

Lecture:

# Standard Model of Particle Physics

Heidelberg SS 2016

QCD Tests

# Contents

- General Concepts
- QCD jets & jet algorithm
- Measurement of  $\alpha_s$
- Measurement of Quark and Gluon Spins
- Measurement of Color Factors

# Intermezzo QCD

## QCD Lagrangian (physical fields)

$$L_{phys} = -\frac{1}{4}F^\alpha{}_{\mu\nu}(x)F_\alpha{}^{\mu\nu}(x) + \sum_k \frac{i}{2}(\bar{q}_k(x)\gamma^\mu\nabla_\mu q_k(x) - \nabla_\mu\bar{q}_k(x)\gamma^\mu q_k(x)) .$$

vector coupling

Covariant derivative:

$$\nabla_\mu q(x) = \partial_\mu q(x) - i g G_\mu^\alpha(x) \hat{t}_\alpha q(x) ;$$

SU(3) group generators

Gluon field: non-abelian coupling

$$F^\alpha_{\mu\nu}(x) = \partial_\mu G_\nu^\alpha(x) - \partial_\nu G_\mu^\alpha(x) + g f_{\beta\gamma}^\alpha G_\mu^\beta(x)G_\nu^\gamma(x) ;$$

SU(3) structure constants      self coupling

# SU(3) Group Representation

color states       $r = \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}$        $g = \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix}$        $b = \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix}$

8 generators ( $N^*N-1$ )

$$t_1 = \begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \quad t_2 = \begin{pmatrix} 0 & -i & 0 \\ i & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \quad t_3 = \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

$$t_4 = \begin{pmatrix} 0 & 0 & 1 \\ 0 & 0 & 0 \\ 1 & 0 & 0 \end{pmatrix} \quad t_5 = \begin{pmatrix} 0 & 0 & -i \\ 0 & 0 & 0 \\ i & 0 & 0 \end{pmatrix} \quad t_6 = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix}$$

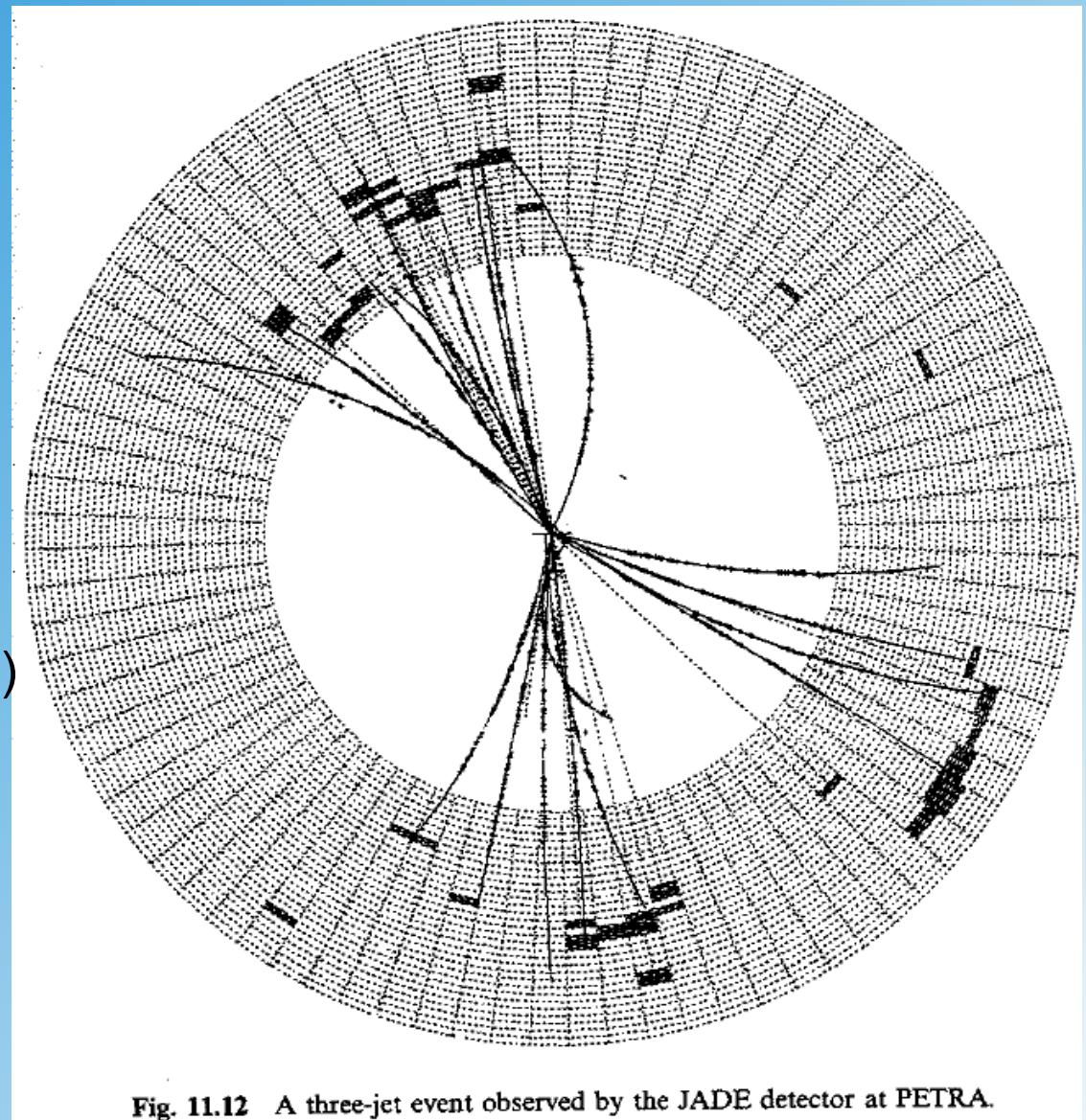
$$t_7 = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & -i \\ 0 & i & 0 \end{pmatrix} \quad t_8 = \frac{1}{\sqrt{3}} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -2 \end{pmatrix}$$

