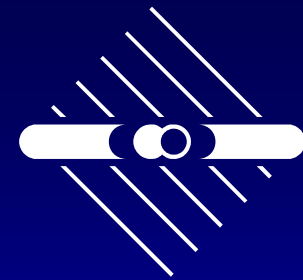
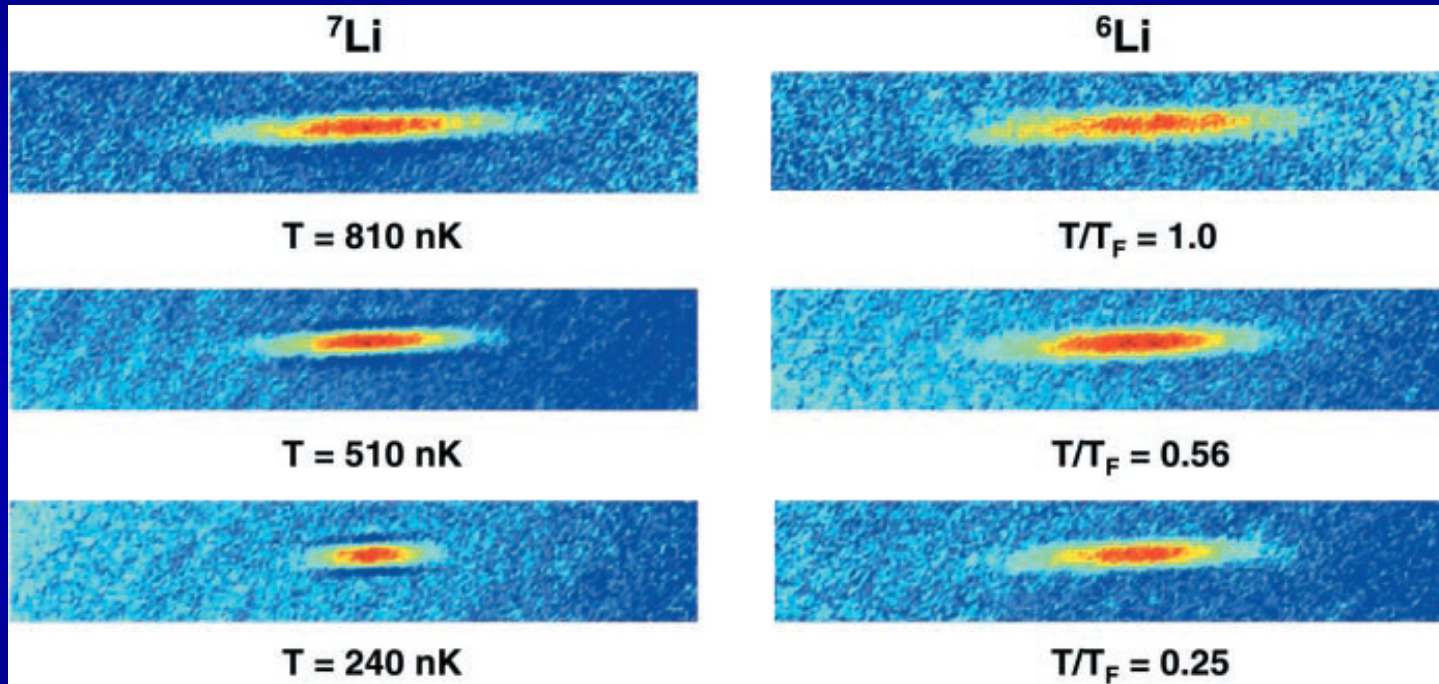


Ultracold degenerate

Fermi gases



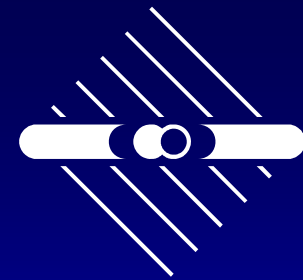
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Selim Jochim

Max-Planck-Institute for Nuclear Physics and
University of Heidelberg

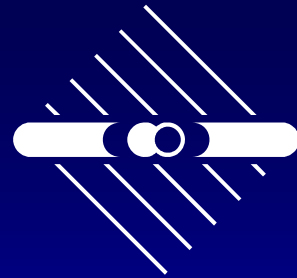
Motivation



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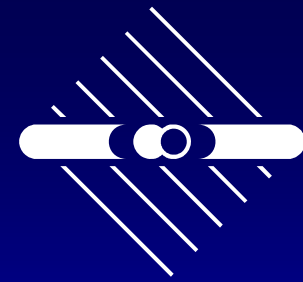
- BEC: drastic effects when degeneracy is reached. Fermi gas: Every state is occupied with one single atom. Could this simply be boring???
- Non-ultracold systems: Superfluidity e.g. in BCS, but at very low temperature.
- Of course now: strongly interacting gases quite successful

Contents



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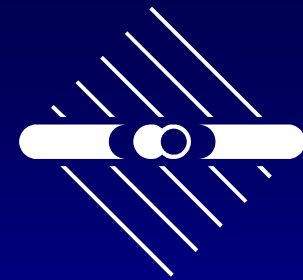
- Properties of degenerate Fermi gas in a harmonic trap
- Experimental realization:
Challenges to prepare, and probe such a gas!
- Hint: How to obtain superfluidity in an ultracold Fermi gas?



