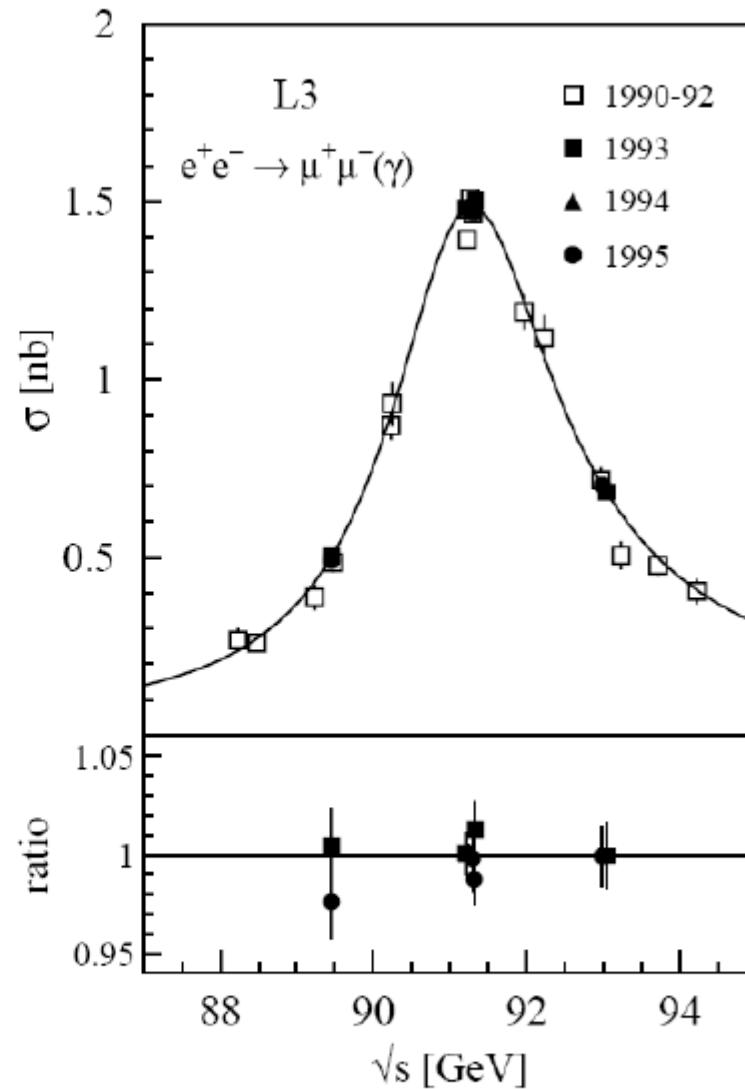
Leads to a deformation of the resonance: large (30%) effect !

# Final State Comparisons

$e^+ e^- \rightarrow \text{hadrons}$

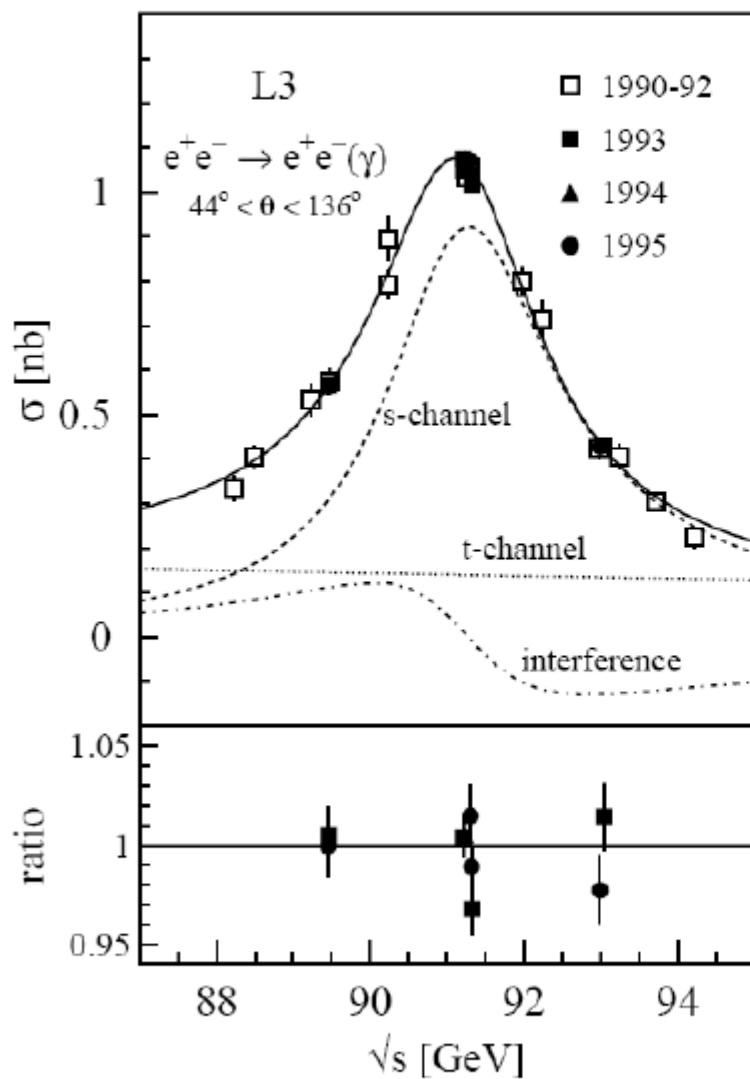


$e^+ e^- \rightarrow \mu^+ \mu^-$



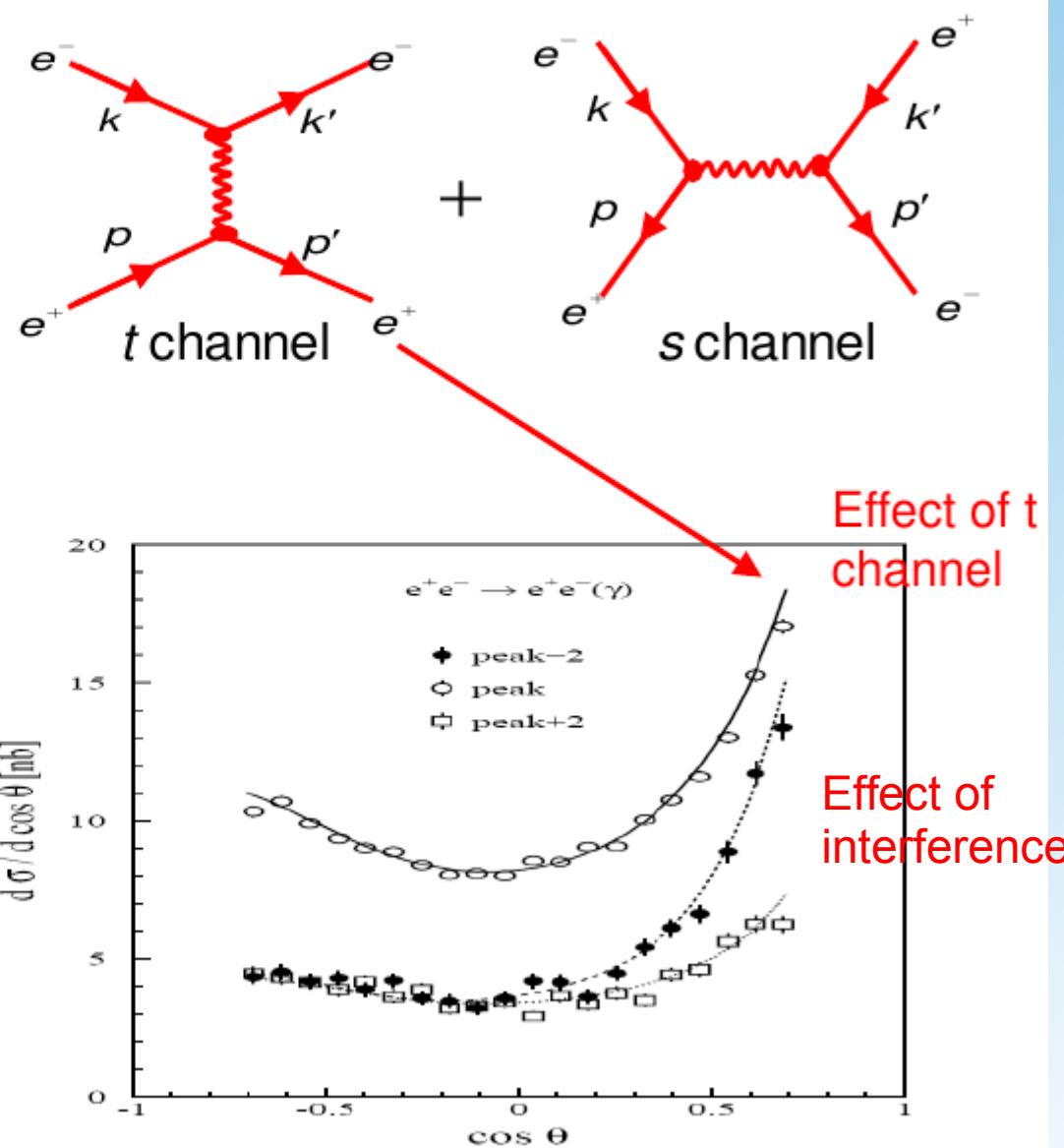
Same resonance shape!

$e^+ e^- \rightarrow e^+ e^-$



s-channel contribution  $\sim (\Gamma_e)^2$

t channel contribution  $\rightarrow$  forward peak



# Z Lineshape Parameters LEP (Average)

$$M_Z = 91.1876 \pm 0.0021 \text{ GeV} \quad \pm 23 \text{ ppm (*)}$$

$$\Gamma_Z = 2.4952 \pm 0.0023 \text{ GeV}$$

$$\Gamma_{\text{had}} = 1.7458 \pm 0.0027 \text{ GeV}$$

$$\Gamma_e = 0.08392 \pm 0.00012 \text{ GeV}$$

$$\Gamma_\mu = 0.08399 \pm 0.00018 \text{ GeV}$$

$$\Gamma_\tau = 0.08408 \pm 0.00022 \text{ GeV}$$

$\pm 0.09 \%$

3 leptons are treated independently

test of lepton universality

$$\Gamma_Z = 2.4952 \pm 0.0023 \text{ GeV}$$

$$\Gamma_{\text{had}} = 1.7444 \pm 0.0022 \text{ GeV}$$

$$\Gamma_e = 0.083985 \pm 0.000086 \text{ GeV}$$

Assuming lepton universality:  $\Gamma_e = \Gamma_\mu = \Gamma_\tau$   
*(predicted by SM:  $g_A$  and  $g_V$  are the same)*

\*) error of the LEP energy determination:  $\pm 1.7 \text{ MeV (19 ppm)}$

<http://lepewwg.web.cern.ch/> (Summer 2005)

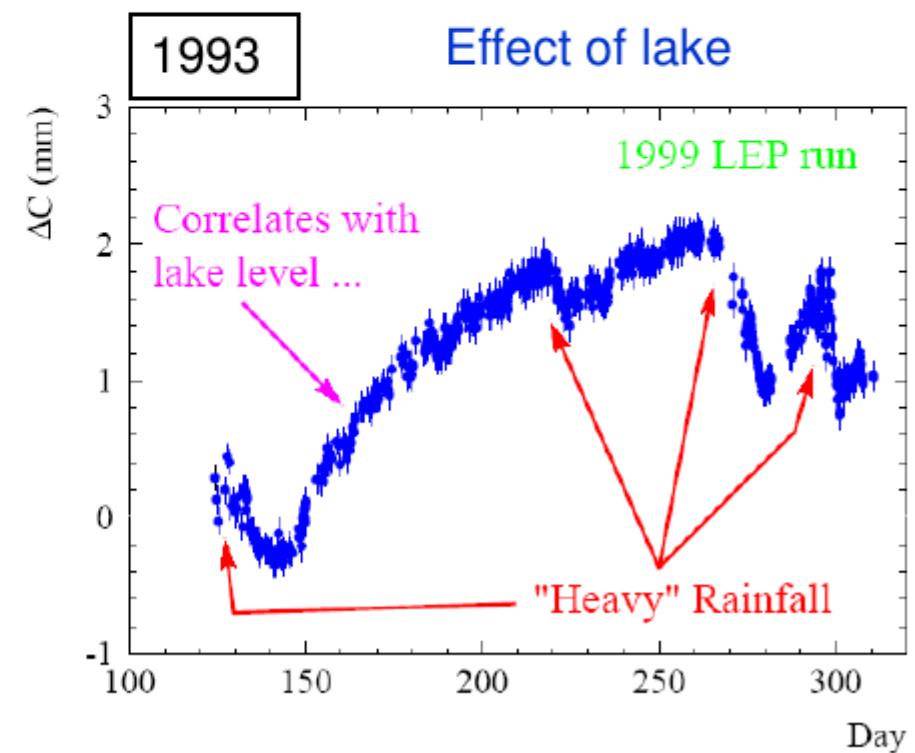
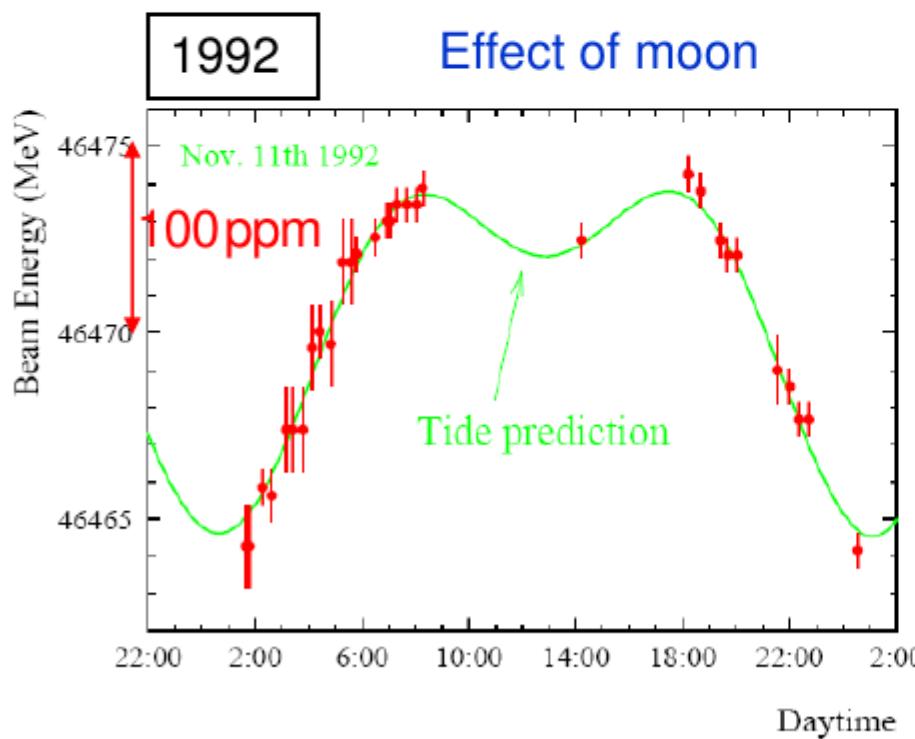
# LEP Energy Calibration

Changes of the circumference of the LEP ring changes the energy of the electrons and thus the CM energy (shifts  $M_Z$ ) :

- tide effects
- water level in lake Geneva

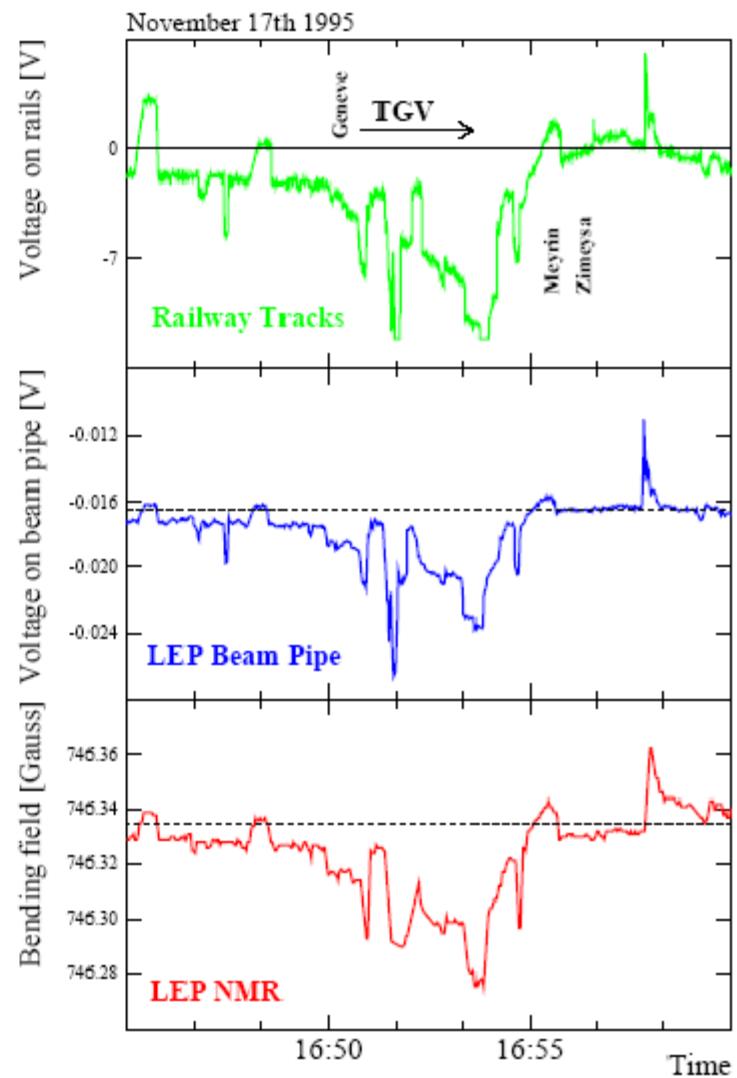
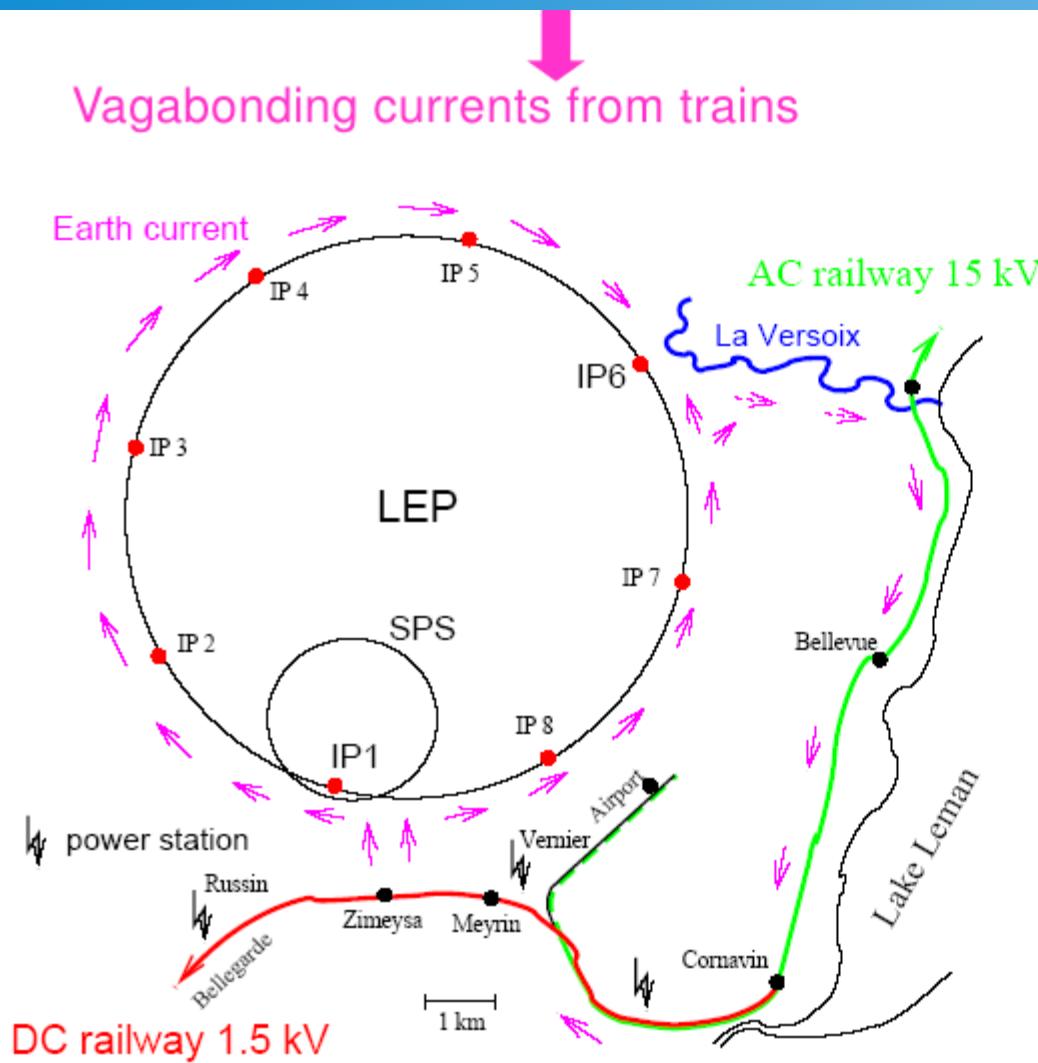


Changes of LEP circumference  
 $\Delta C = 1 \dots 2 \text{ mm}/27\text{km} (4 \dots 8 \times 10^{-8})$



The total strain is  $4 \times 10^{-8}$  ( $\Delta C = 1 \text{ mm}$ )

# TGV (Trains Grand Vitesse) Effect



In conclusion:

Measurements at the ppm level are difficult to perform. Many effects must be considered!