# Three-Jet Event at PETRA

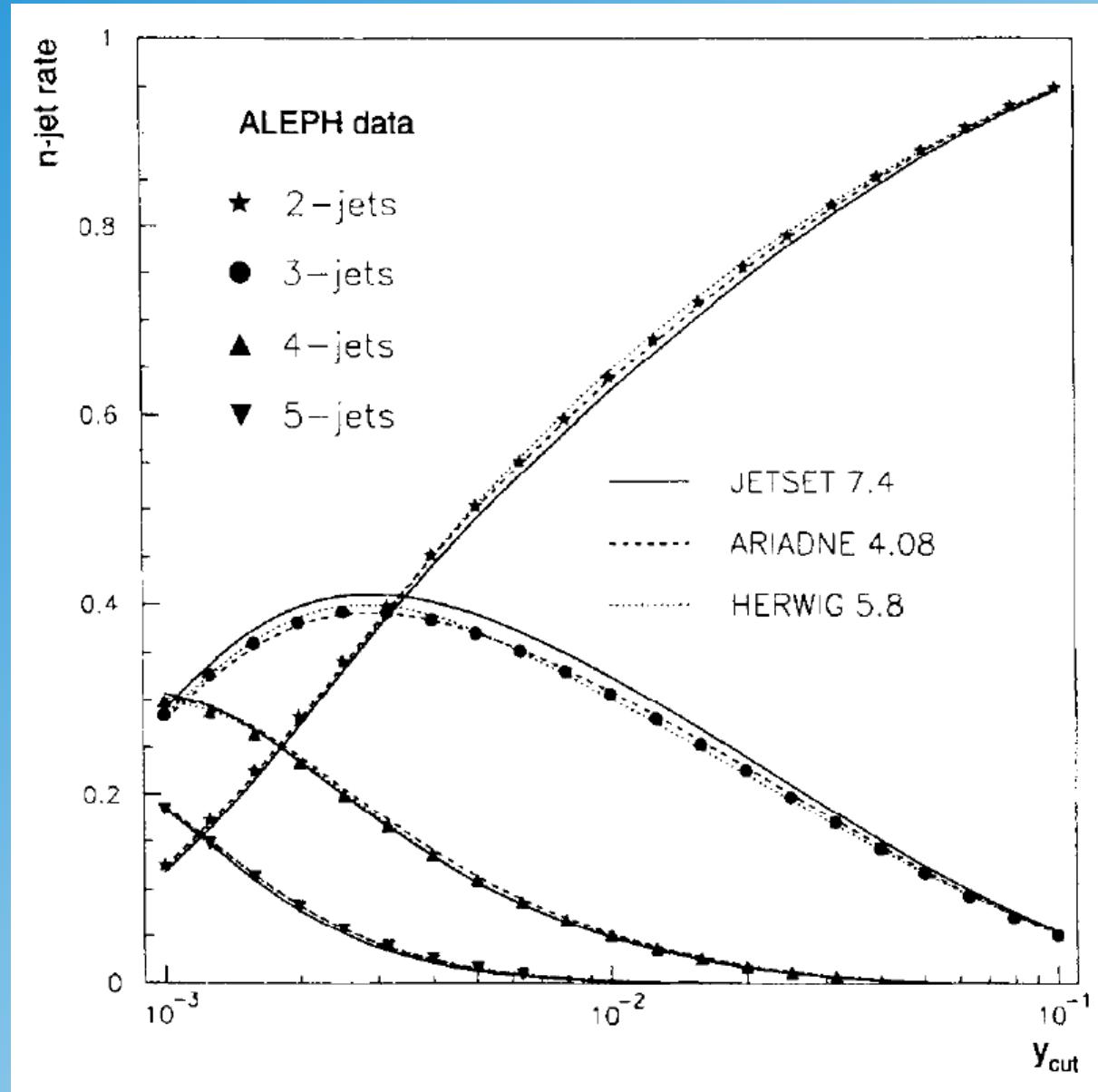
Reaction:

$$e^+ e^- \rightarrow q \bar{q} g$$

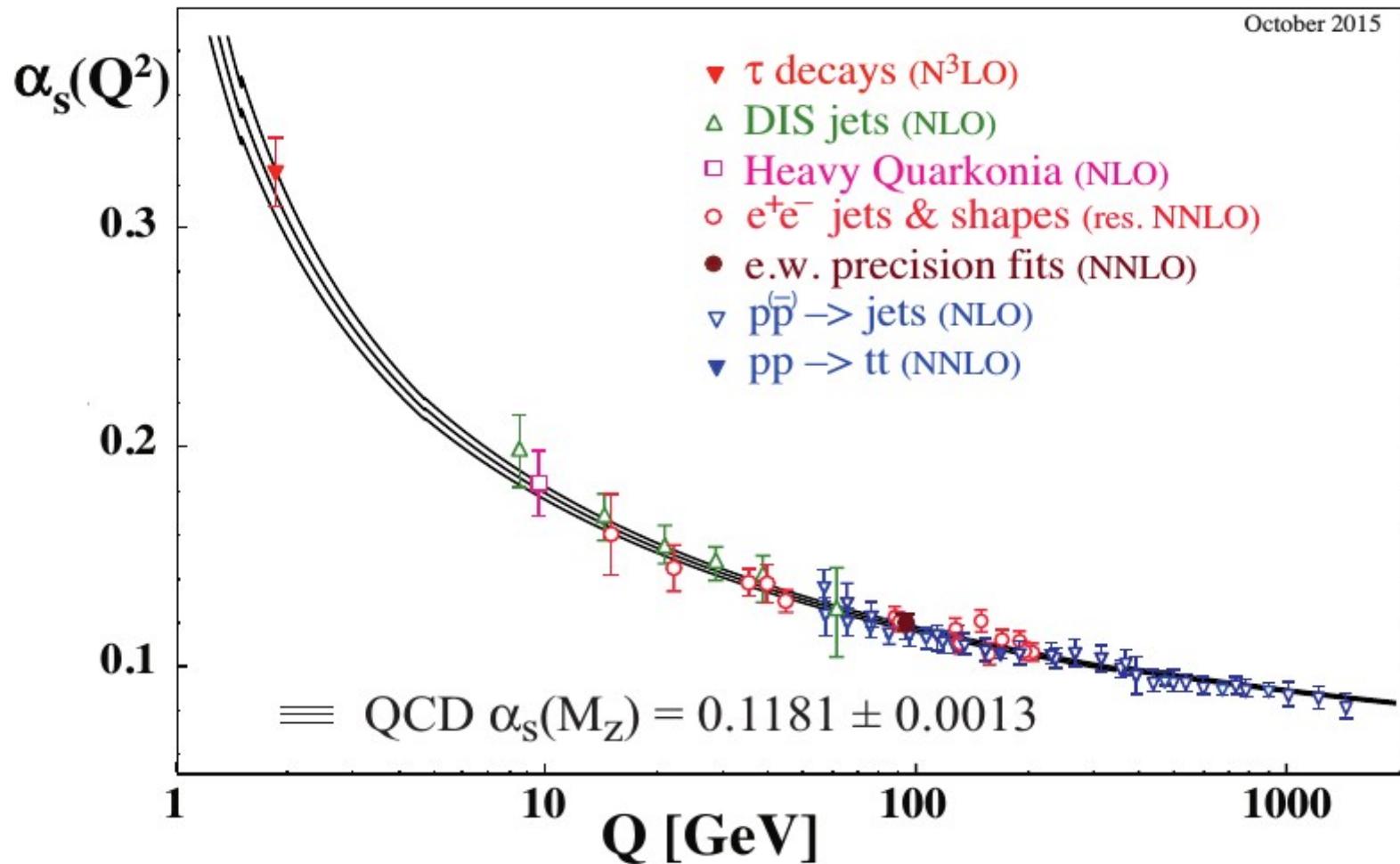
- Hard gluon emission
  - calculable in pQCD
  - event topology
- Soft gluon emissions
  - parton showers (non-pQCD)
  - high particle multiplicities
  - collinear emissions
  - makes “jet” structure
- Hadronisation
  - long distance scale
  - formation of hadrons from quarks and gluons