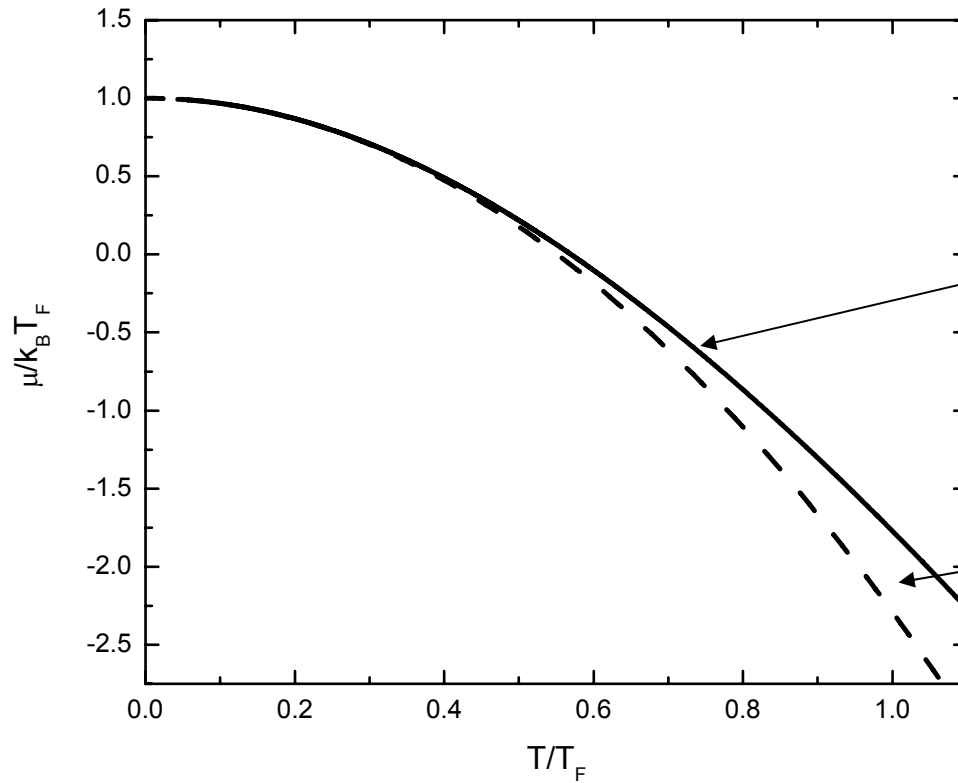
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-
- ...continue on black board ...

Chemical potential of a Fermi Gas



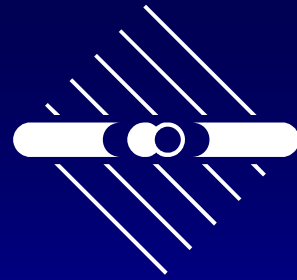
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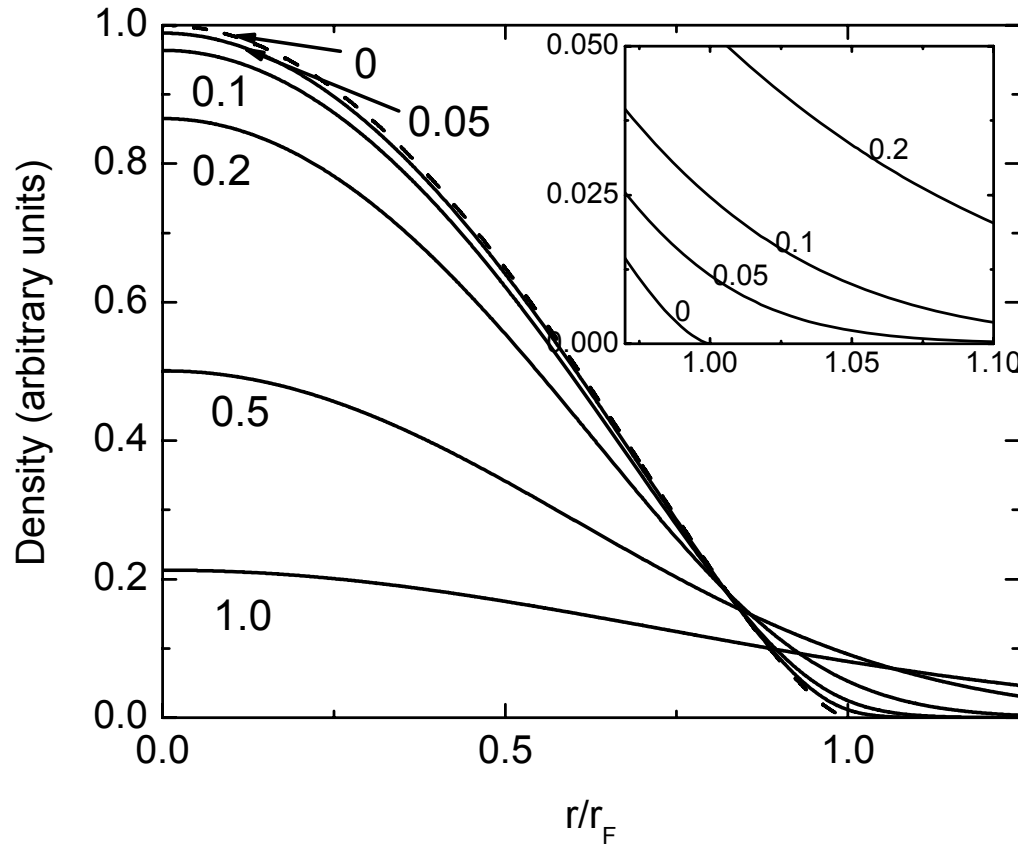
Exact calculation