# Number Light Neutrino Generations

In the Standard Model:

$$\Gamma_Z = \Gamma_{had} + 3 \cdot \underbrace{\Gamma_\ell}_{\text{invisible}} + \underbrace{N_\nu \cdot \Gamma_\nu}_{\text{invisible}} \rightarrow \left\{ \begin{array}{l} e^+ e^- \rightarrow Z \rightarrow \nu_e \bar{\nu}_e \\ e^+ e^- \rightarrow Z \rightarrow \nu_\mu \bar{\nu}_\mu \\ e^+ e^- \rightarrow Z \rightarrow \nu_\tau \bar{\nu}_\tau \end{array} \right.$$

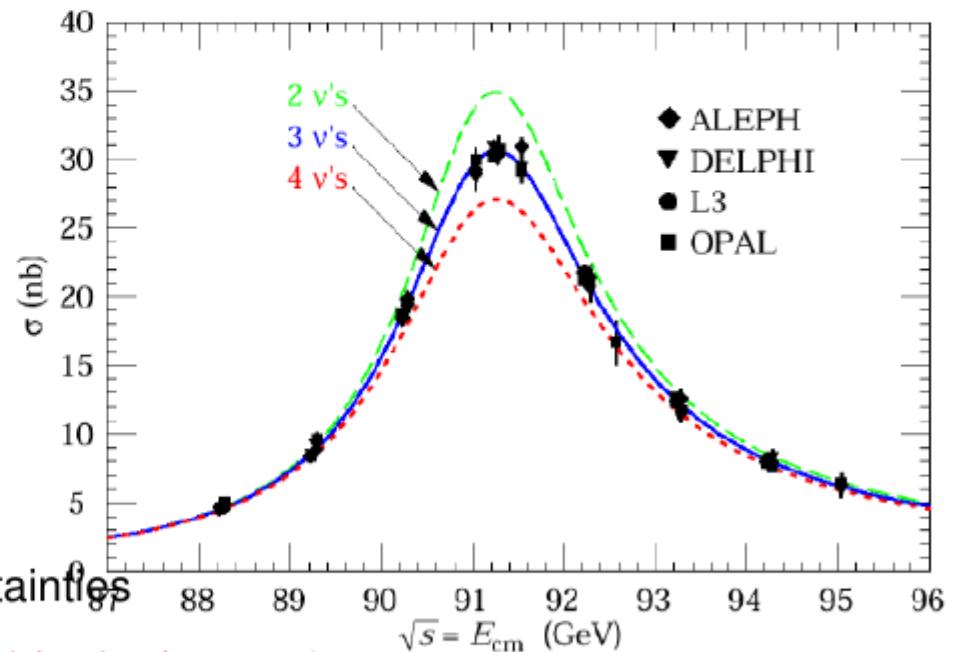
$$\Gamma_{inv} = 0.4990 \pm 0.0015 \text{ GeV}$$

To determine the number of light neutrino generations:

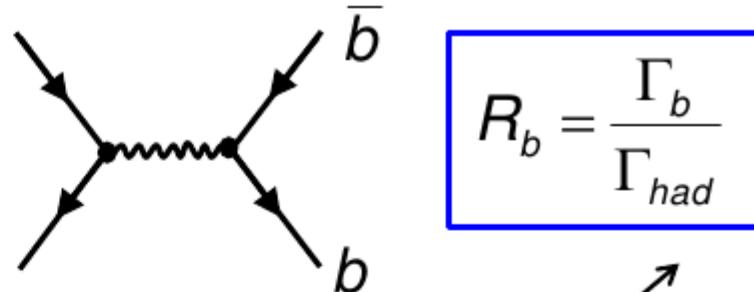
$$N_\nu = \frac{\Gamma_{inv}}{\Gamma_{\nu,SM}} = \underbrace{\left( \frac{\Gamma_{inv}}{\Gamma_\ell} \right)}_{5.9431 \pm 0.0163} \exp \underbrace{\left( \frac{\Gamma_\ell}{\Gamma_\nu} \right)_{SM}}_{=1/1.991 \pm 0.001} \quad (\text{small theo. uncertainties from } m_{top}, M_H)$$

$$N_\nu = 2.9840 \pm 0.0082$$

No room for new physics:  $Z \rightarrow \text{new}$



# Heavy Quark production

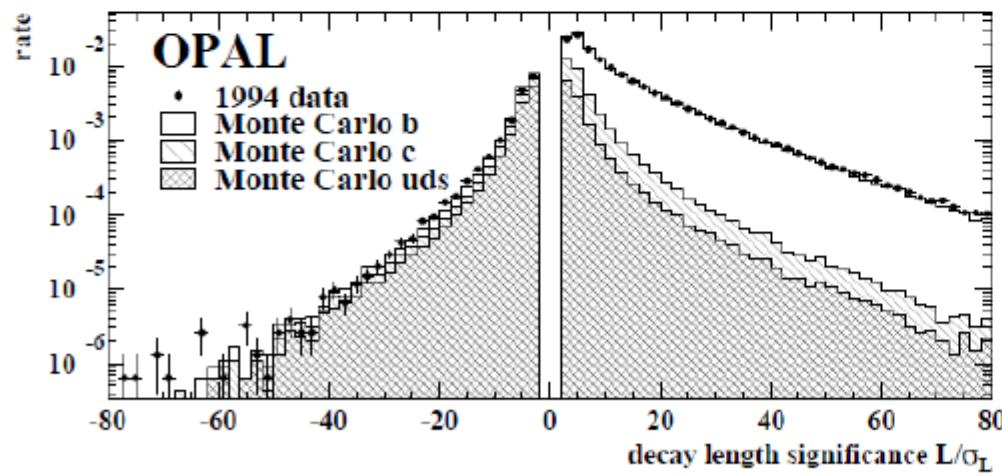
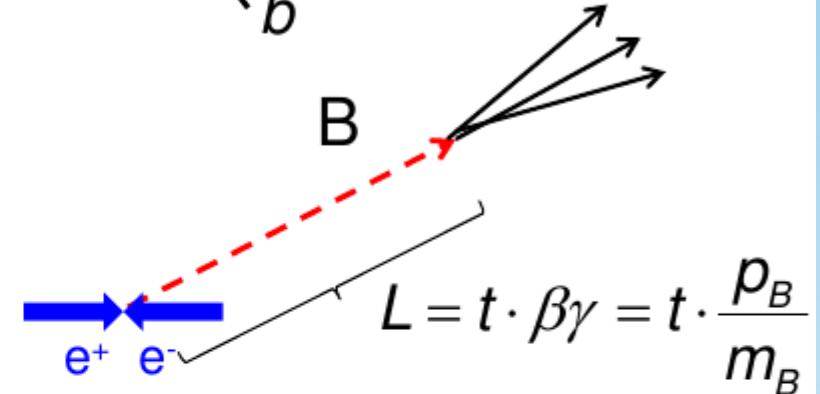


$$R_b = \frac{\Gamma_b}{\Gamma_{had}}$$

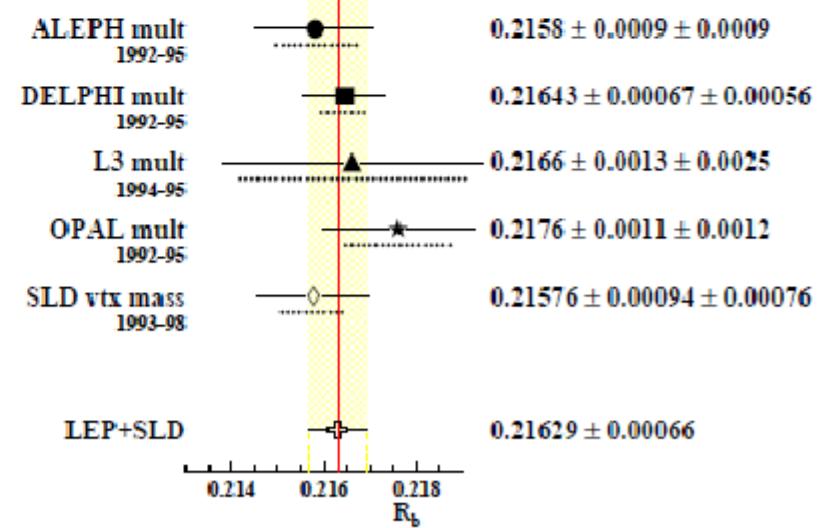
Identification of b-Quark events:

b-quarks hadronize to b-hadrons (B's,  $\Lambda_b$ ) with typical lifetime of  $\sim 1$  ps  $\rightarrow$  decay length

Use displaced “2<sup>nd</sup>” B decay vertex as signature.

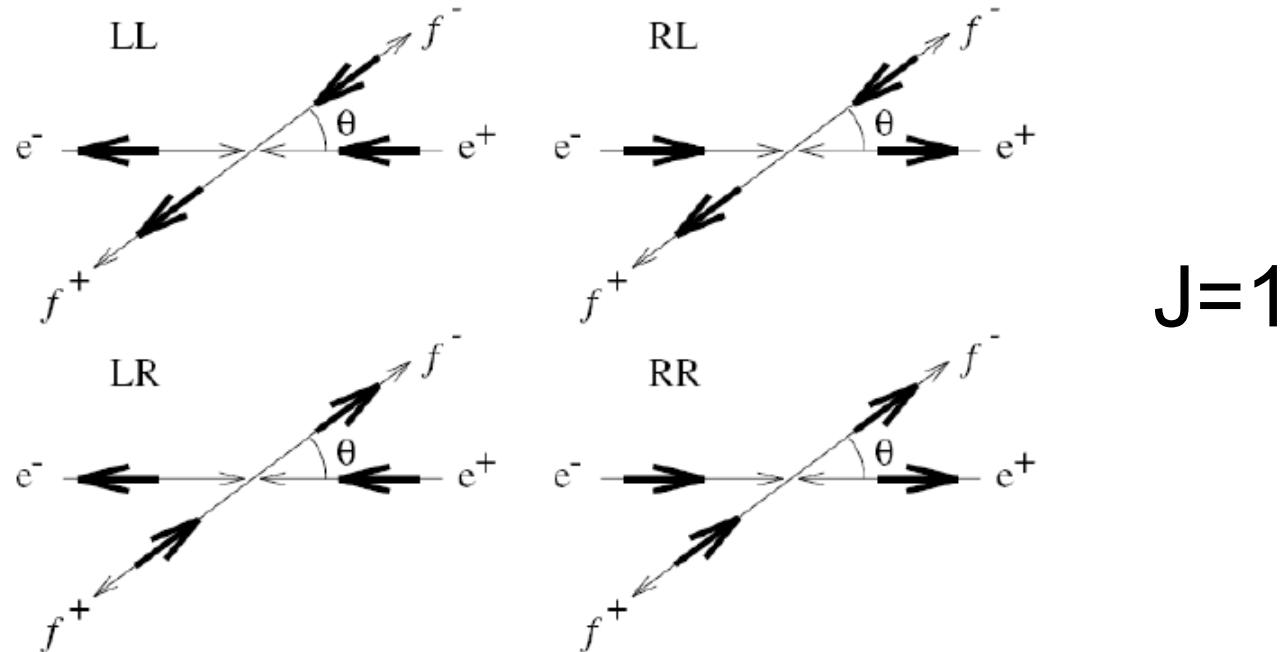


Significance =  $L / \text{error}$



$Z \rightarrow b\bar{b}$  decay ratio

# Helicity Amplitudes and Asymmetries



Observables:

$$\sigma_F = \sigma_{LL} + \sigma_{RR}$$

$$\sigma_B = \sigma_{RL} + \sigma_{LR}$$

$$A_{FB} = \frac{\sigma_F - \sigma_B}{\sigma_F + \sigma_B}$$

Forward-backward asym. (final)

$$\sigma_L = \sigma_{LL} + \sigma_{LR}$$

$$\sigma_R = \sigma_{RL} + \sigma_{RR}$$

$$A_{LR} = \frac{\sigma_L - \sigma_R}{\sigma_L + \sigma_R}$$

Left right asym. (initial)

$$\sigma_- = \sigma_{LL} + \sigma_{RL}$$

$$\sigma_+ = \sigma_{RR} + \sigma_{LR}$$

$$\mathcal{P}_f = \frac{\sigma_+ - \sigma_-}{\sigma_+ + \sigma_-}$$

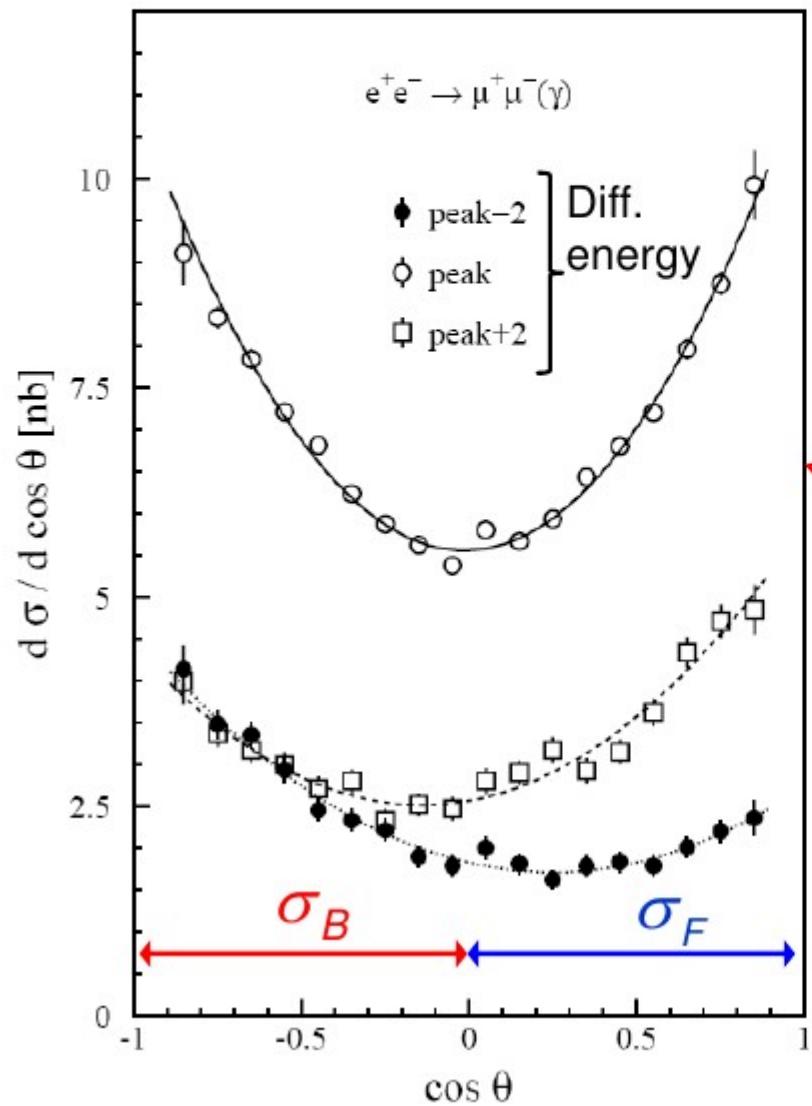
fermion polarization (final)

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# Forward-Backward Asymmetry

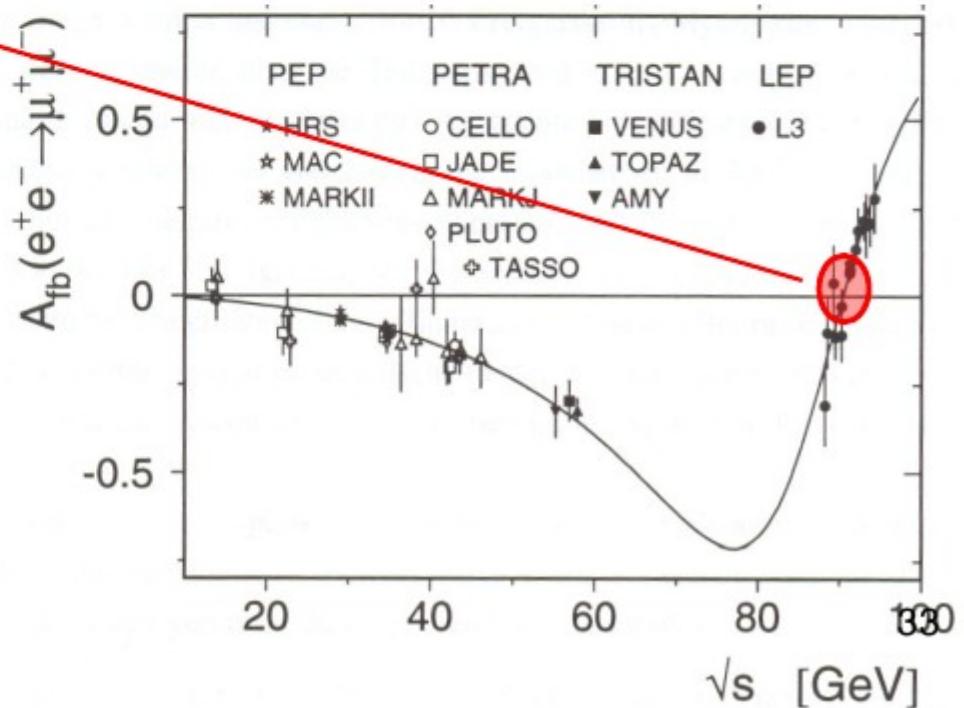
$$e^+ e^- \rightarrow Z \rightarrow \mu^+ \mu^-$$

$$\frac{d\sigma}{d\cos\theta} \sim (1 + \cos^2\theta) + \frac{8}{3} A_{FB} \cos\theta$$



$$\text{with } A_{FB} = \frac{\sigma_F - \sigma_B}{\sigma_F + \sigma_B}$$

$$\sigma_{F(B)} = \int_{0(-1)}^{1(0)} \frac{d\sigma}{d\cos\theta} d\cos\theta$$



# Forward-Backward Asymmetry

Angular distribution: (see above)

$$F_{\gamma Z}(\cos \theta) = \frac{Q_e Q_\mu}{4 \sin^2 \theta_W \cos^2 \theta_W} [2g_V^e g_V^\mu (1 + \cos^2 \theta) + 4g_A^e g_A^\mu \cos \theta]$$

$$F_Z(\cos \theta) = \frac{1}{16 \sin^4 \theta_W \cos^4 \theta_W} [(g_V^{e^2} + g_A^{e^2})(g_V^{\mu^2} + g_A^{\mu^2}) (1 + \cos^2 \theta) + 8g_V^e g_A^e g_V^\mu g_A^\mu \cos \theta]$$

Forward-backward asymmetry  $A_{FB}$

- Away from the resonance large  $\rightarrow$  interference term dominates

$$A_{FB} \sim g_A^e g_A^f \cdot \frac{s(s - M_Z^2)}{(s - M_Z^2)^2 + M_Z^2 \Gamma_Z^2} \quad \rightarrow \text{large}$$

- At the Z pole: Interference = 0 (see energy dependence of interference term)

$$A_{FB} = 3 \cdot \frac{g_V^e g_A^e}{(g_V^e)^2 + (g_A^e)^2} \cdot \frac{g_V^\mu g_A^\mu}{(g_V^\mu)^2 + (g_A^\mu)^2} = \frac{3}{4} A_e A_\mu$$

$\rightarrow$  very small because  $g_V^l$  small in SM

# Forward-Backward Asymmetry

Asymmetrie at the Z pole

$$A_{FB} \sim g_A^e g_V^e g_A^f g_V^f$$

Cross section at the Z pole

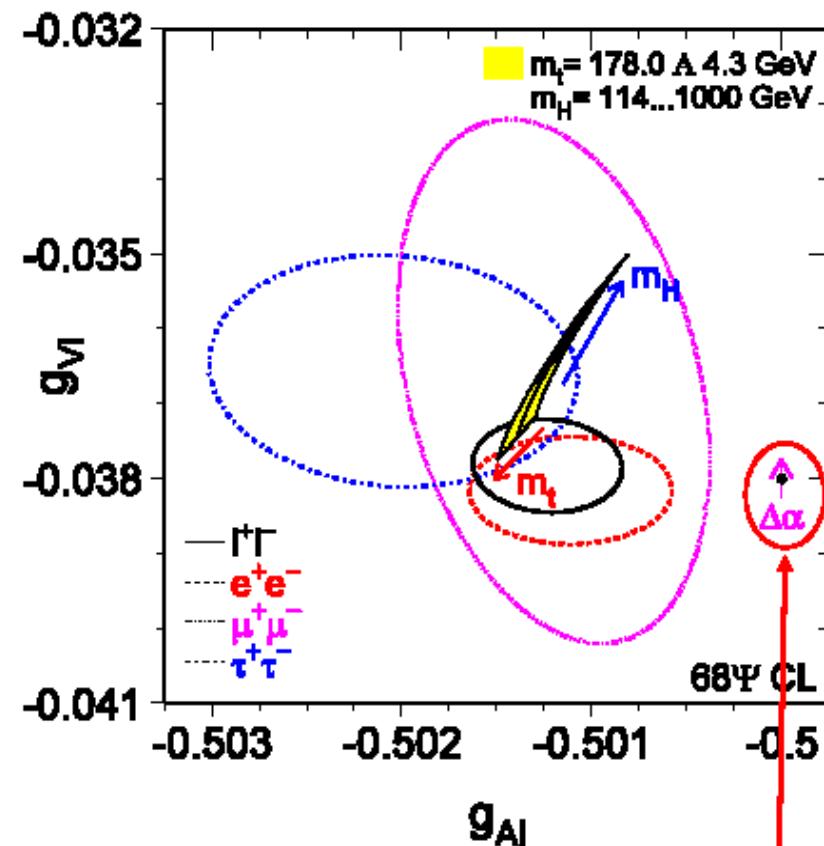
$$\sigma_Z \sim [(g_V^e)^2 + (g_A^e)^2][(g_V^{\mu})^2 + (g_A^{\mu})^2]$$



Lepton asymmetries together with lepton pair cross sections allow the determination of the lepton couplings  $g_A$  and  $g_V$ .