# Jet Rates (ALEPH)

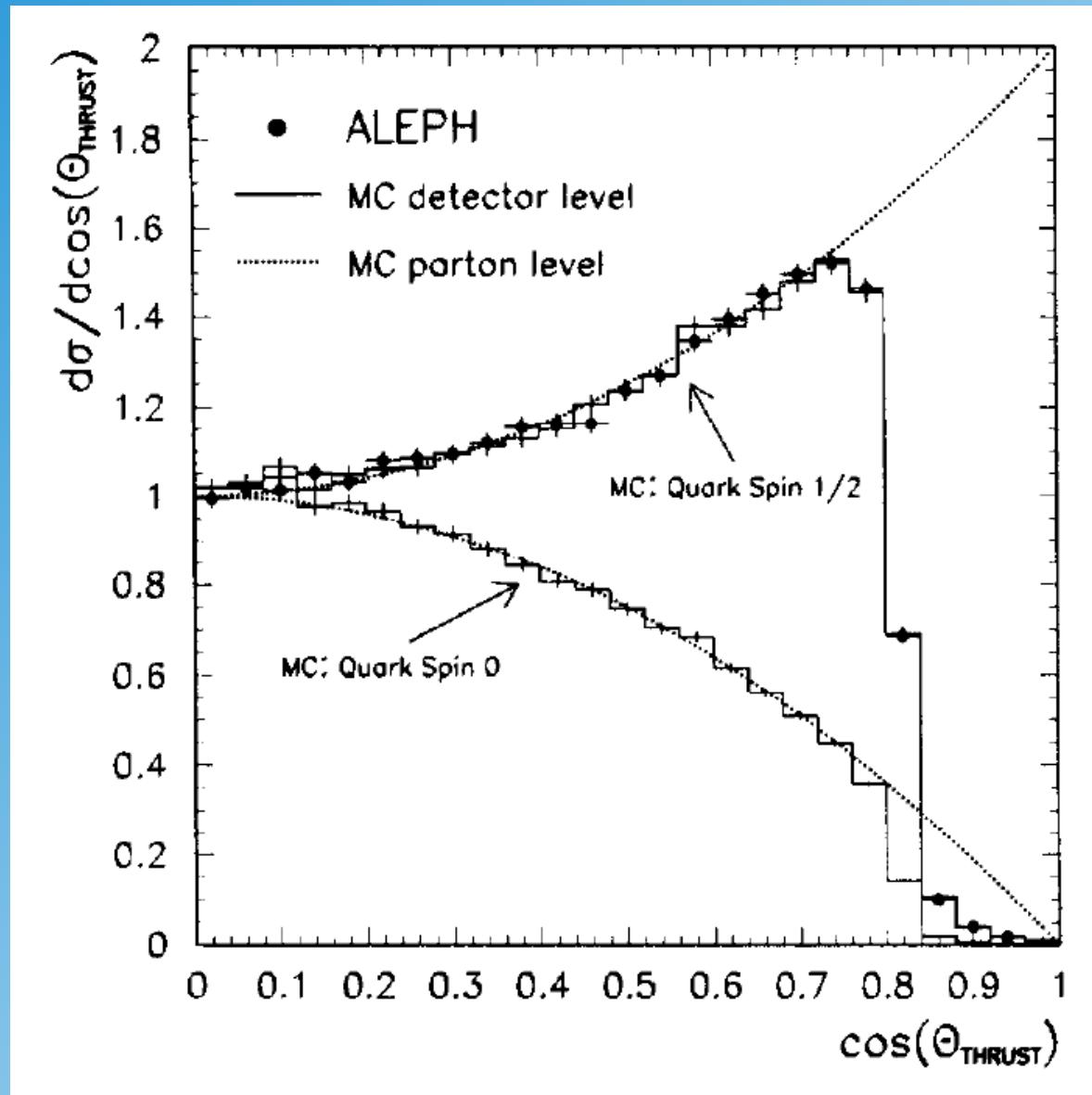


# Running alpha<sub>s</sub>

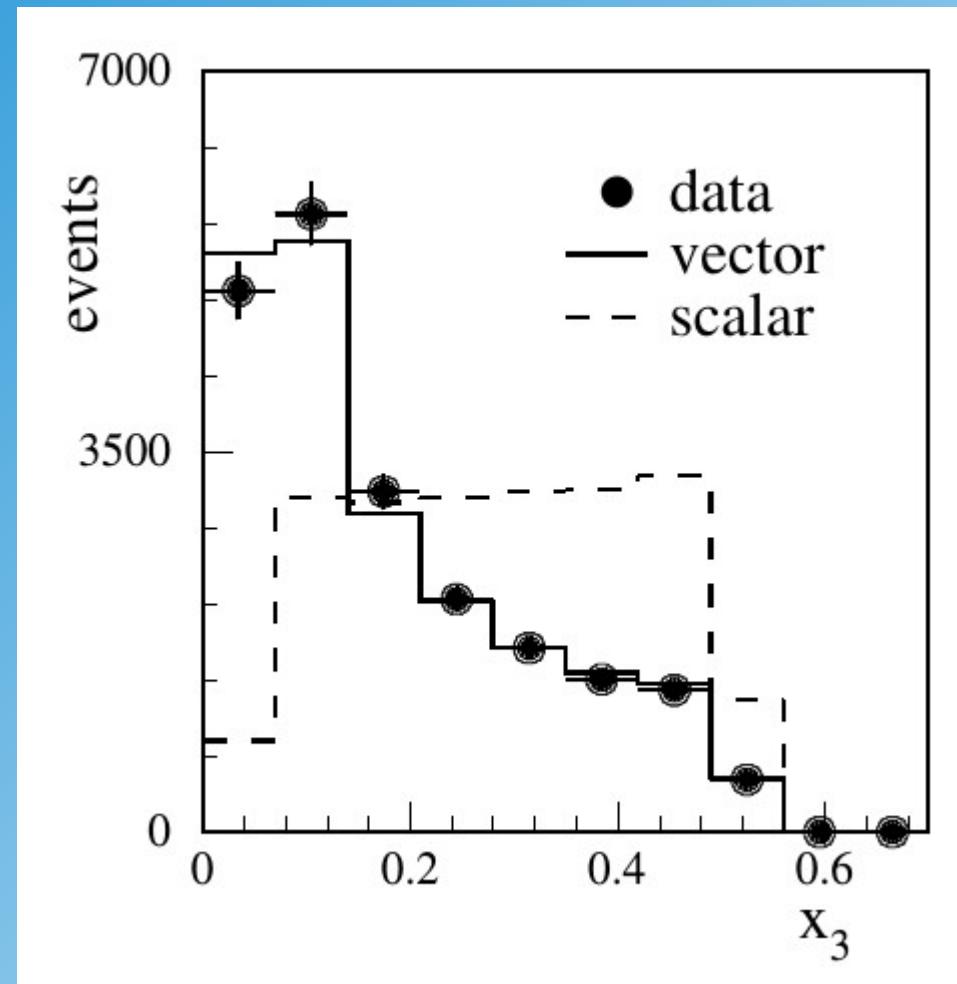


**Figure 9.3:** Summary of measurements of  $\alpha_s$  as a function of the energy scale  $Q$ . The respective degree of QCD perturbation theory used in the extraction of  $\alpha_s$  is indicated in brackets (NLO: next-to-leading order; NNLO: next-to-next-to leading order; res. NNLO: NNLO matched with resummed next-to-leading logs; N<sup>3</sup>LO: next-to-NNLO).

