

## Exercise 7: Signal and Background

N. Berger ([nberger@physi.uni-heidelberg.de](mailto:nberger@physi.uni-heidelberg.de))

21.11.2011

Please send your solutions to [nberger@physi.uni-heidelberg.de](mailto:nberger@physi.uni-heidelberg.de) until 28. 11. 2011, 12:00. Put your answers in an email (subject line *SMIPP:Exercise07*). Test your programs before sending them off...

- 1. Signal and background** Go back to exercise 5.2 and again simulate equal amounts of kaons (Landau distribution with mean 2 and "sigma" 0.4) and pions (1, 0.3) in a five layer energy loss particle identification detector. Form a truncated mean by throwing away the largest measurement each. Now make plots of the efficiency, purity, signal to background ratio, signal to  $\sqrt{\text{background}}$  ratio for both pions and kaons as a function of the cut value. How does this change if only 10% of the particles are kaons? (Attach .cpp and .h or .C or .py files and suitable plots)
- 2. Unbinned Likelihood - Searching for a Resonance** Assume we are studying an invariant mass distribution in some decay channel (e.g. the  $\pi^+\pi^-$  mass in  $J/\psi \rightarrow \gamma\pi^+\pi^-$  or the  $t\bar{t}$  mass in  $pp \rightarrow t\bar{t}X$  or whatever your favourite physics example is. Assume this mass distribution is dominated by a single resonance, which we can describe by a Breit-Wigner distribution (`TRandom3::BreitWigner()`) of mass 2 (GeV/ $c^2$  for the pions, TeV $c^2$  for the tops) and width 0.1 (same units). Generate 100 events (masses  $m_i$ ) according to that distribution. Now construct the log likelihood function

$$\log L = \log \left( \prod_{i=1}^N BW(m_i, M, \Gamma) \right) = \sum_{i=1}^N \log (BW(m_i, M, \Gamma)), \quad (1)$$

where you can use `TMath::BreitWigner()` for the Breit-Wigner function. Assume that you know the width and scan the assumed resonance mass  $M$  and plot  $\log L$  as a function of the mass. The maximum of that curve is your measured value,  $1\sigma$  errors are where your likelihood changes by 0.5 on either side. What is your result?

(Attach .cpp and .h or .C or .py files and suitable plots)

- 3. Unbinned Likelihood - Searching for a Resonance II** Take the example from above, but now add in 2000 equidistributed background events in the mass range from 1 to 3 (units again up to you). Throw away Breit-Wigner events with masses outside that range. Now construct a background-only likelihood function (flat) and a signal + background likelihood function, where you leave the relative normalisation free. Assuming you know mass and width of the resonance, now perform a scan as above in that normalisation parameter. Then compare the  $\log L$  for the background only hypothesis and the (optimal) signal + background

hypothesis.

(Attach .cpp and .h or .C or .py files and suitable plots)

4. **Unbinned Likelihood - Searching for a Resonance III** Again take the example from above and perform a toy MC test of your findings. Perform the experiment 1000 times, generating only background; how often do you find a likelihood ratio ( $\log L$  difference) larger than in 3? Do the same whilst generating the resonance and the background, how often do you find a likelihood ratio smaller than in 3? If you had not generated it yourself, how sure would you be that there is a resonance?

(Attach .cpp and .h or .C or .py files and suitable plots)