Good agreement between the 3 lepton species confirms “lepton universality”



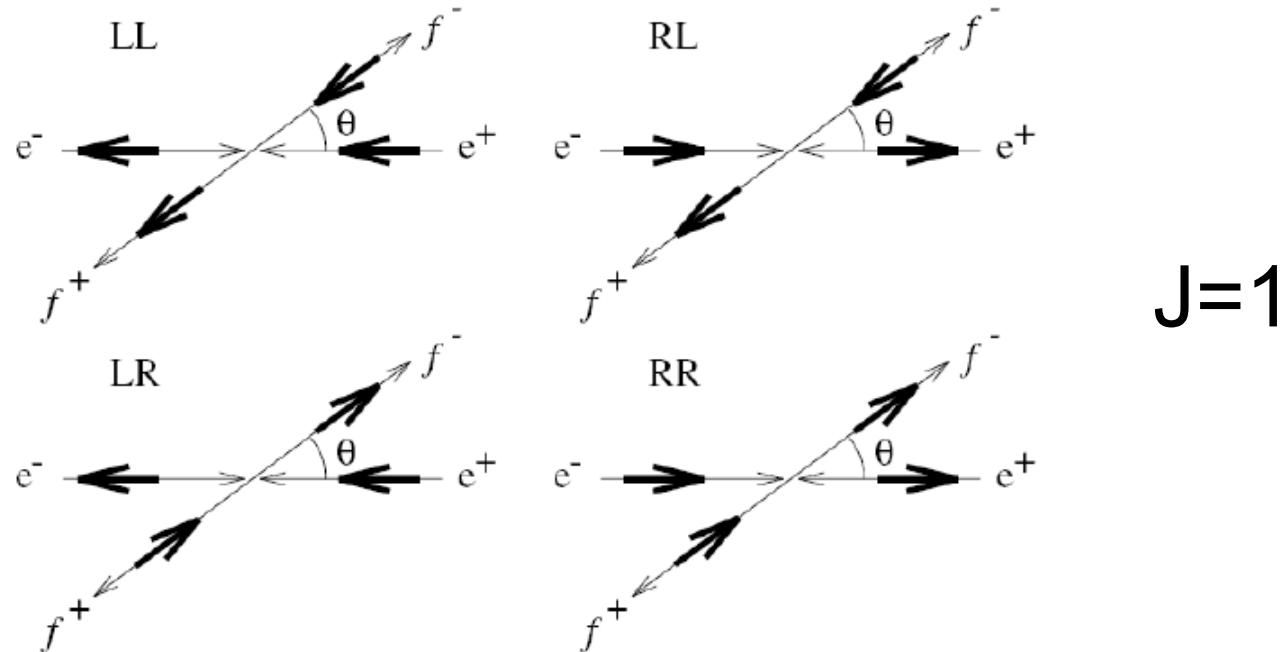
Lowest order SM prediction:

$$g_V = T_3 - 2q \sin^2 \theta_W \quad g_A = T_3$$

Deviation from lowest order SM prediction is an effect of higher-order electroweak corrections.

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# Helicity Amplitudes and Asymmetries



Observables:

$$\sigma_F = \sigma_{LL} + \sigma_{RR}$$

$$\sigma_B = \sigma_{RL} + \sigma_{LR}$$

$$A_{FB} = \frac{\sigma_F - \sigma_B}{\sigma_F + \sigma_B}$$

Forward-backward asym. (final)

$$\sigma_L = \sigma_{LL} + \sigma_{LR}$$

$$\sigma_R = \sigma_{RL} + \sigma_{RR}$$

$$A_{LR} = \frac{\sigma_L - \sigma_R}{\sigma_L + \sigma_R}$$

Left right asym. (initial)

$$\sigma_- = \sigma_{LL} + \sigma_{RL}$$

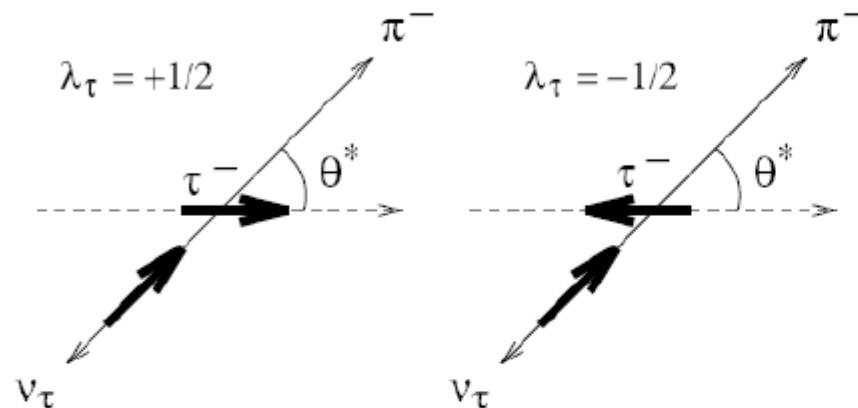
$$\sigma_+ = \sigma_{RR} + \sigma_{LR}$$

$$\mathcal{P}_f = \frac{\sigma_+ - \sigma_-}{\sigma_+ + \sigma_-}$$

fermion polarization (final)

## Experimental Method to measure tau polarization:

$$\tau^- \rightarrow \pi^- \nu_\tau \quad \text{Spin } 1/2 \rightarrow \text{Spin } 0 + \text{Spin } 1/2$$



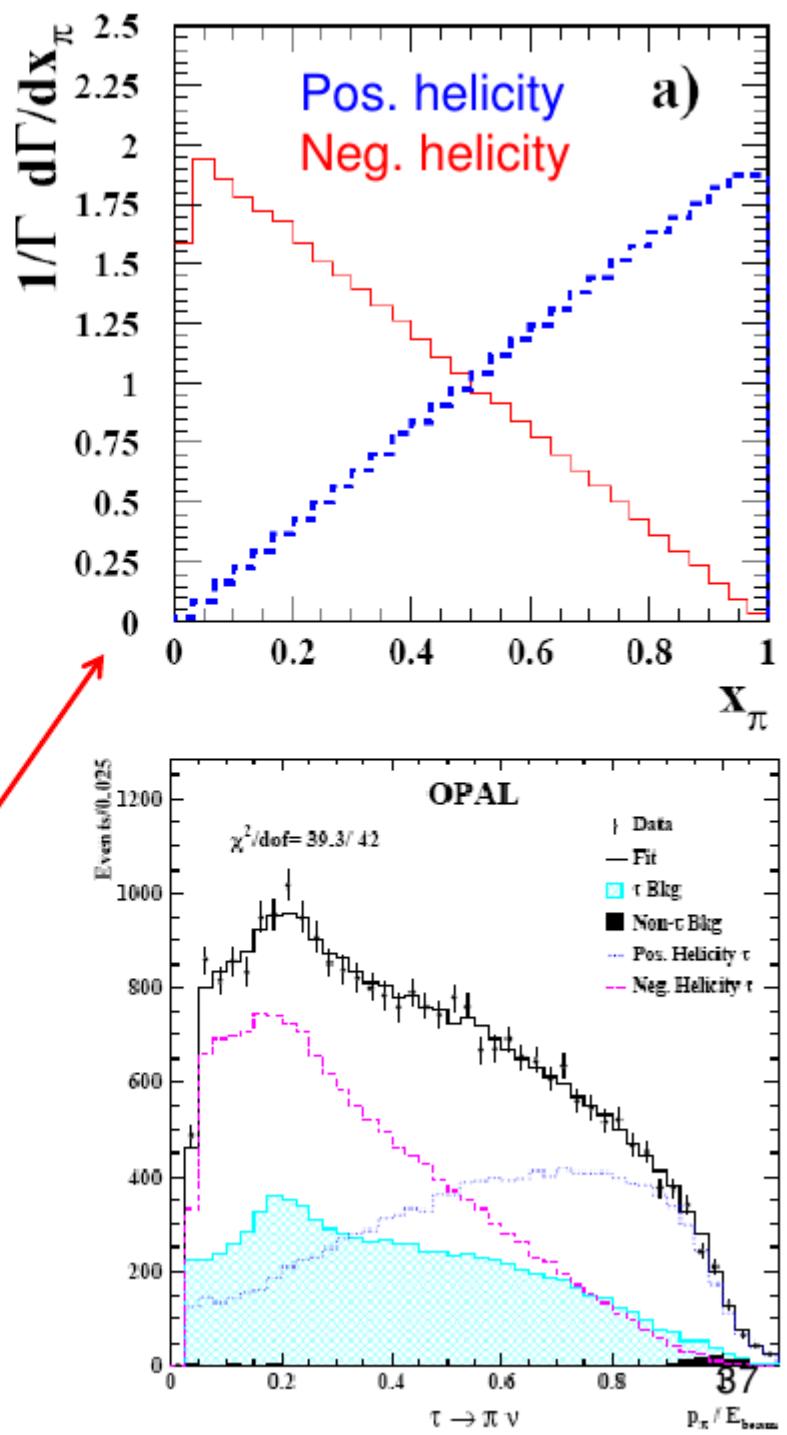
$$\frac{1}{\Gamma} \frac{d\Gamma}{d\cos\theta^*} = \frac{1}{2} (1 + \mathcal{P}_\tau \cos\theta^*)$$



Boost into lab frame

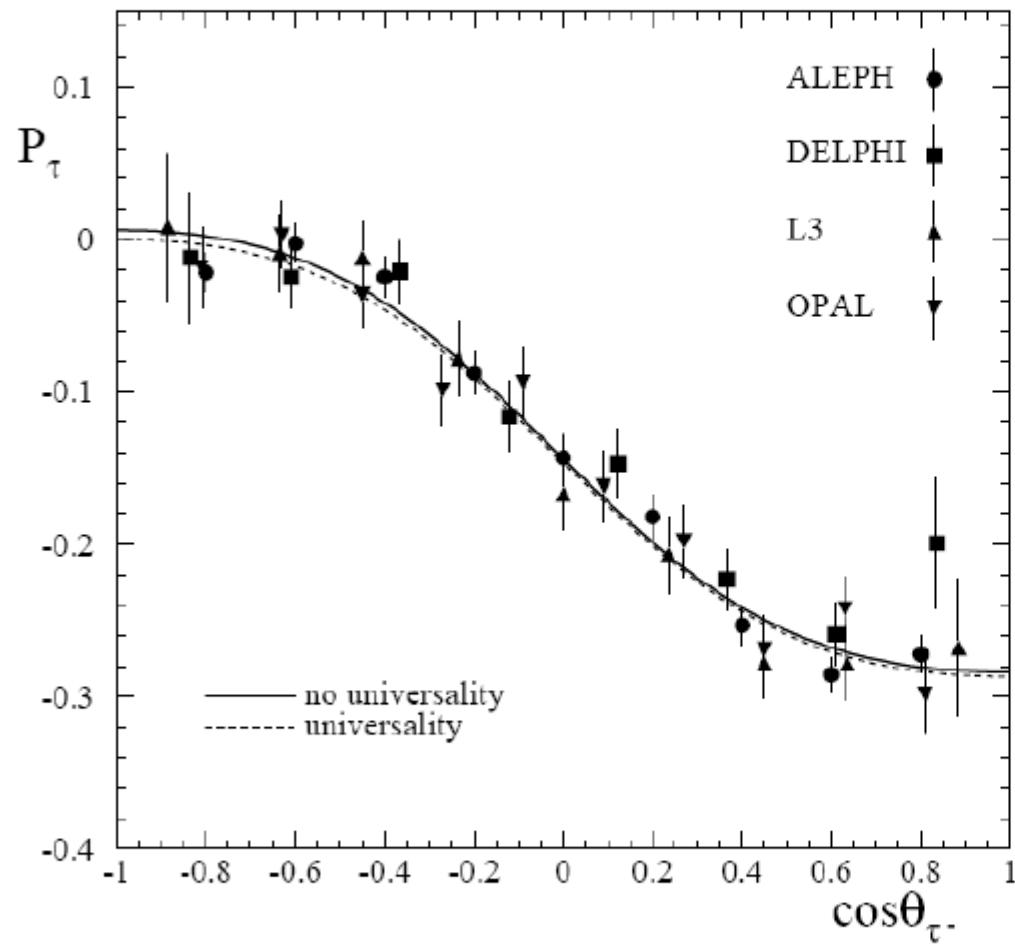
$$\frac{1}{\Gamma} \frac{d\Gamma}{dx_\pi} = 1 + \mathcal{P}_\tau (2x_\pi - 1) \quad x_\pi = E_\pi / E_\tau$$

Fit of the two theoretical distribution to data yields the polarization:  $\sim 0.15$



# Result Tau Polarisation

Measured  $P_\tau$  vs  $\cos\theta_{\tau^-}$ .



$$\mathcal{P}_f(\cos\theta) = -\frac{\mathcal{A}_f(1 + \cos^2\theta) + 2\mathcal{A}_e \cos\theta}{(1 + \cos^2\theta) + 2\mathcal{A}_f\mathcal{A}_e \cos\theta}$$

$$\mathcal{A}_\tau = 0.1439 \pm 0.0043$$

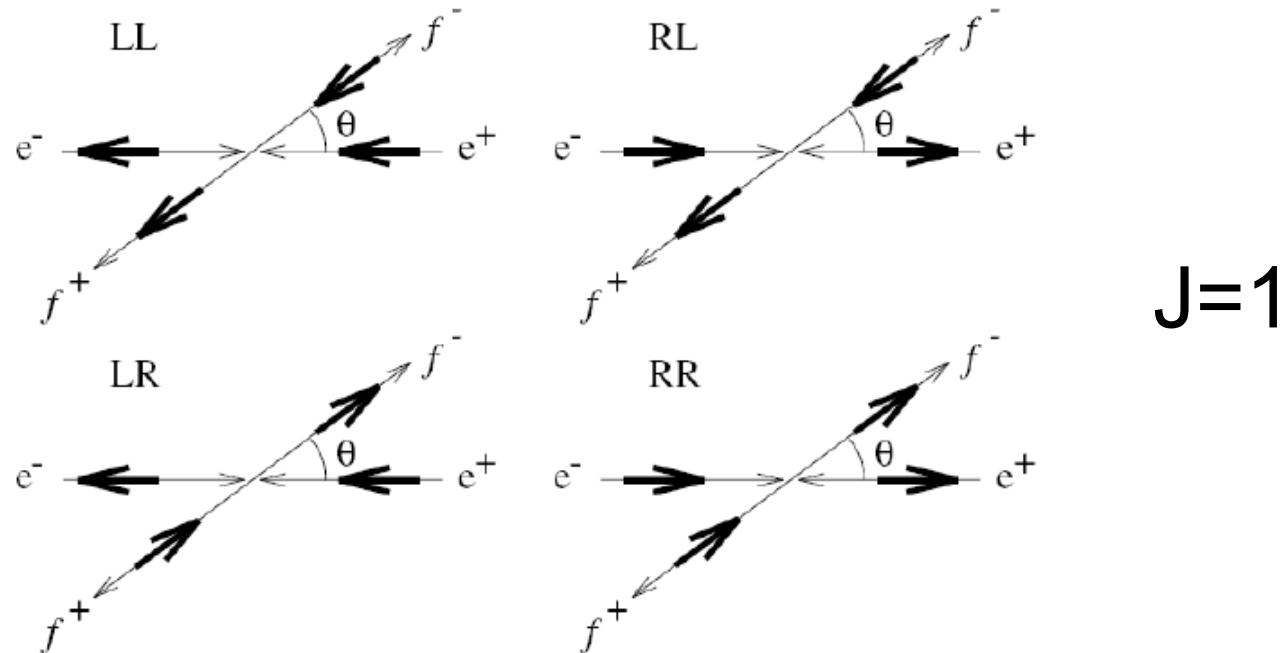
$$\mathcal{A}_e = 0.1498 \pm 0.0049$$

$$\mathcal{A}_\ell = 0.1465 \pm 0.0033$$

$$\sin^2 \theta_w^{eff} = 0.23159 \pm 0.00041$$

[hep-ex/0509008](https://arxiv.org/abs/hep-ex/0509008)

# Helicity Amplitudes and Asymmetries



Observables:

$$\sigma_F = \sigma_{LL} + \sigma_{RR}$$

$$\sigma_B = \sigma_{RL} + \sigma_{LR}$$

$$A_{FB} = \frac{\sigma_F - \sigma_B}{\sigma_F + \sigma_B}$$

Forward-backward asym. (final)

$$\sigma_L = \sigma_{LL} + \sigma_{LR}$$

$$\sigma_R = \sigma_{RL} + \sigma_{RR}$$

$$A_{LR} = \frac{\sigma_L - \sigma_R}{\sigma_L + \sigma_R}$$

Left right asym. (initial)

$$\sigma_- = \sigma_{LL} + \sigma_{RL}$$

$$\sigma_+ = \sigma_{RR} + \sigma_{LR}$$

$$\mathcal{P}_f = \frac{\sigma_+ - \sigma_-}{\sigma_+ + \sigma_-}$$

fermion polarization (final)

# Left Right Asymmetry at SLD

Measure cross section  $\sigma_L$  ( $\sigma_R$ ) for LH (RH) initial state electrons:

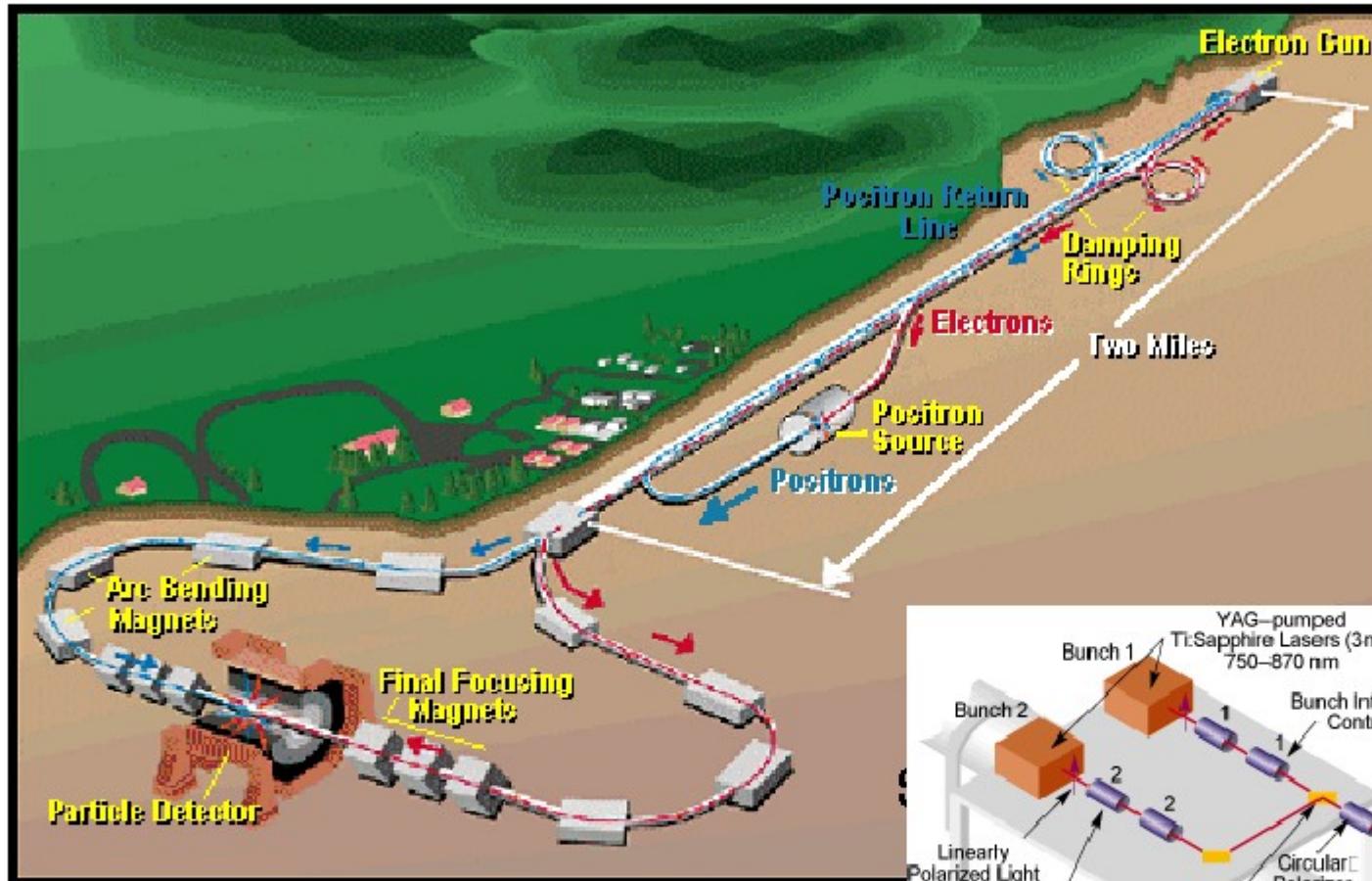
$$A_{LR} = \frac{1}{\mathcal{P}_e} \frac{\sigma_L^f - \sigma_R^f}{\sigma_L^f + \sigma_R^f}$$

Polarization of  
electron beam:  
 $P \sim 70 - 80\%$

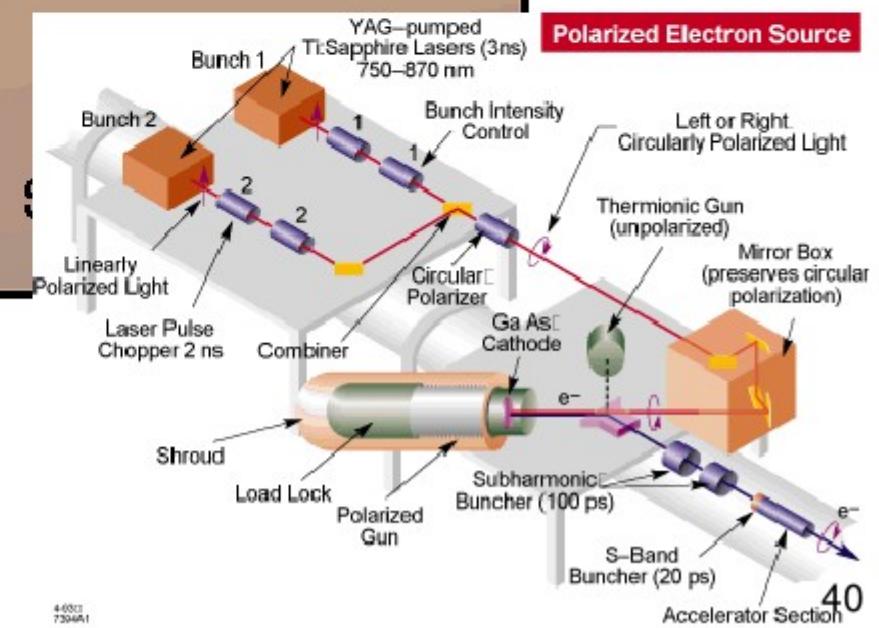
$$A_{LR} = \frac{2g_V^e g_A^e}{(g_V^e)^2 + (g_A^e)^2} = \frac{2(1 - 4 \sin^2 \theta_w)}{1 + (1 - 4 \sin^2 \theta_w)^2} = A_e$$

Powerful determination of  $\sin^2 \theta_w$ .  
Requires longitudinal polarization of colliding beams

# SLAC Linear Accelerator

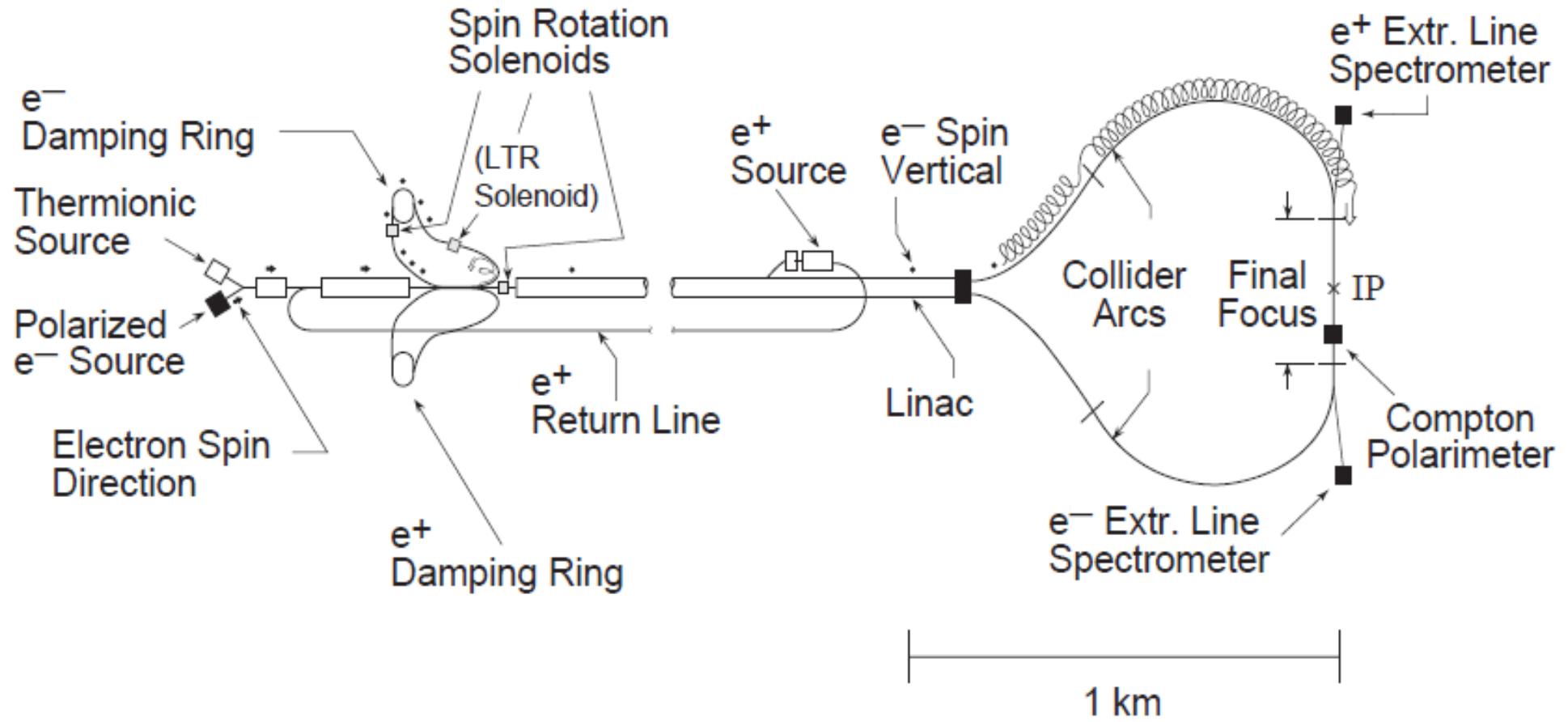


Typical beam polarization of 70%.



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# SLAC Linear Accelerator



# Compton Polarimeter

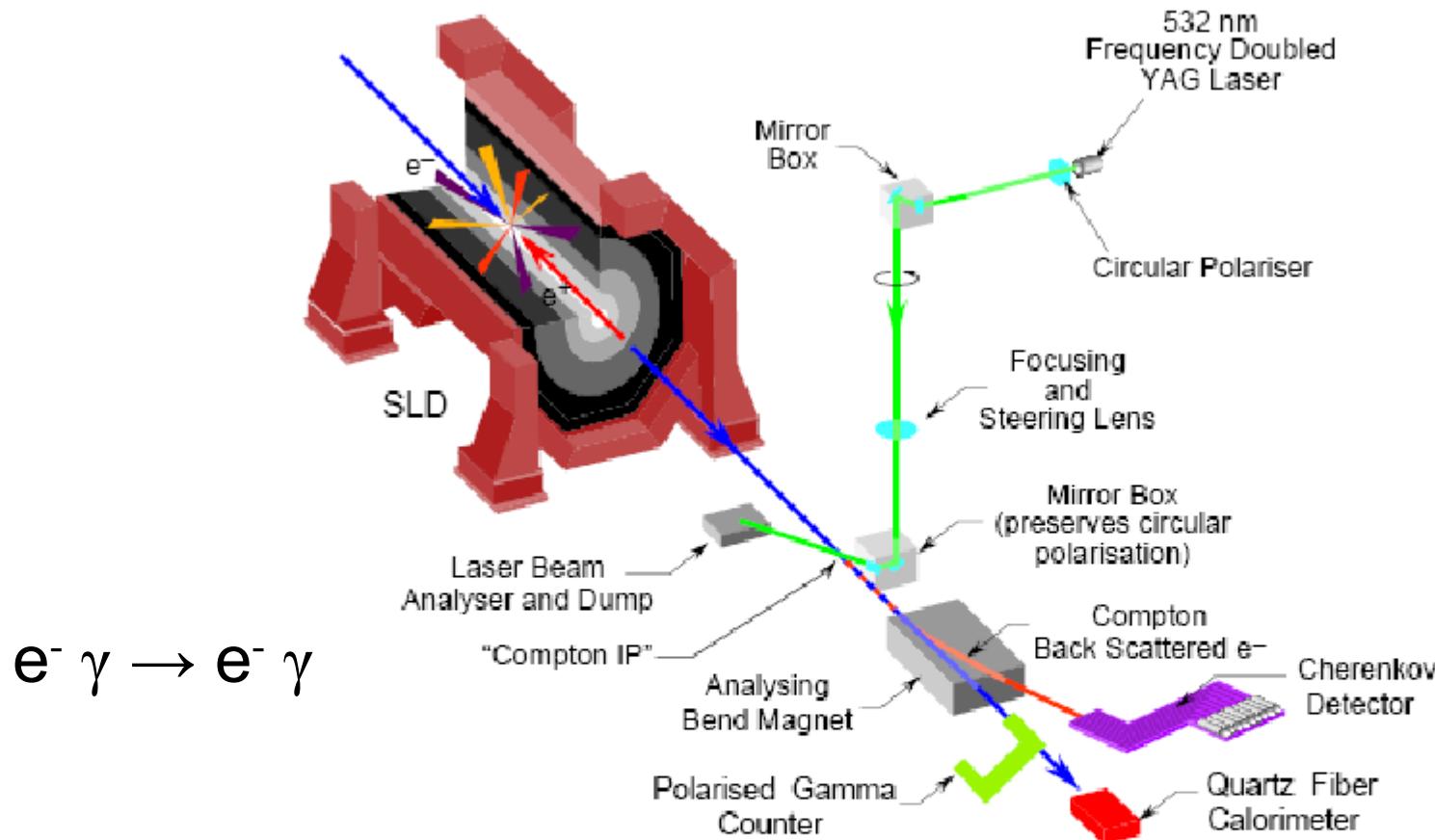
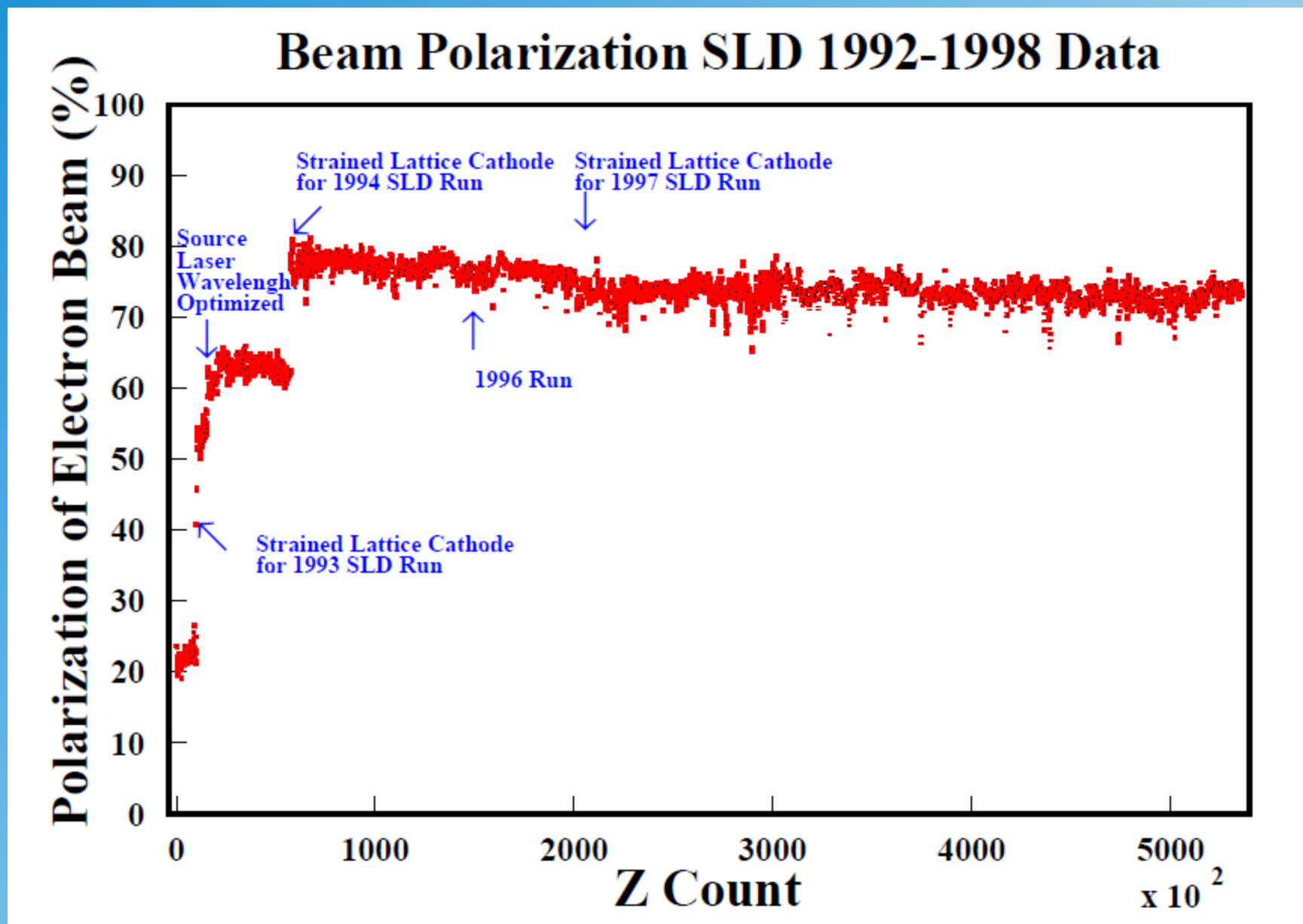
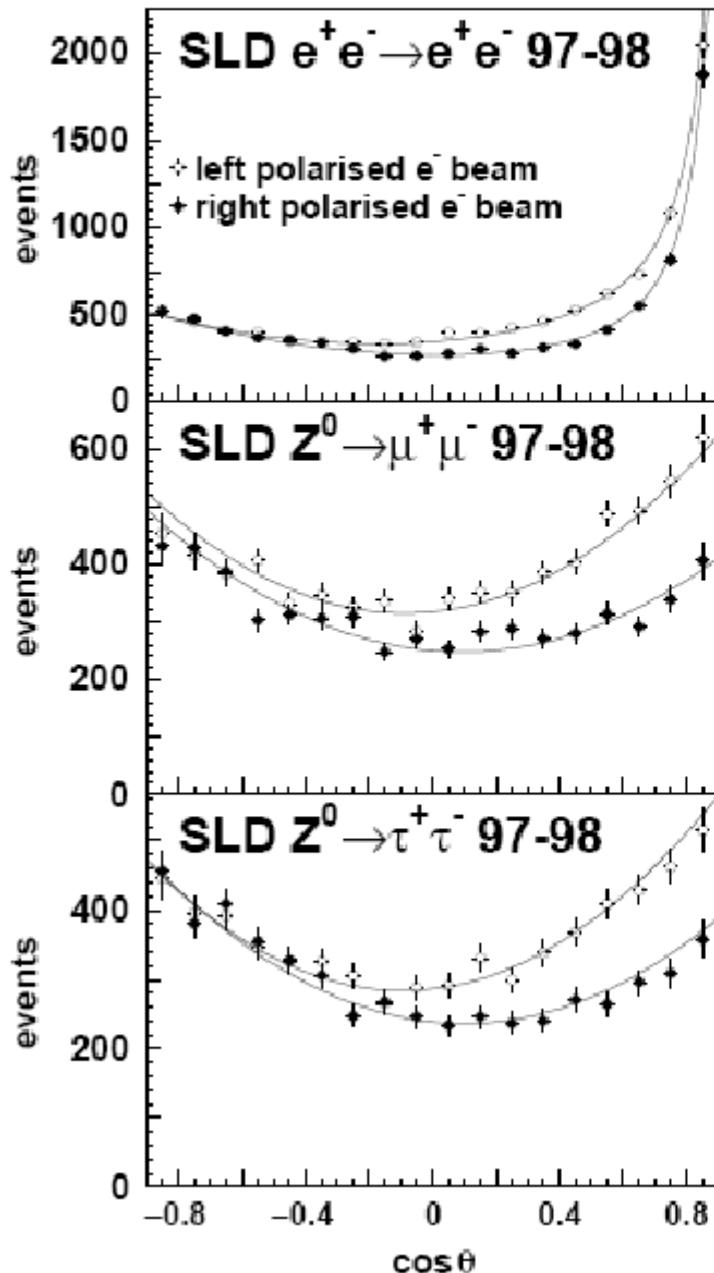


Figure 3.1: A conceptual diagram of the SLD Compton Polarimeter. The laser beam, consisting of 532 nm wavelength 8 ns pulses produced at 17 Hz and a peak power of typically 25 MW, were circularly polarised and transported into collision with the electron beam at a crossing angle of 10 mrad approximately 30 meters from the IP. Following the laser/electron-beam collision, the electrons and Compton-scattered photons, which are strongly boosted along the electron beam direction, continue downstream until analysing bend magnets deflect the Compton-scattered electrons into a transversely-segmented Cherenkov detector. The photons continue undeflected and are detected by a gamma counter (PGC) and a calorimeter (QFC) which are used to cross-check the polarimeter calibration.