# Quark Spin

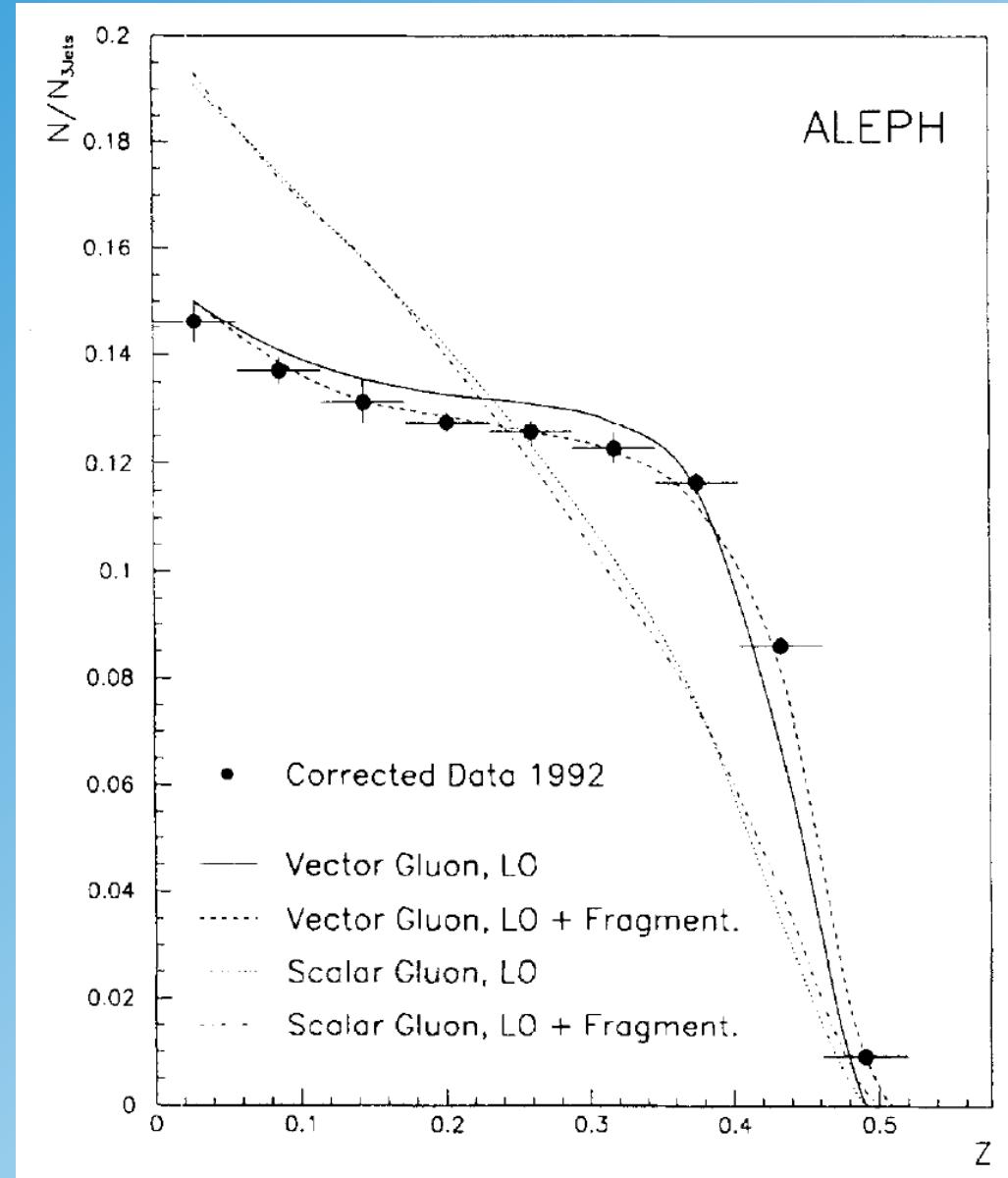


# Gluon Spin



# Fragmentation Effect

$$Z = (x_2 - x_3) / \sqrt{3}$$

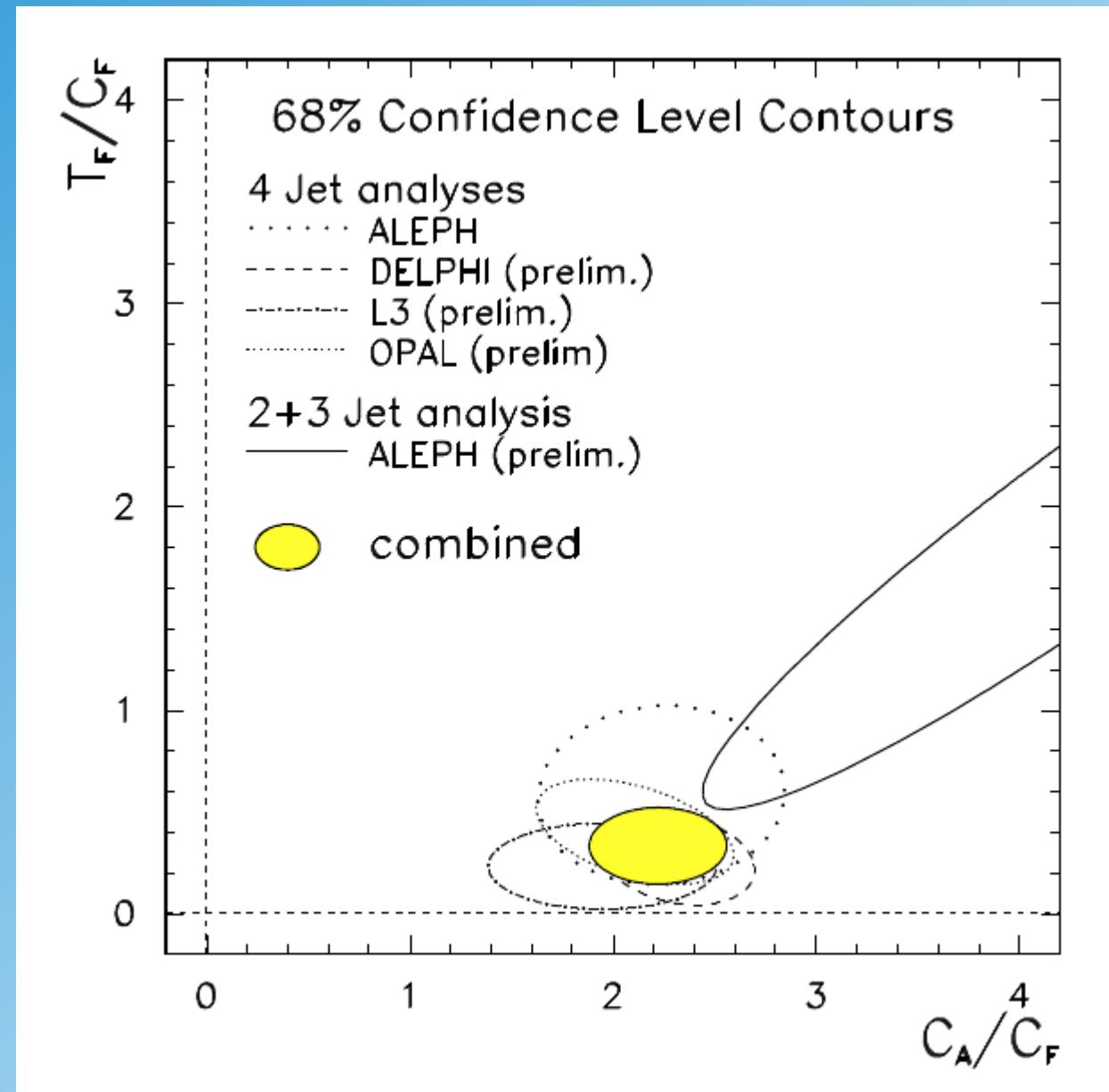
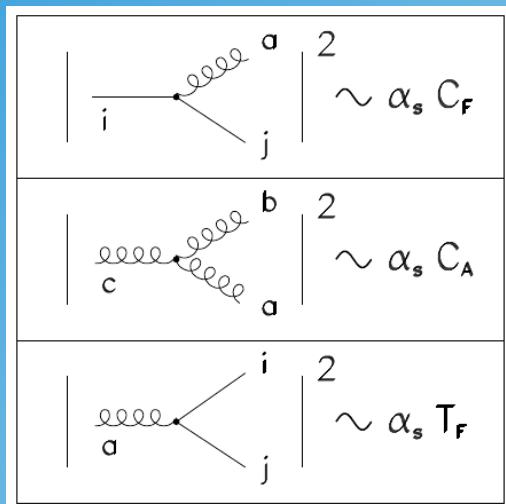