# SLAC Electron Polarisation



# Results Polarisation Asymmetry



Leptonic Final States

SLD

Asymmetry  
clearly seen for  
LH and RH  
cross section.

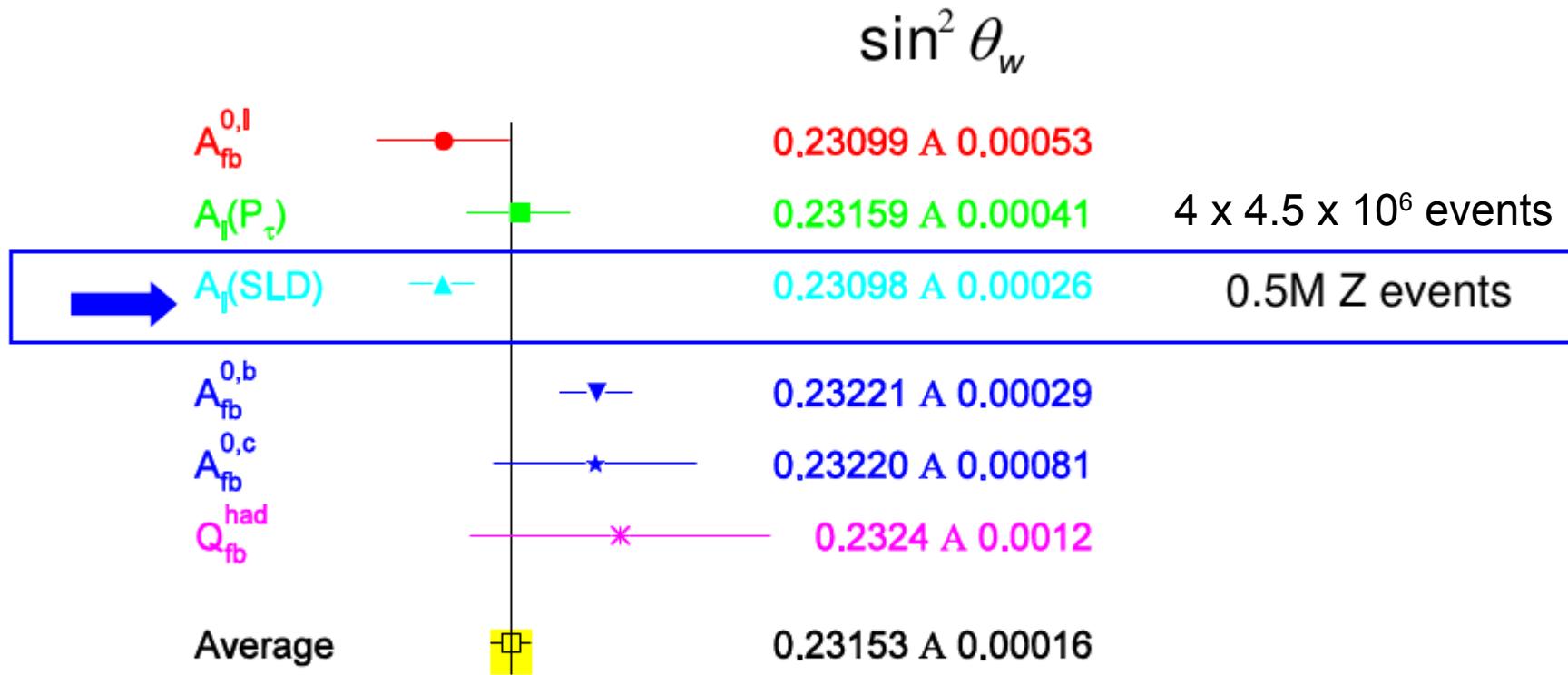
SLD All data:

$$A_{LR} = 0.1513 \pm 0.0021$$

$$\sin^2 \theta_w = 0.23098 \pm 0.00026$$

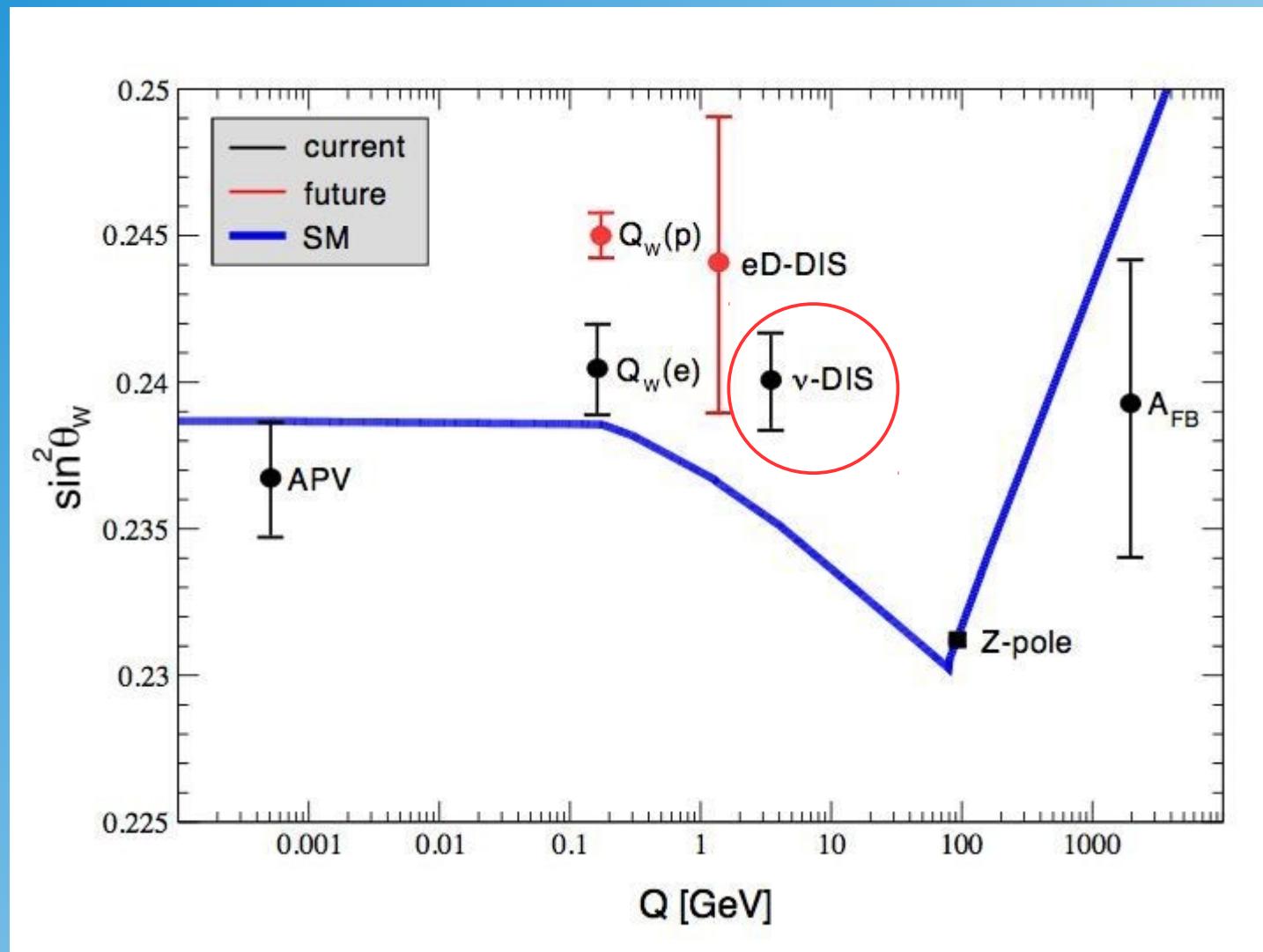
With  $0.5 \times 10^6$   
Z-decays

# Results Weinberg Angle



Despite the smaller statistics – SLD beats LEP in precision!

# “Running” of Weinberg Angle



→ note: here  $\sin^2 \Theta_W$  defined in the  $\overline{\text{MS}}$  scheme

# Discrepancies in the SM

## A Precise Determination of Electroweak Parameters in Neutrino-Nucleon Scattering

G. P. Zeller<sup>5</sup>, K. S. McFarland<sup>8,3</sup>, T. Adams<sup>4</sup>, A. Alton<sup>4</sup>, S. Avvakumov<sup>8</sup>, L. de Barbaro<sup>5</sup>, P. de Barbaro<sup>8</sup>, R. H. Bernstein<sup>3</sup>, A. Bodek<sup>8</sup>, T. Bolton<sup>4</sup>, J. Brau<sup>6</sup>, D. Buchholz<sup>5</sup>, H. Budd<sup>8</sup>, L. Bugel<sup>3</sup>, J. Conrad<sup>2</sup>, R. B. Drucker<sup>6</sup>, B. T. Fleming<sup>2</sup>, R. Frey<sup>6</sup>, J.A. Formaggio<sup>2</sup>, J. Goldman<sup>4</sup>, M. Goncharov<sup>4</sup>, D. A. Harris<sup>8</sup>, R. A. Johnson<sup>1</sup>, J. H. Kim<sup>2</sup>, S. Koutsoliotas<sup>2</sup>, M. J. Lamm<sup>3</sup>, W. Marsh<sup>3</sup>, D. Mason<sup>6</sup>, J. McDonald<sup>7</sup>, C. McNulty<sup>2</sup>, D. Naples<sup>7</sup>, P. Nienaber<sup>3</sup>, A. Romosan<sup>2</sup>, W. K. Sakamoto<sup>8</sup>, H. Schellman<sup>5</sup>, M. H. Shaevitz<sup>2</sup>, P. Spentzouris<sup>2</sup>, E. G. Stern<sup>2</sup>, N. Suwonjandee<sup>1</sup>, M. Tzanov<sup>7</sup>, M. Vakili<sup>1</sup>, A. Vaitaitis<sup>2</sup>, U. K. Yang<sup>8</sup>, J. Yu<sup>3</sup>, and E. D. Zimmerman<sup>2</sup>

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<sup>7</sup>*University of Pittsburgh, Pittsburgh, PA 15260*

<sup>8</sup>*University of Rochester, Rochester, NY 14627*

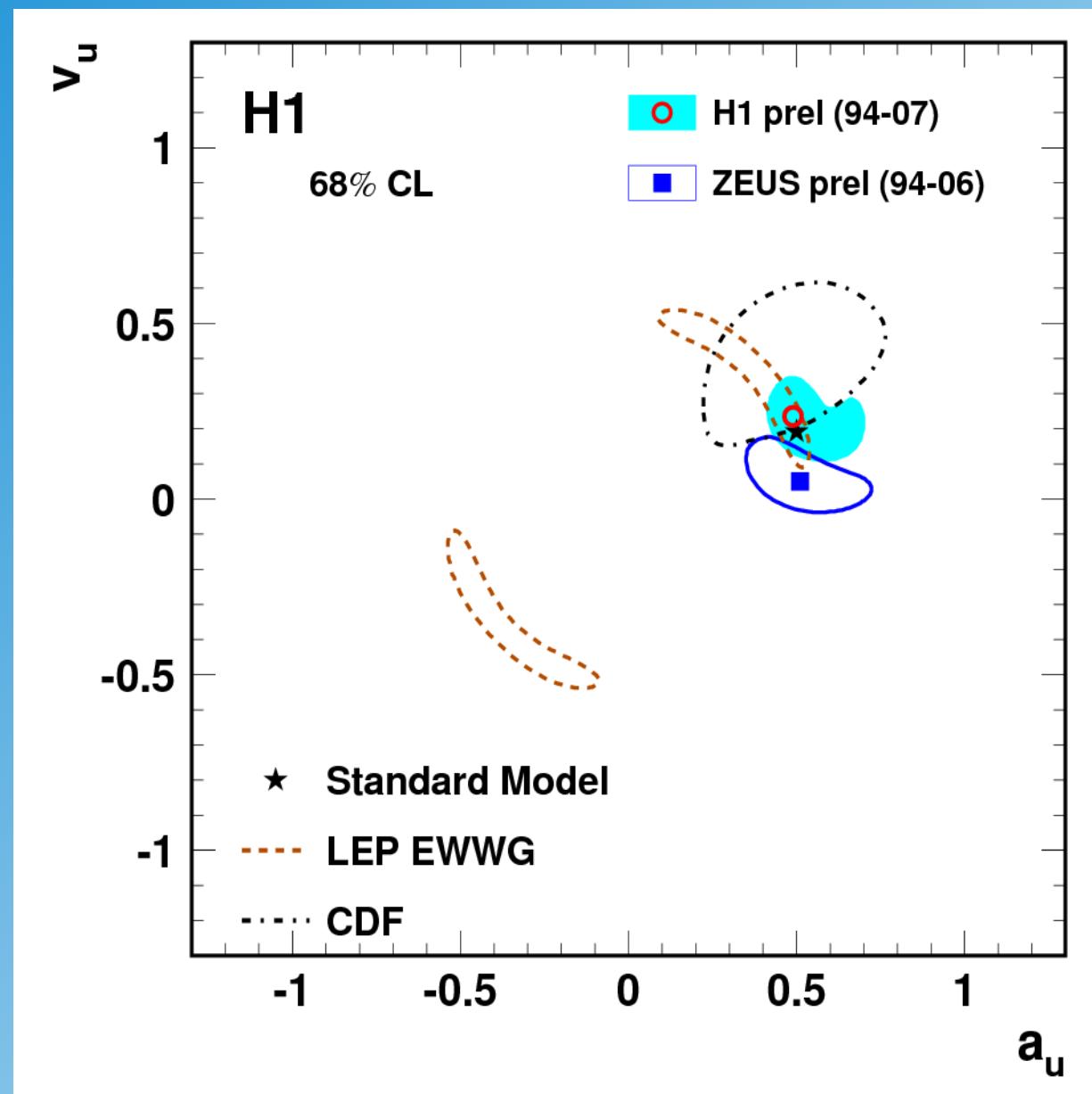
(February 4, 2008)

The NuTeV collaboration has extracted the electroweak parameter  $\sin^2 \theta_W$  from the measurement of the ratios of neutral current to charged current  $\nu$  and  $\bar{\nu}$  cross-sections. Our value,  $\sin^2 \theta_W^{(\text{on-shell})} = 0.2277 \pm 0.0013(\text{stat}) \pm 0.0009(\text{syst})$ , is 3 standard deviations above the standard model prediction. We also present a model independent analysis of the same data in terms of neutral-current quark couplings.

NuTev:  $\sin^2 \theta_W = 0.2277 \pm 0.0015$  (2003)

SM prediction:  $\sin^2 \theta_W = 0.22280 \pm 0.00035$  (2004)

# NC Quark Couplings: HERA + Tevatron

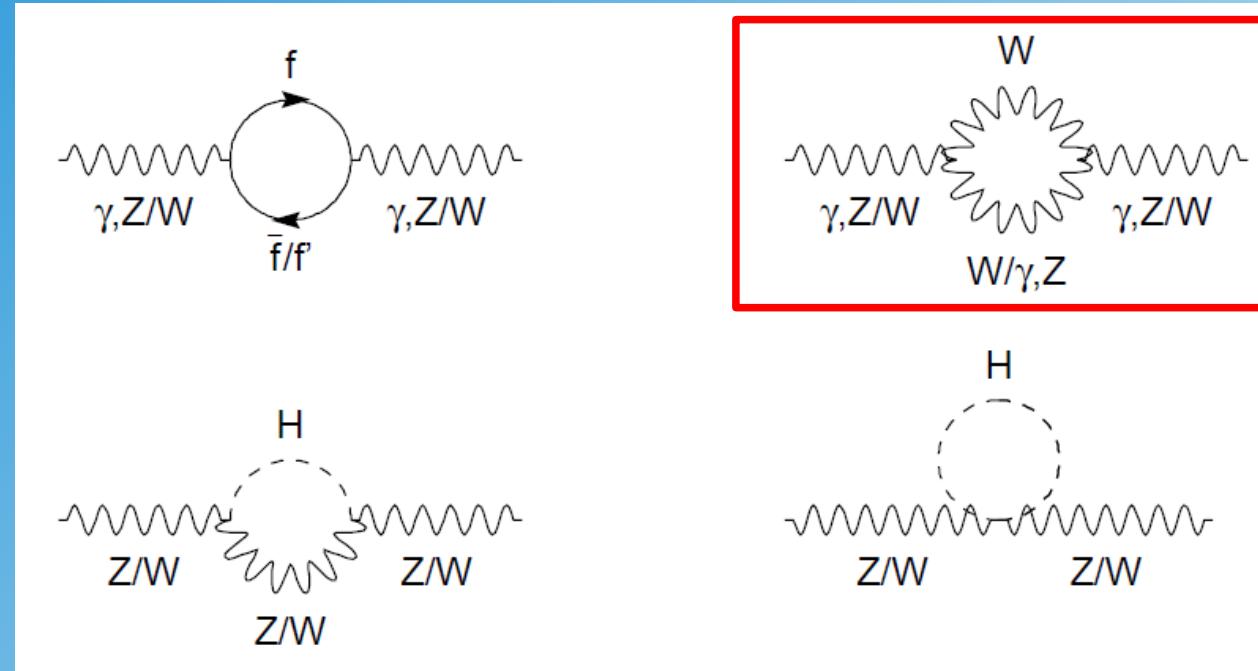


comparison LEP, Tevatron, HERA

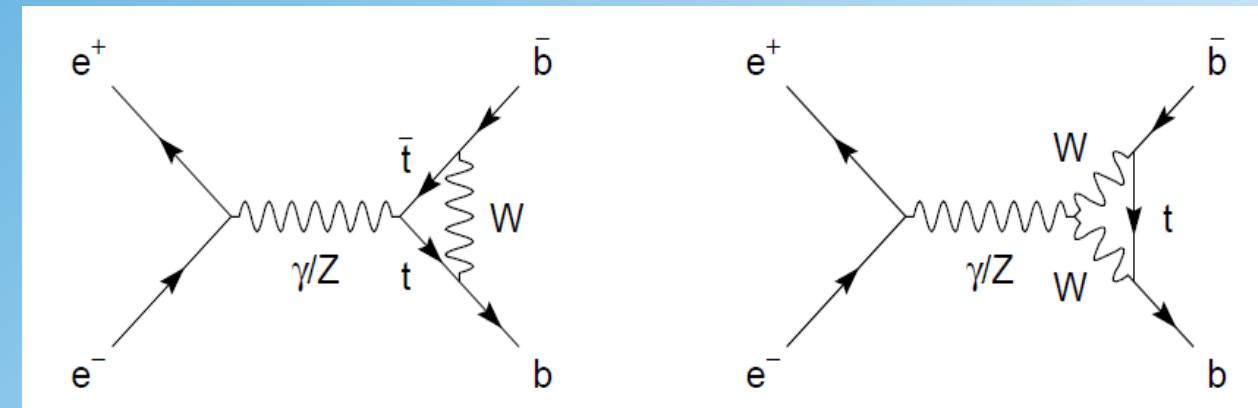
# Indirect W-Mass Constraints from LEP1

W-mass also enters in virtual radiative corrections:

self-energy

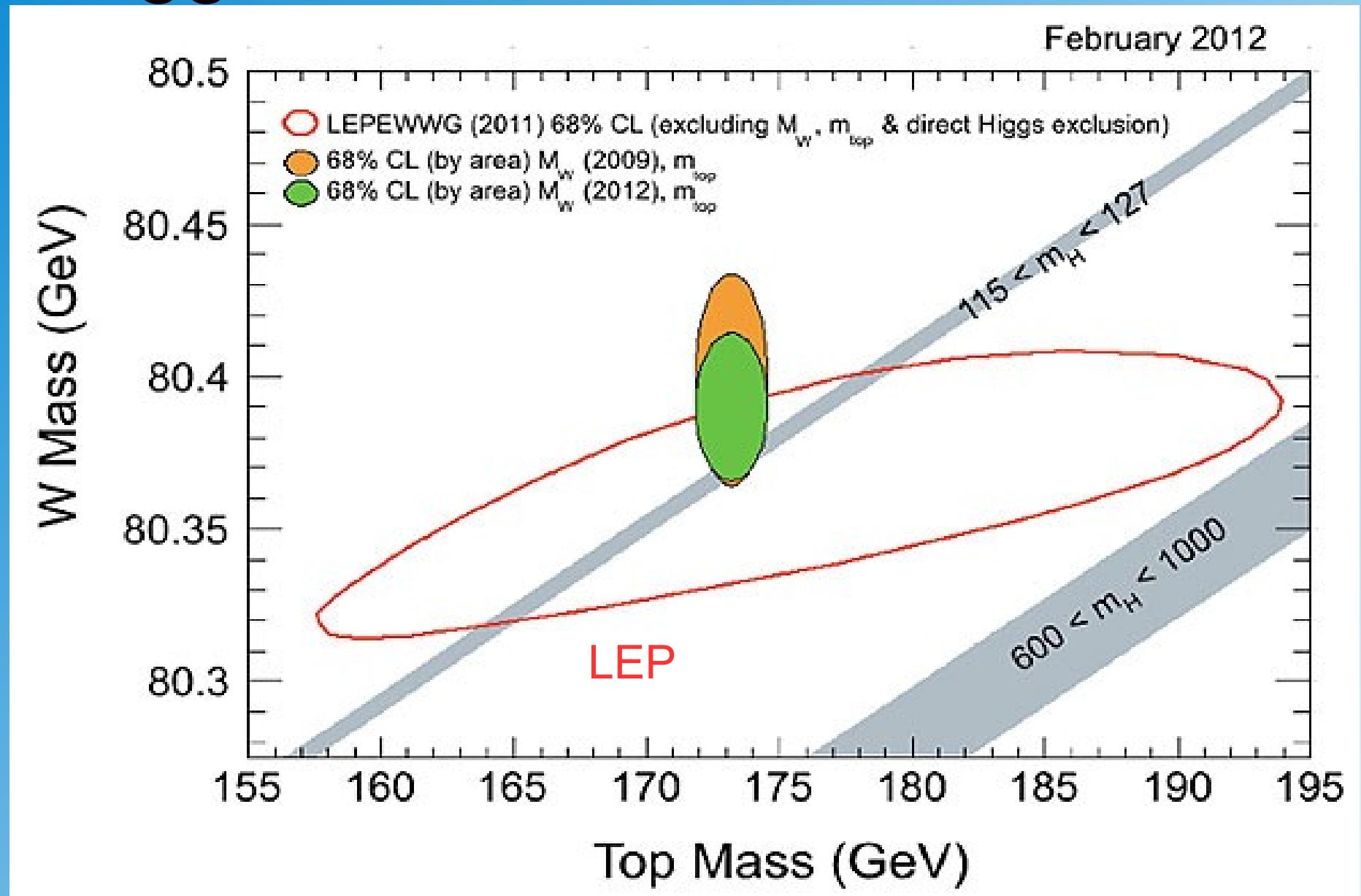


vertex correction



+ box diagrams

# Higgs Mass Constraint from LEP

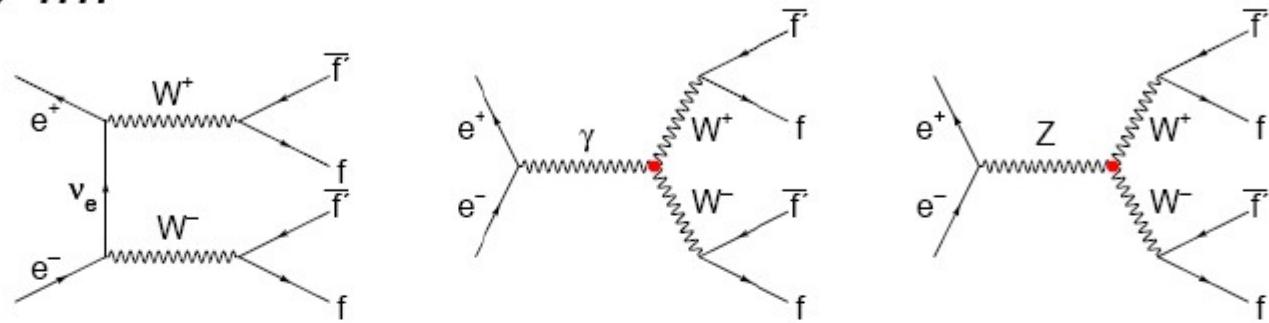


# LEP 2

after 1996 the LEP energy was steadily increased up to more than  $E_{\text{cms}} = 200 \text{ GeV}$

# $W^+ W^-$ Pair Production

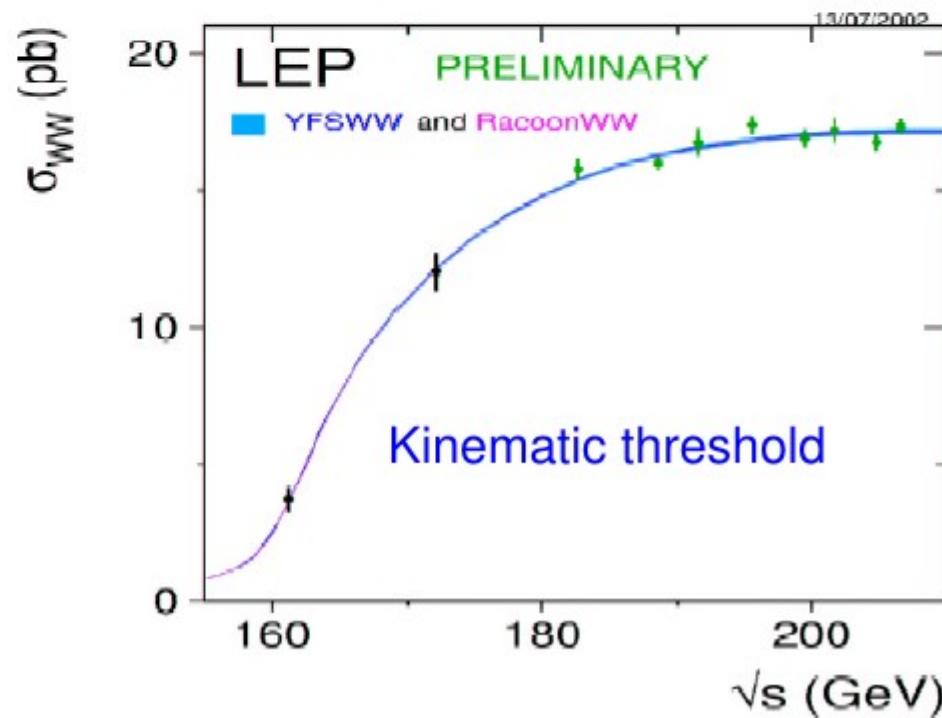
$$e^+ e^- \rightarrow WW \rightarrow f\bar{f} f\bar{f}$$



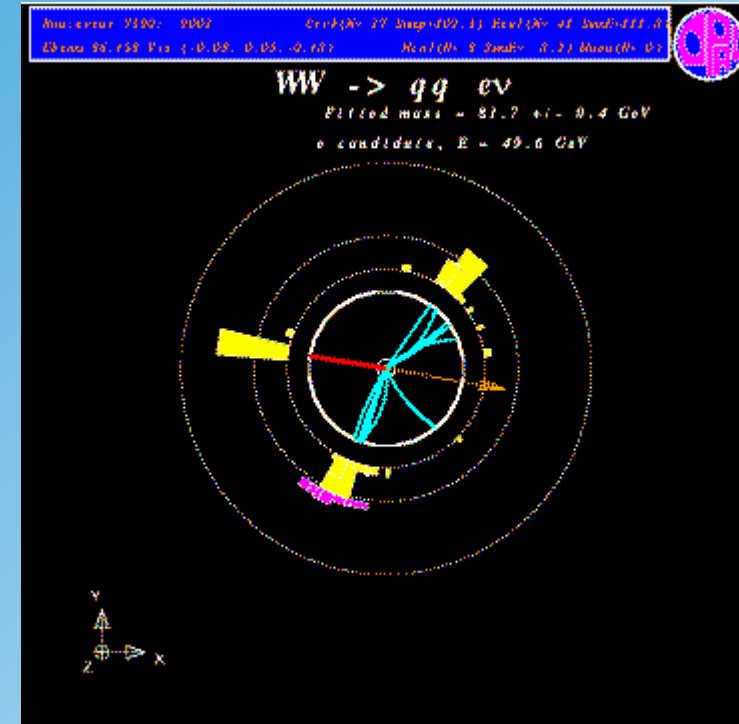
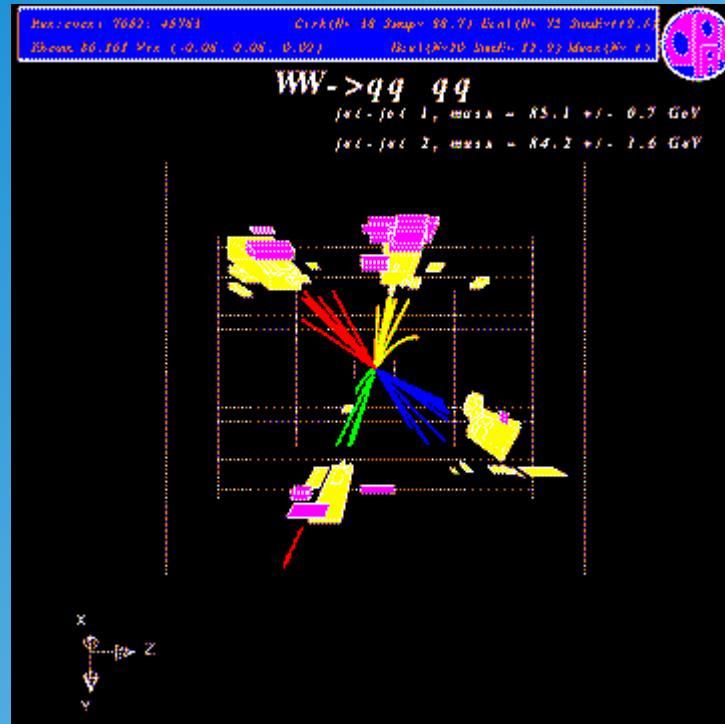
Threshold behavior of the cross section (kinematics, phase space) for  $ee \rightarrow WW$  production:



Phase space factor =  $f(M_W, \sqrt{s})$ :  
→ Allows determination of  $M_W$



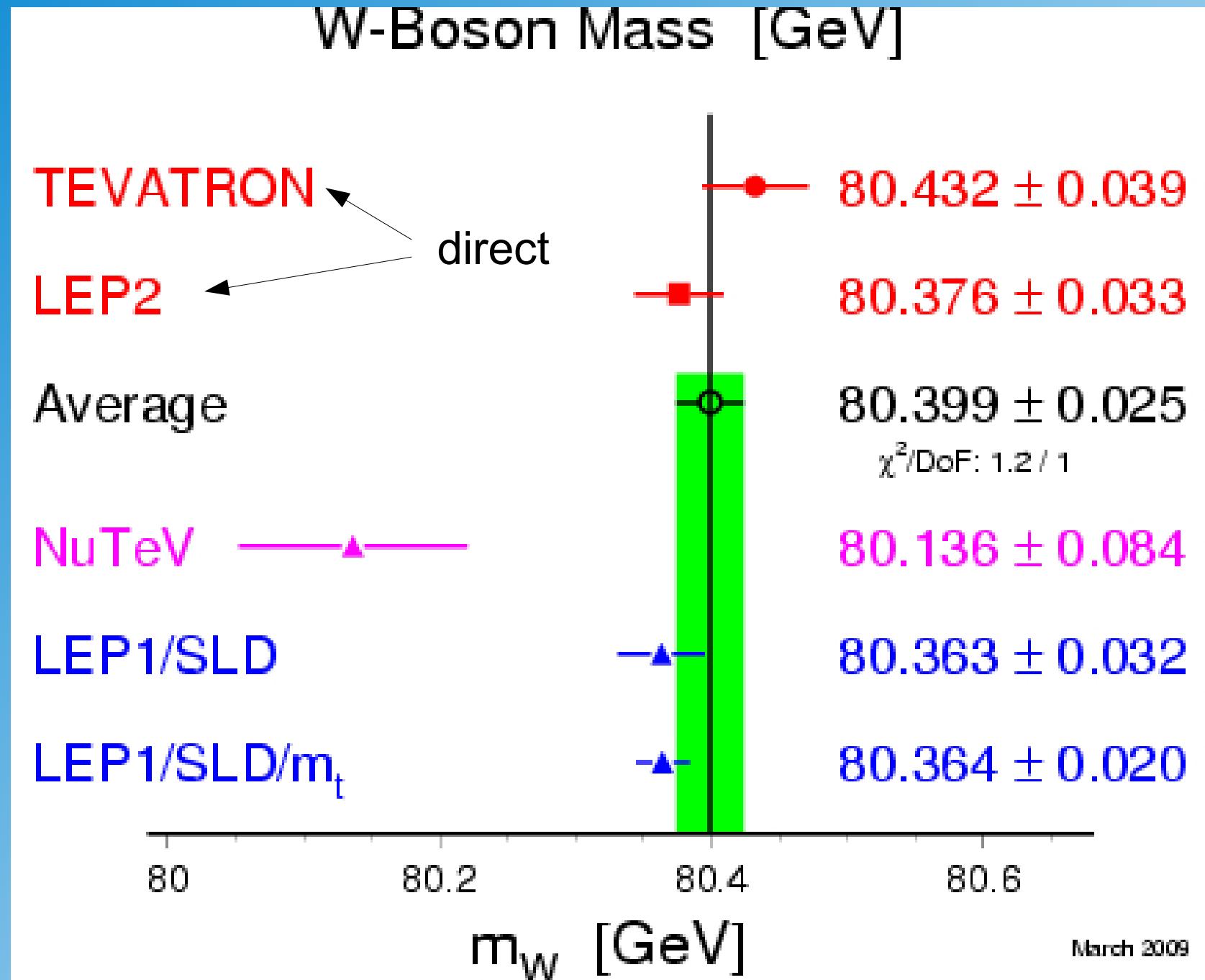
# WW Candidates



kinematics of  $WW \rightarrow qqqq$  (46%) and  $WW \rightarrow qq\ell\nu$  (44%)  
used to reconstruct W-mass

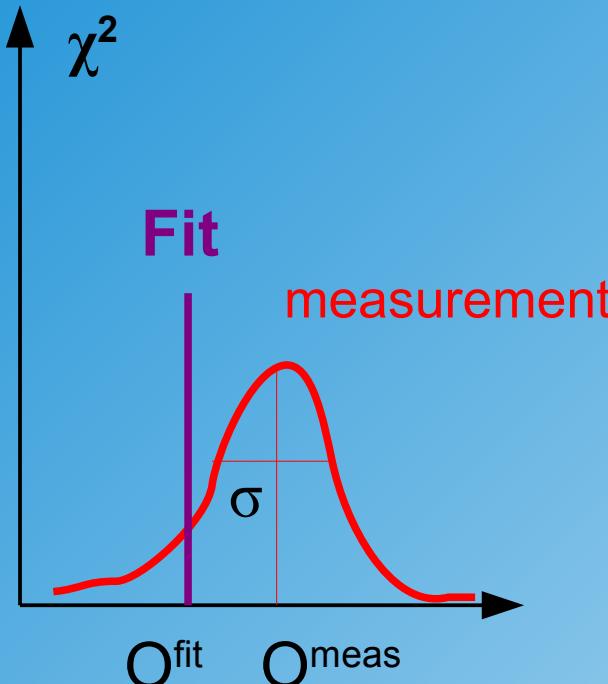
problems: color reconnection + missing neutrino!

# Electroweak Fit of the W-Boson Mass



# The SM pull plot

Z-pole parameters



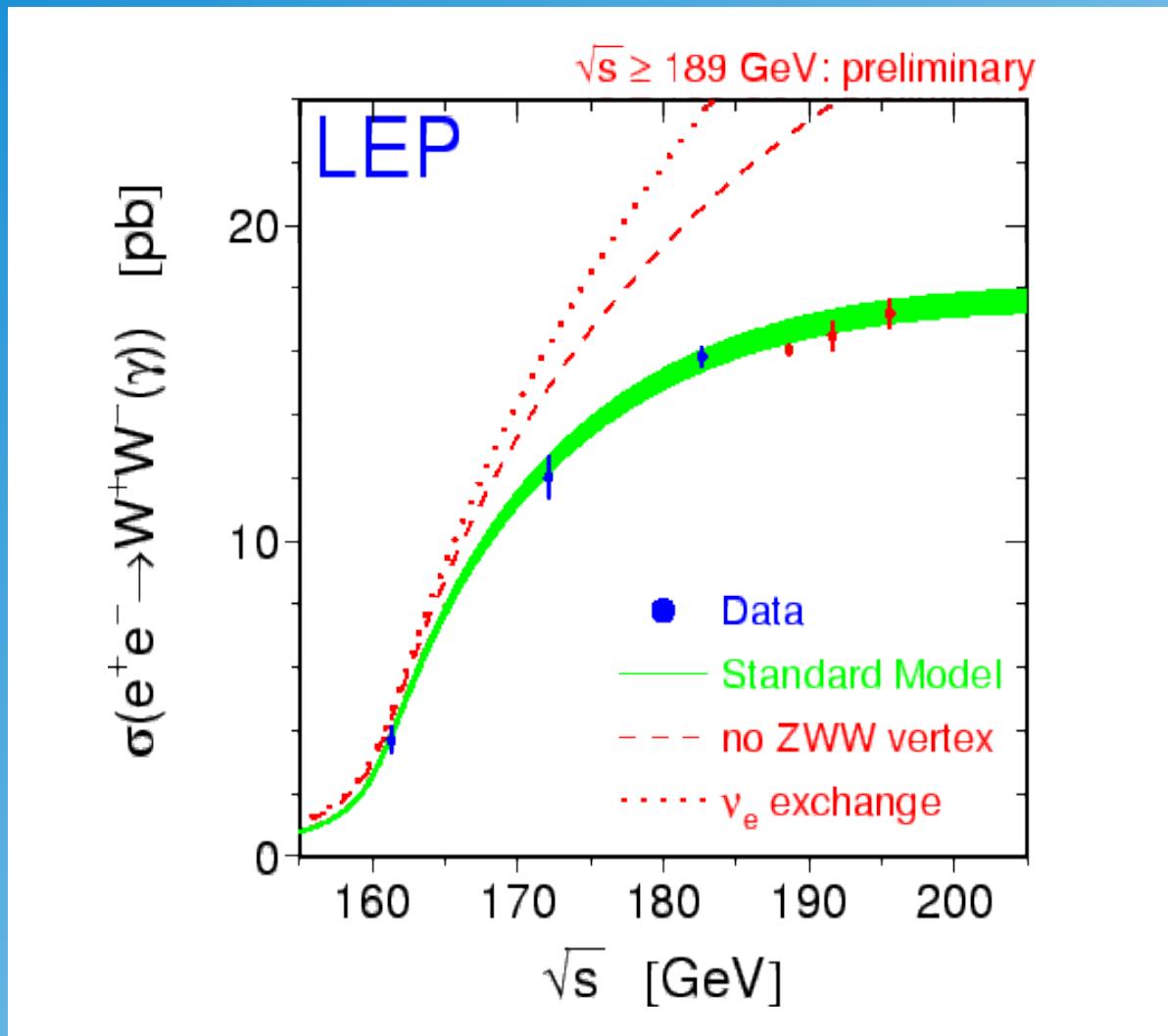
	Measurement	Fit	$ O^{meas} - O^{fit} /\sigma^{meas}$
$\Delta\alpha_{had}^{(5)}(m_Z)$	$0.02758 \pm 0.00035$	0.02767	0.2
$m_Z$ [GeV]	$91.1875 \pm 0.0021$	91.1874	0.1
$\Gamma_Z$ [GeV]	$2.4952 \pm 0.0023$	2.4959	0.3
$\sigma_{had}^0$ [nb]	$41.540 \pm 0.037$	41.478	1.7
$R_I$	$20.767 \pm 0.025$	20.742	1.0
$A_{fb}^{0,I}$	$0.01714 \pm 0.00095$	0.01643	0.7
$A_I(P_\tau)$	$0.1465 \pm 0.0032$	0.1480	0.5
$R_b$	$0.21629 \pm 0.00066$	0.21579	0.7
$R_c$	$0.1721 \pm 0.0030$	0.1723	0.1
$A_{fb}^{0,b}$	$0.0992 \pm 0.0016$	0.1038	2.9
$A_{fb}^{0,c}$	$0.0707 \pm 0.0035$	0.0742	1.0
$A_b$	$0.923 \pm 0.020$	0.935	0.5
$A_c$	$0.670 \pm 0.027$	0.668	0.1
$A_I(SLD)$	$0.1513 \pm 0.0021$	0.1480	1.7
$\sin^2\theta_{eff}^{lept}(Q_{fb})$	$0.2324 \pm 0.0012$	0.2314	0.9
$m_W$ [GeV]	$80.399 \pm 0.025$	80.378	1.0
$\Gamma_W$ [GeV]	$2.098 \pm 0.048$	2.092	0.2
$m_t$ [GeV]	$173.1 \pm 1.3$	173.2	0.1

March 2009

=> consistent with SM

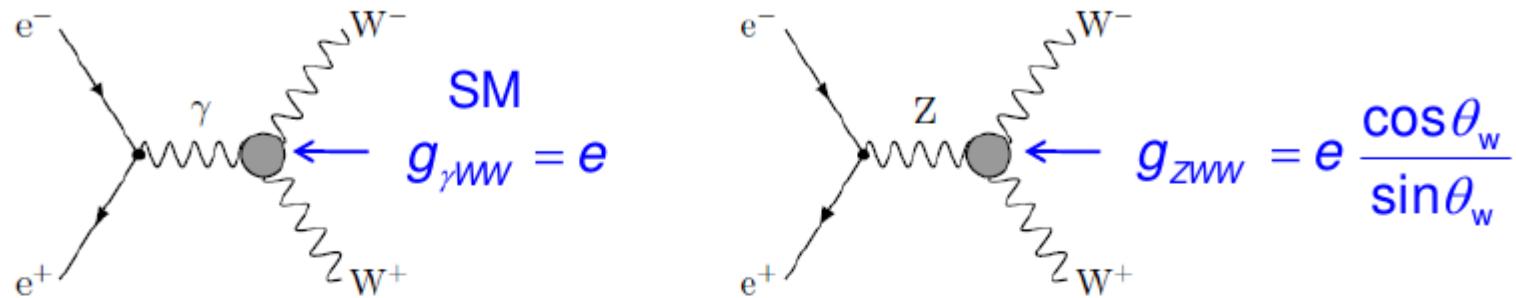
# Triple Gauge Couplings

WW Production Cross Section



LEP 2 has proven  
existence of triple  
gauge couplings

# Test of trilinear gauge boson coupling in WW production



Triple gauge coupling an important result of the non-abelian gauge structure.