# QCD Color Factors

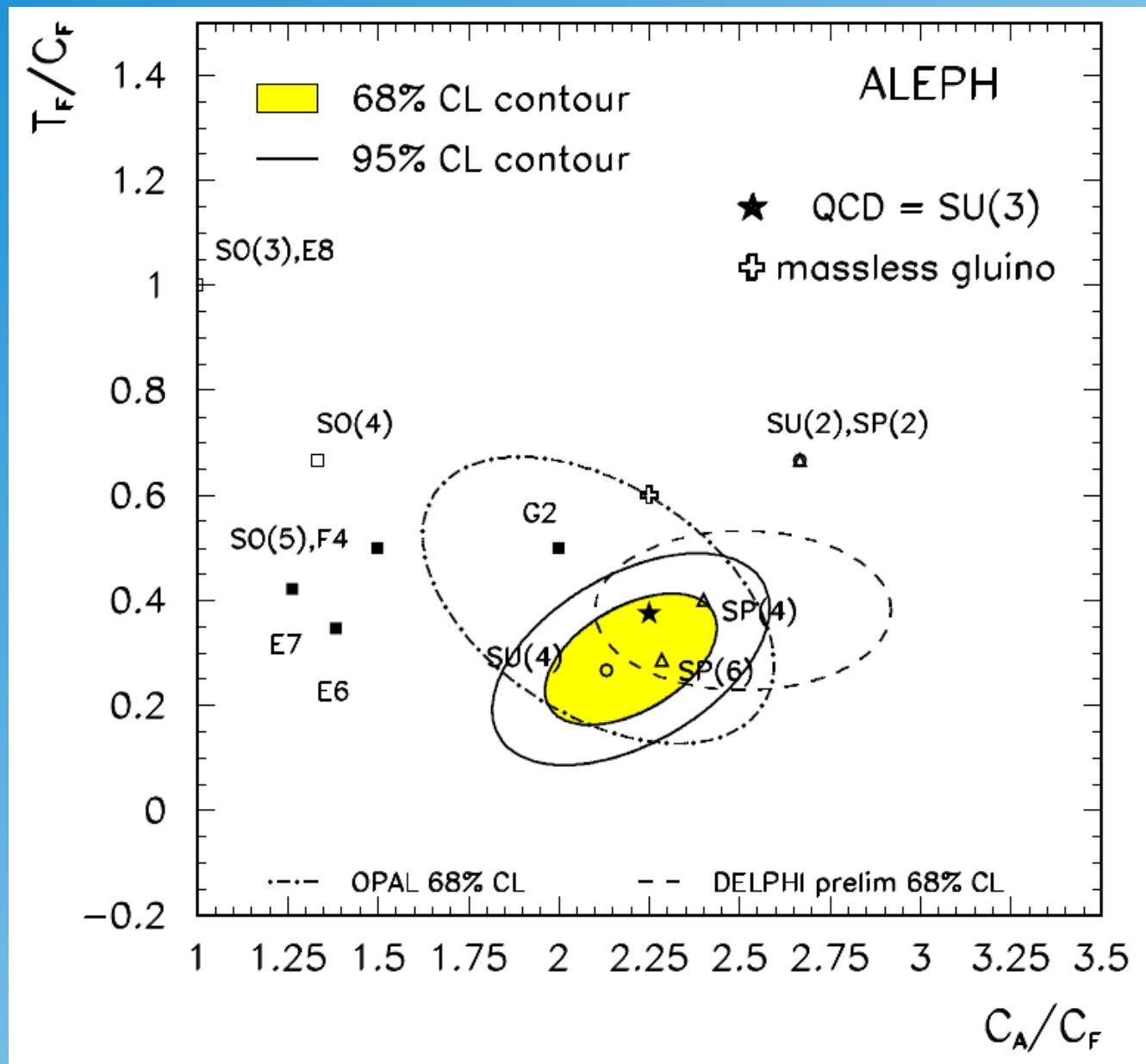
Theory:

$$C_A/C_F = 9/4$$

$$T_F/C_F = 3/8$$

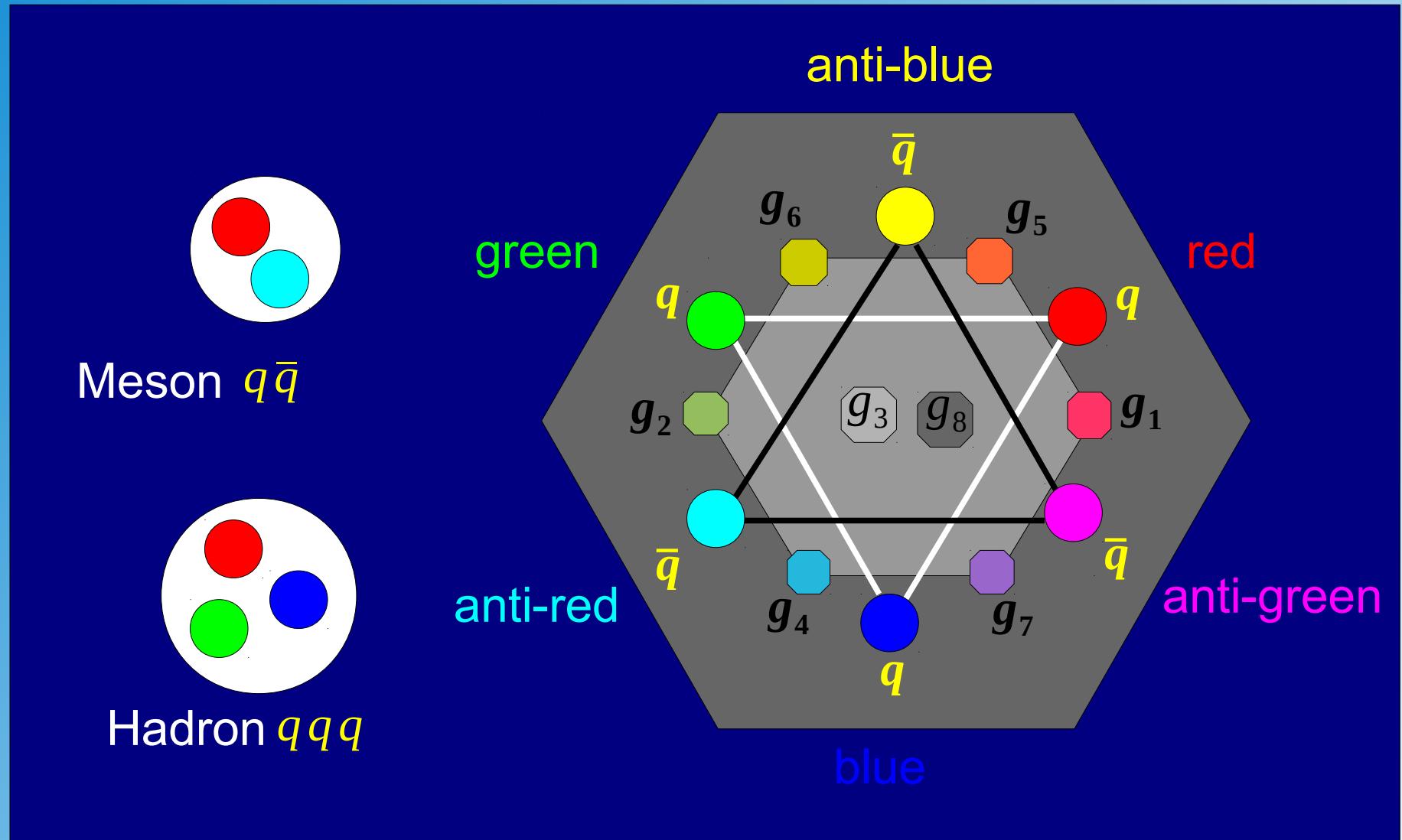


# QCD Color Factors

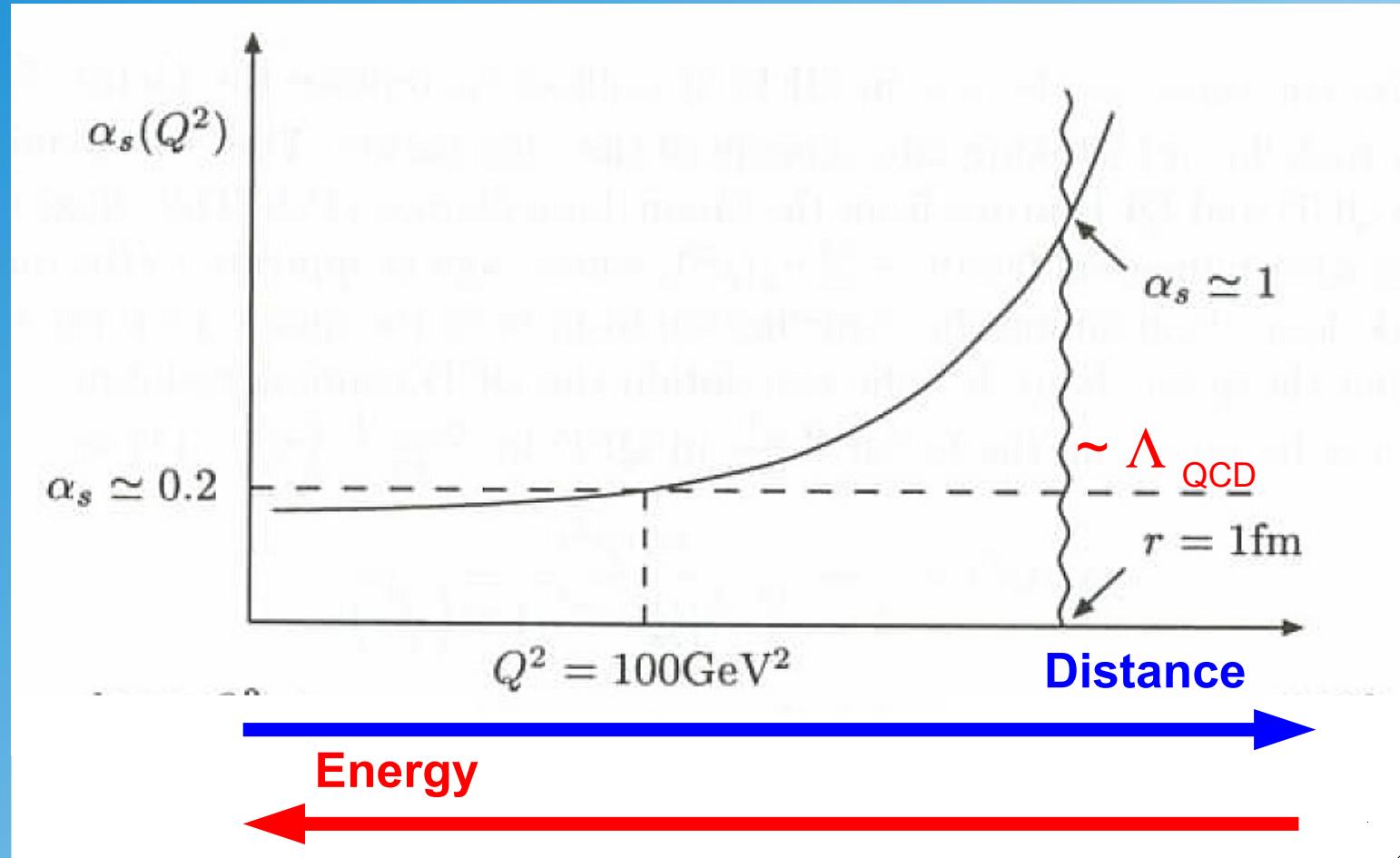


G.Dissertori

# Quantum Chromodynamics

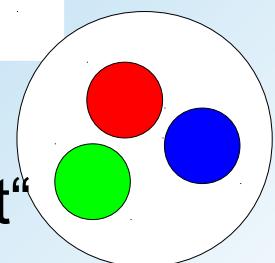


# Running of alpha<sub>s</sub>



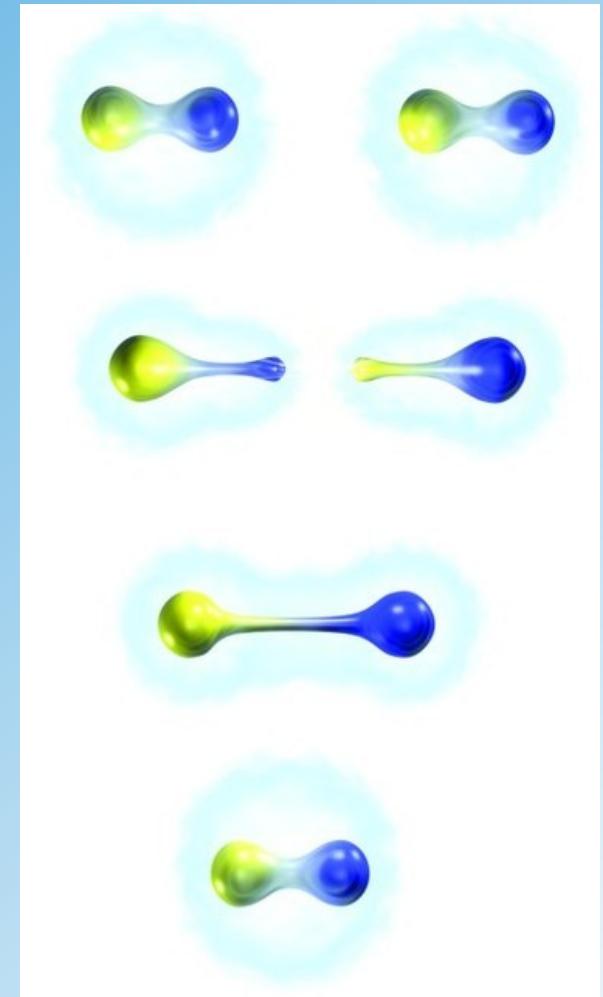
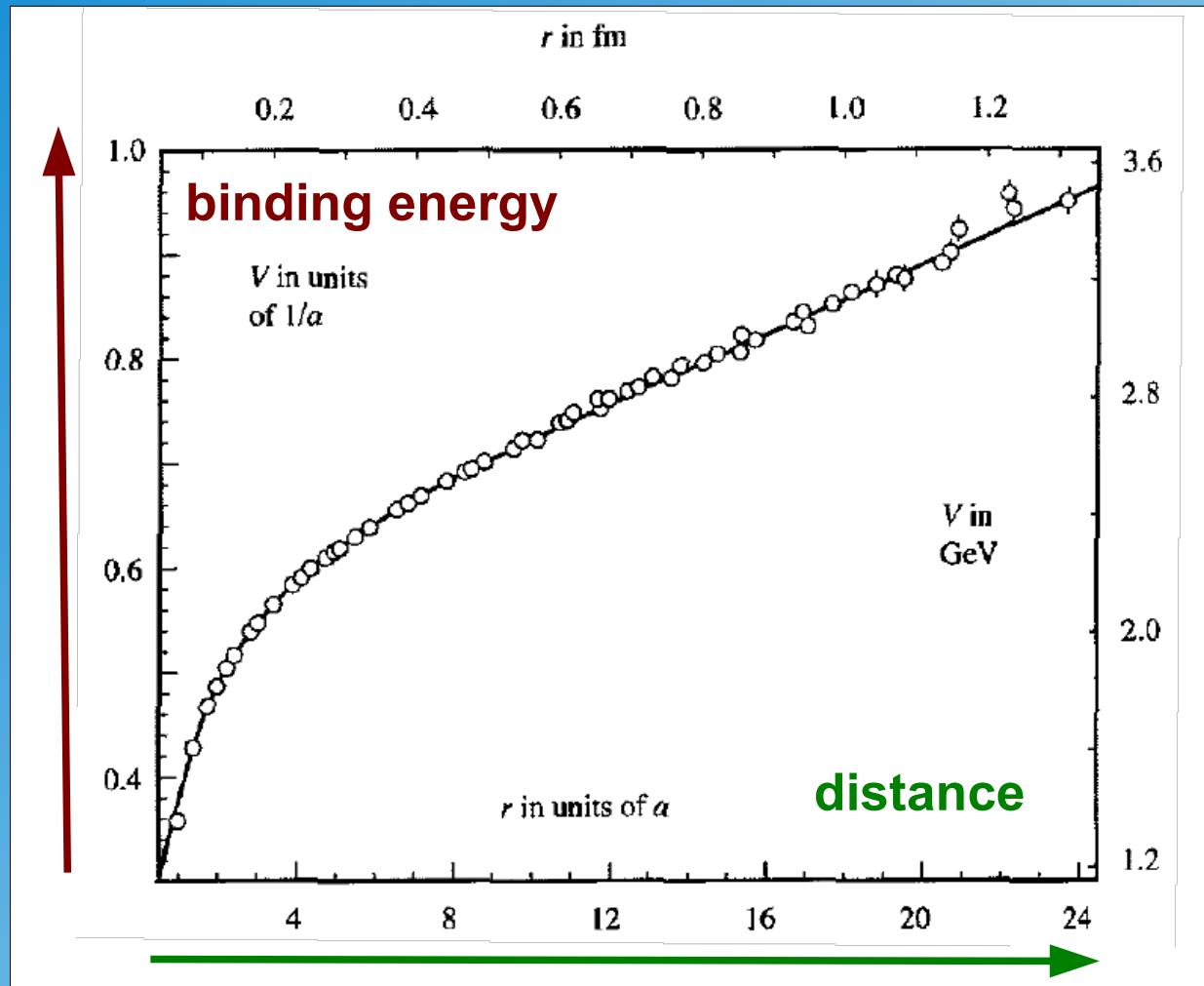
„Asymptotic Freedom“

„Confinement“



# Confinement

The force between two quarks is 50000 N !!!



consequence: free quarks or gluons are not observable