Most general Lagrangian for  $\gamma$ VWW:

$$\begin{aligned}
 i\mathcal{L}_{\text{eff}}^{\text{VWW}} / g_{\text{VWW}} &= \boxed{g_1^V} V^\mu (W_{\mu\nu}^- W^{+\nu} - W_{\mu\nu}^+ W^{-\nu}) \\
 &\quad + \boxed{\kappa_V} W_\mu^+ W_\nu^- V^{\mu\nu} + \frac{\lambda_V}{m_W^2} V^{\mu\nu} W_\nu^{+\rho} W_{\rho\mu}^- \\
 &\quad + ig_5^V \varepsilon_{\mu\nu\rho\sigma} ((\partial^\rho W^{-\mu}) W^{+\nu} - W^{-\mu} (\partial^\rho W^{+\nu})) V^\sigma \\
 &\quad + ig_4^V W_\mu^+ W_\nu^- (\partial^\mu V^\nu + \partial^\nu V^\mu) \\
 &\quad - \frac{\tilde{\kappa}_V}{2} W_\mu^- W_\nu^+ \varepsilon^{\mu\nu\rho\sigma} V_{\rho\sigma} - \frac{\tilde{\lambda}_V}{2m_W^2} W_{\mu\mu}^- W_\nu^{+\mu} \varepsilon^{\nu\rho\alpha\beta} V_{\alpha\beta}.
 \end{aligned}$$

$\boxed{\phantom{0}} = 1,$   
all others 0

$\Delta\kappa, \Delta g_1 \neq 0$   
Deviation from SM

Interpretation for  $\gamma$ WW

$$\begin{aligned}
 q_W &= \pm g_V^\gamma \text{ charge} \\
 \mu_W &= \frac{e}{2M_W} (1 + \kappa_\gamma + \lambda_\gamma) \\
 &\quad \text{Dipol moment}
 \end{aligned}$$

### Triple Gauge couplings:

Assuming electromagnetic gauge invariance as well as C and P conservation, the number of independent TGCs reduces to five.  
 Common set: {  $g_1^Z$ ,  $\kappa_Z$ ,  $\kappa_\gamma$ ,  $\lambda_Z$ ,  $\lambda_\gamma$  }

Parameters used by the LEP experiments are:  $g_1^Z$ ,  $\kappa_\gamma$ ,  $\lambda_\gamma$

With additional gauge constraints

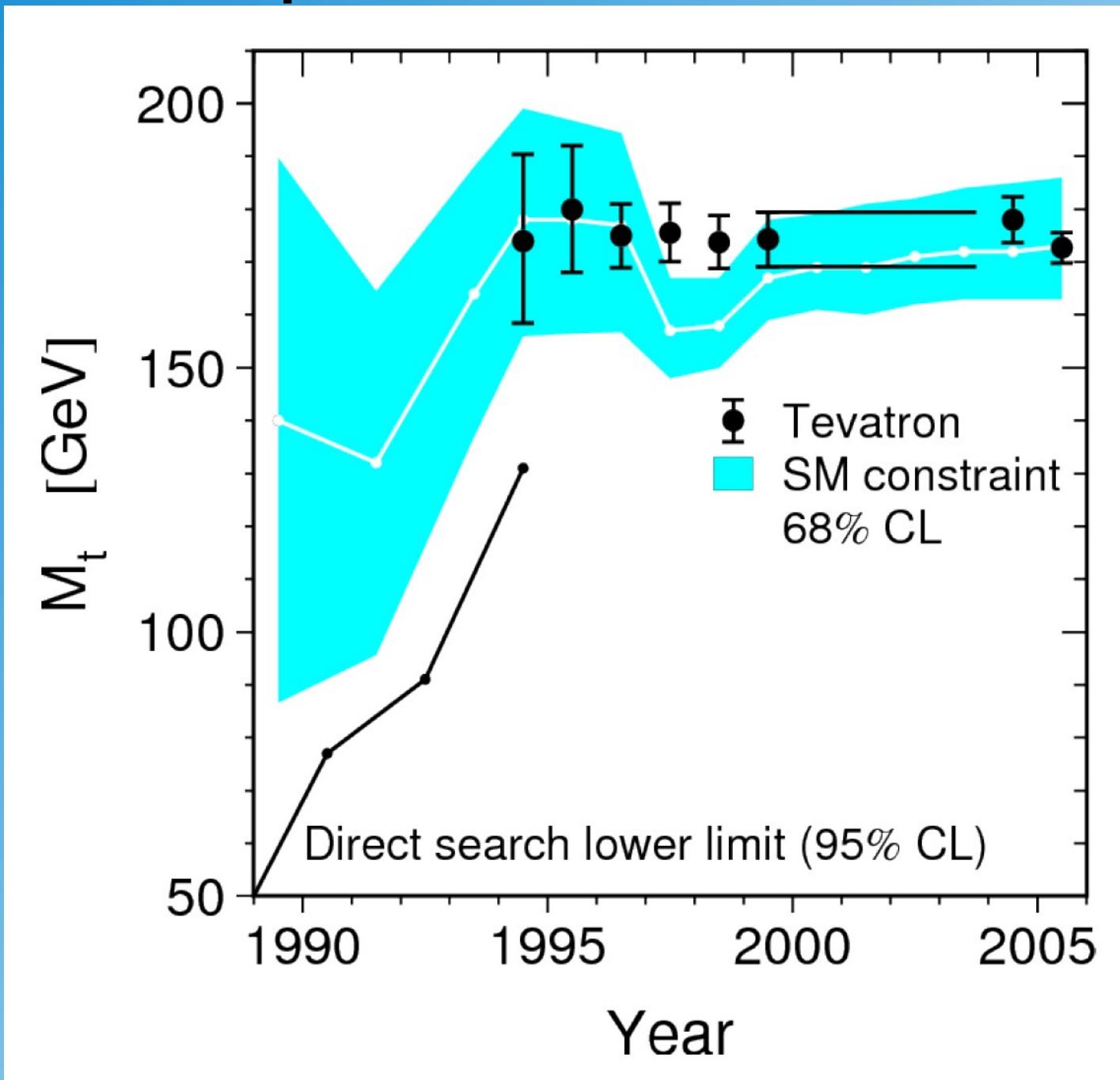
$$\begin{aligned}\kappa_Z &= g_1^Z - (\kappa_\gamma - 1) \tan^2 \theta_W \\ \lambda_Z &= \lambda_\gamma,\end{aligned}$$

From a fit to the angular distribution of the WW:

Parameter	68% C.L.	
$g_1^Z$	$0.984^{+0.022}_{-0.019}$	
$\kappa_\gamma$	$0.973^{+0.044}_{-0.045}$	$=1$ in SM
$\lambda_\gamma$	$-0.028^{+0.020}_{-0.021}$	$=0$ in SM

Standard Model structure of VWW triple boson coupling confirmed.

# Top Mass Prediction



# Top Mass Prediction from Radiative Corrections

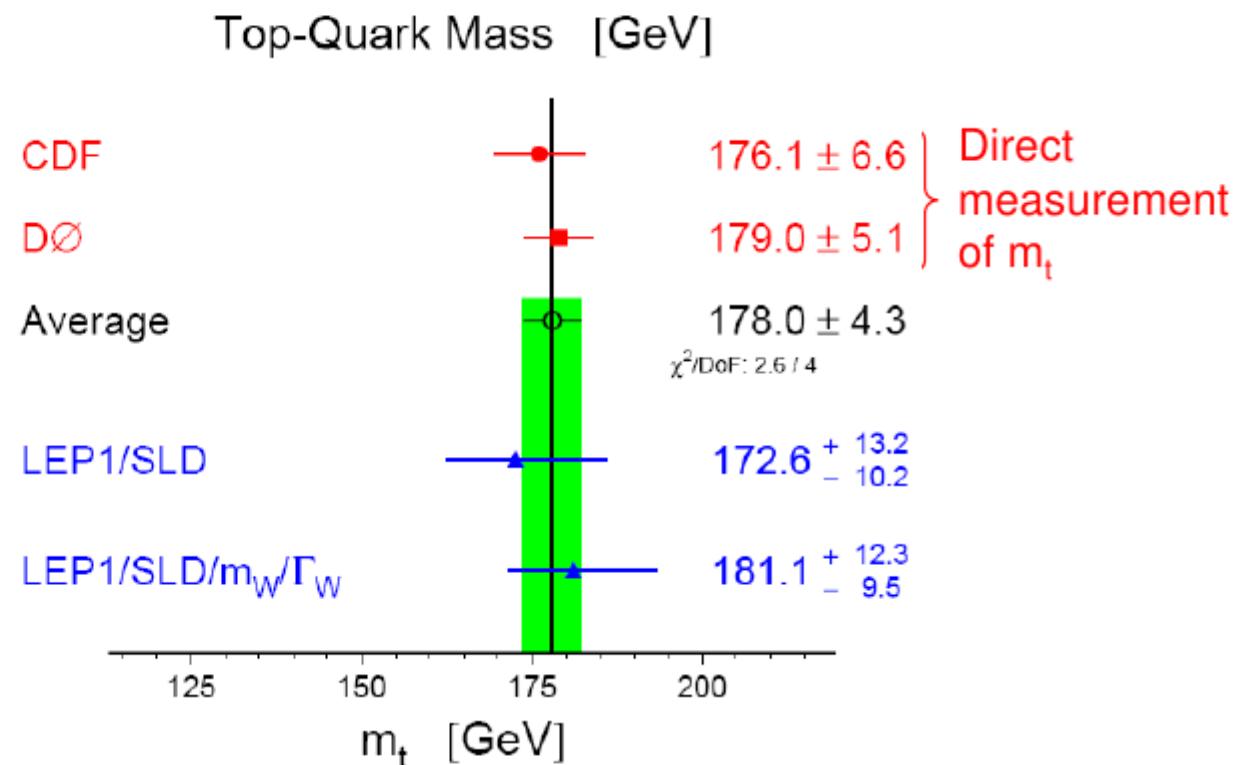
$$\text{e.g.: } \Delta r(m_t, M_H) = -\frac{3\alpha \cos^2 \theta_w}{16\pi \sin^4 \theta_w} \frac{m_t^2}{M_W^2} - \frac{11\alpha}{48\pi \sin^2 \theta_w} \ln \frac{M_H^2}{M_W^2} + \dots$$

The measurement of the radiative corrections:

$$\sin^2 \theta_{\text{eff}} \equiv \frac{1}{4} (1 - \bar{g}_V / \bar{g}_A)$$

$$\sin^2 \theta_{\text{eff}} = (1 + \Delta \kappa) \sin^2 \theta_w$$

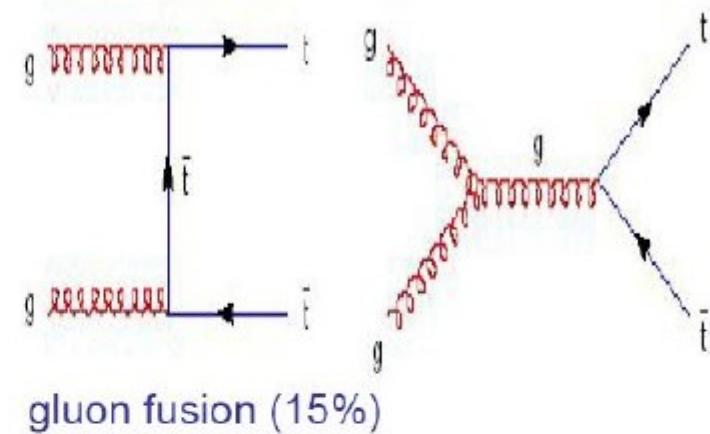
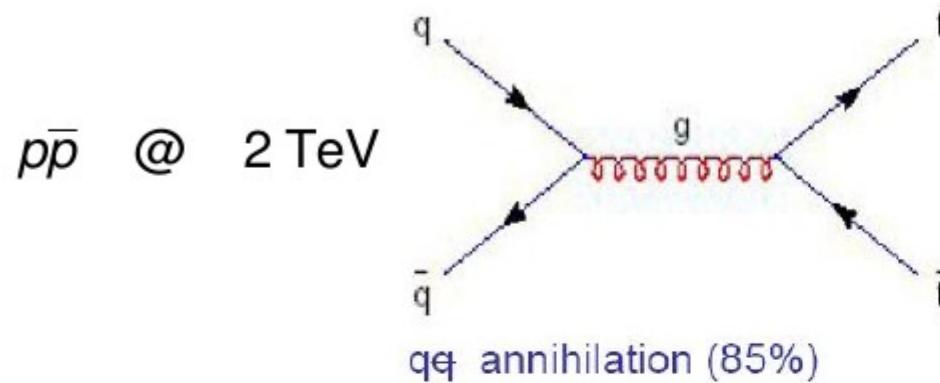
Allows the indirect determination of the unknown parameters  $m_t$  and  $M_H$ .



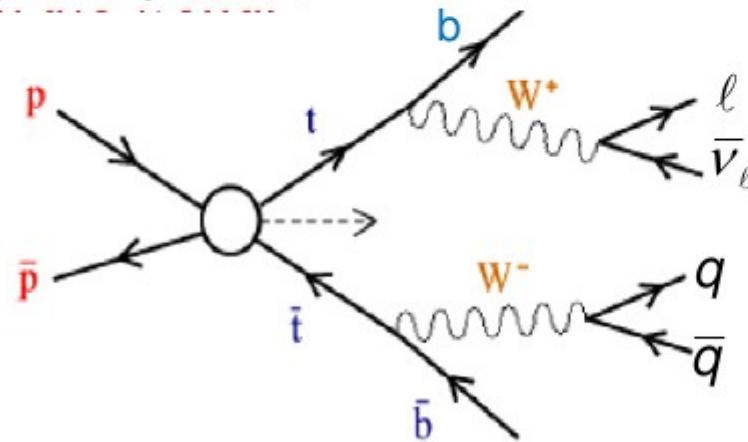
Good agreement between the indirect prediction of  $m_t$  and the value obtained in direct measurements confirm the radiative corrections of the SM

Prediction of  $m_t$  by LEP before the discovery of the top at TEVATRON.

# Top Discovery at Tevatron in 1995

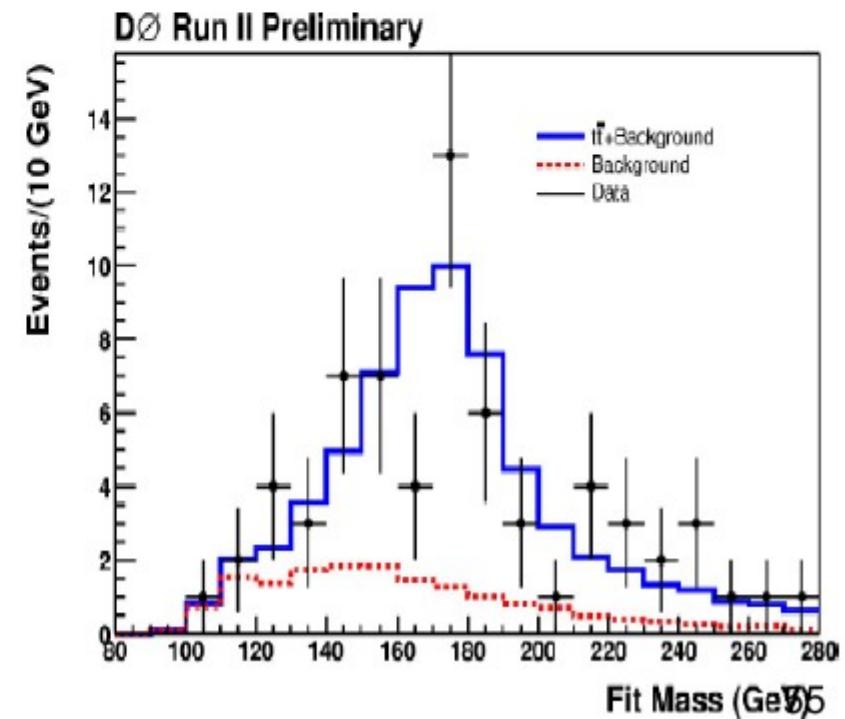


Top decay (decays before hadronization)

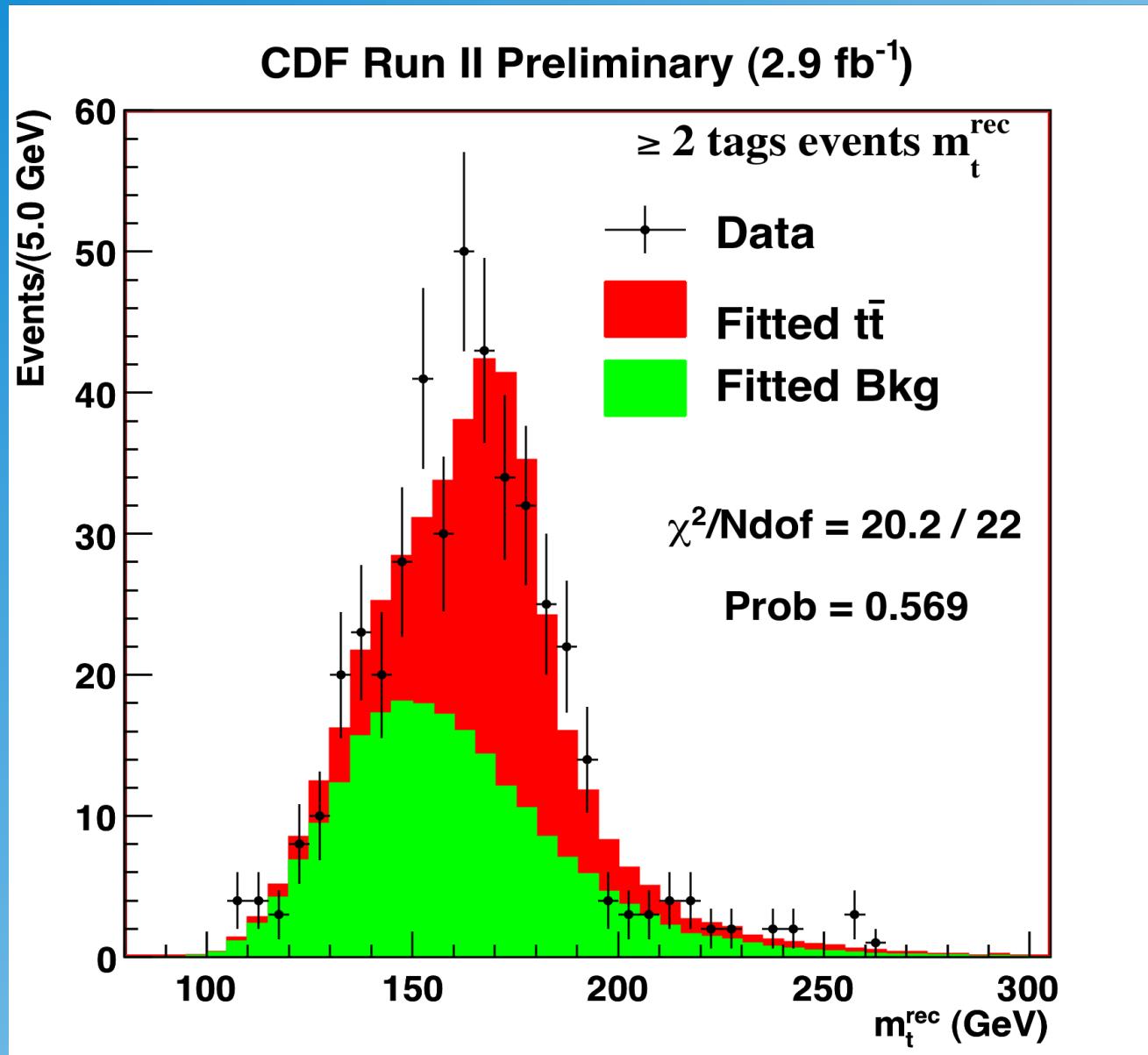


Channel used for mass reconstruction:

$$m_t = m_{inv}(b\text{-jet}, W \rightarrow \text{jet} + \text{jet})$$



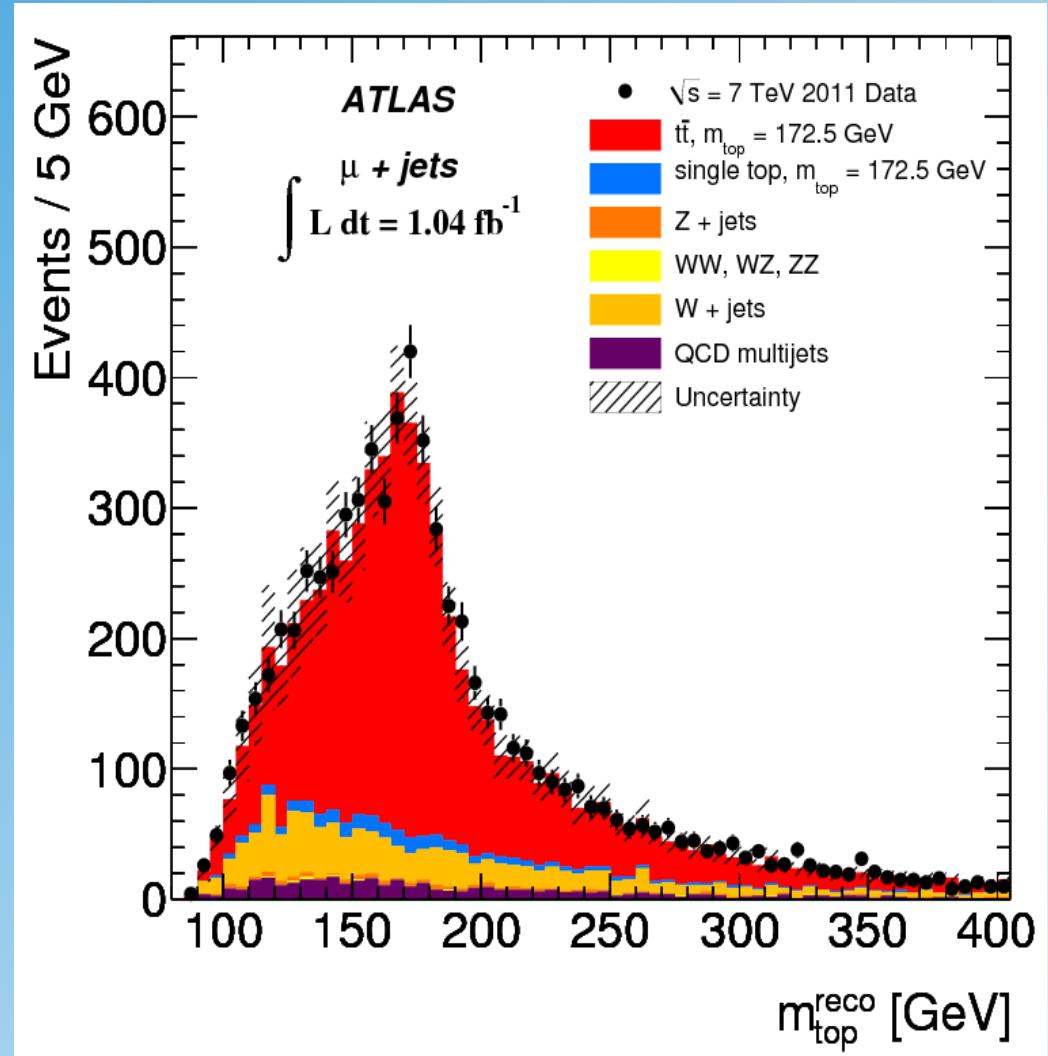
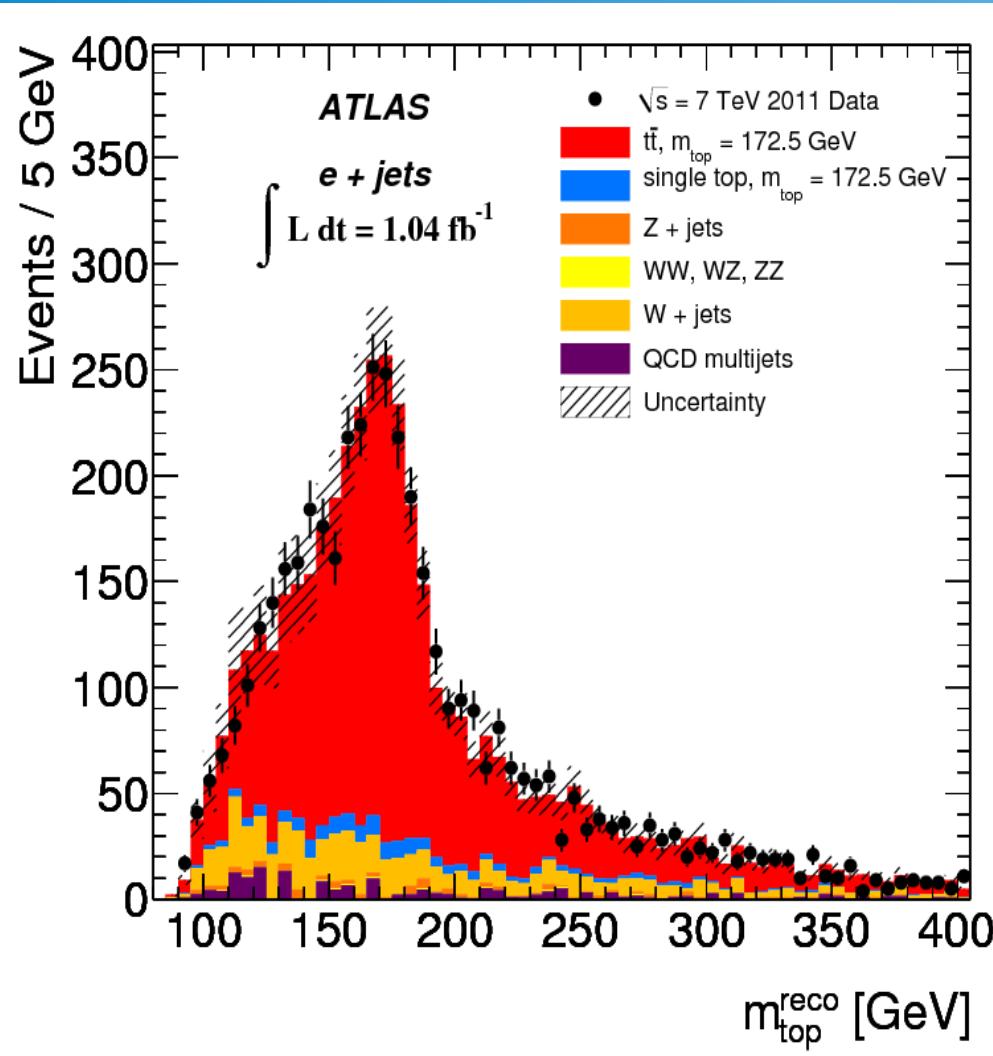
# Top Mass Reconstruction



multi-channel  
analysis

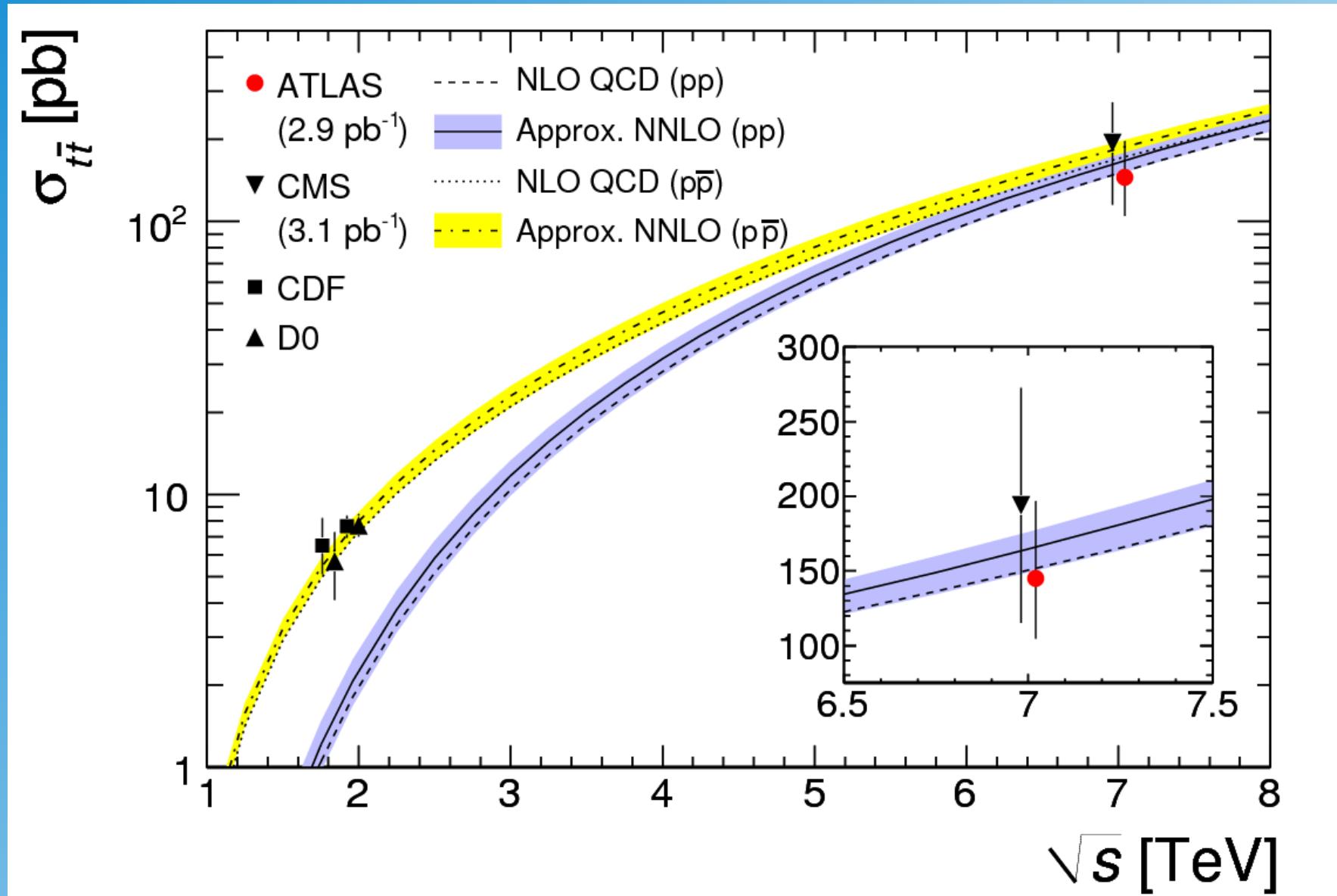
$m_t \sim 172 (1) \text{ GeV}$

# First Results from ATLAS (LHC)



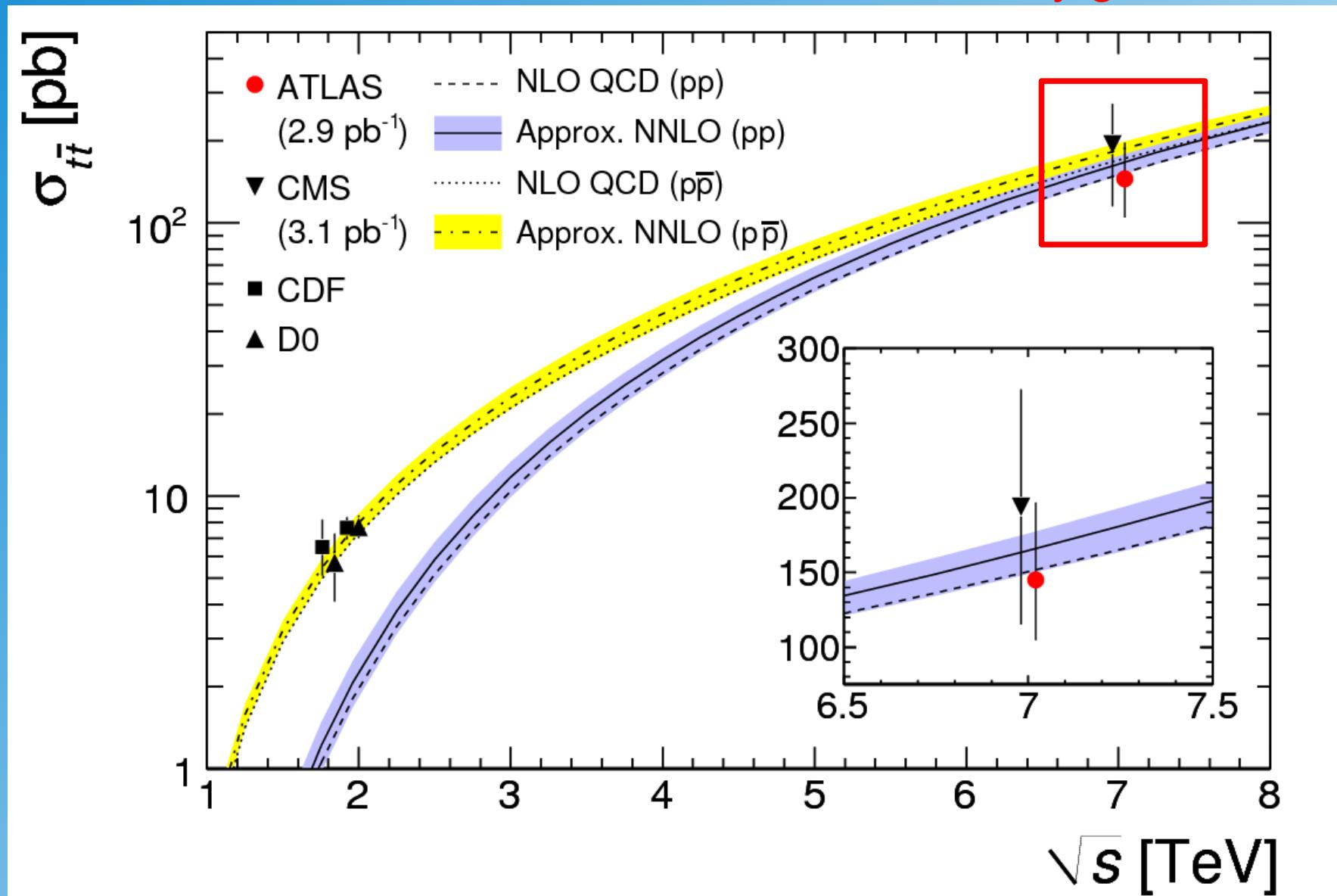
in the mean time millions of tops recorded!

# First Results from ATLAS (LHC)



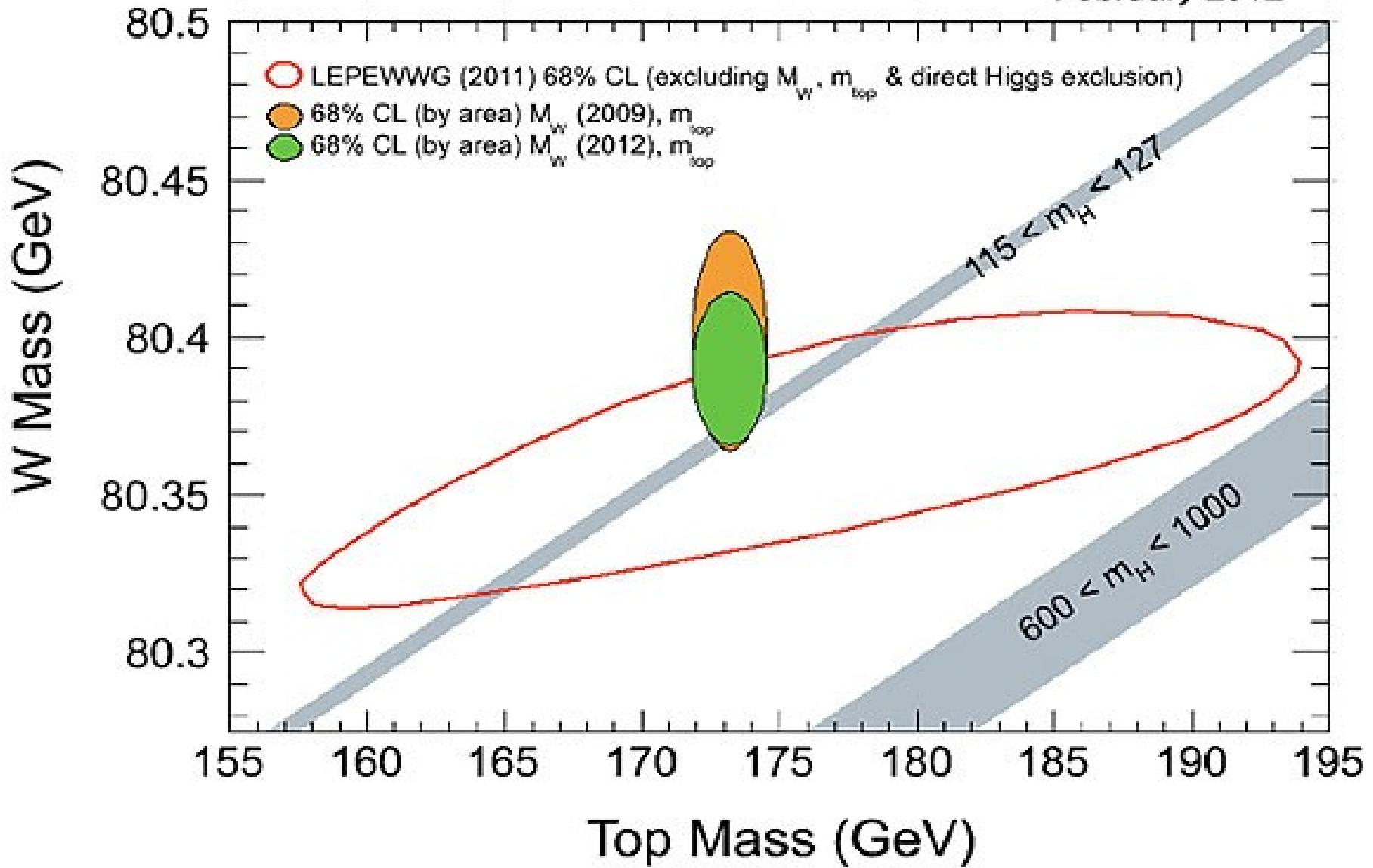
# First Results from ATLAS (LHC)

mainly gluon fusion



# Higgs Mass Constraint

February 2012



Higgs mass should be light!