Sommerfeld approx.

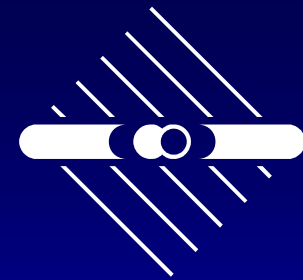
Density distribution



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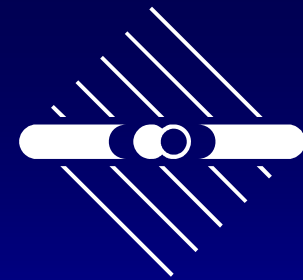
Experiments



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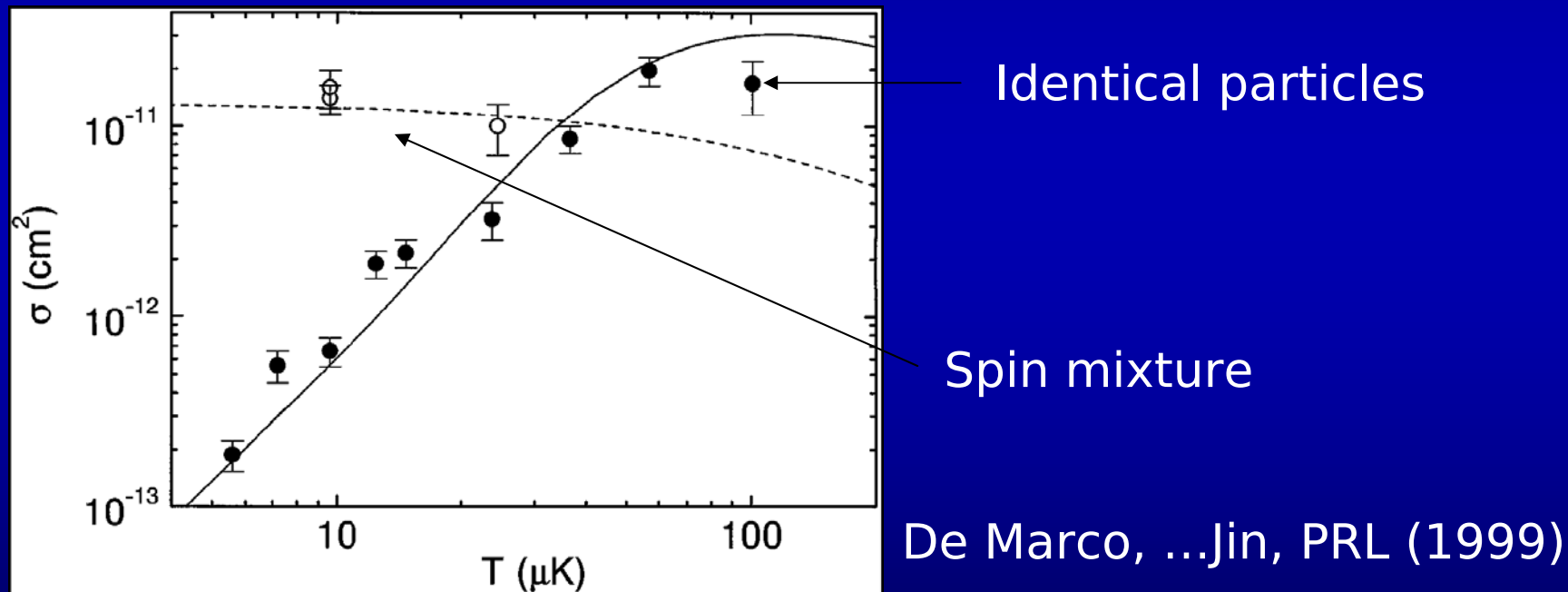
- How to cool a Fermi gas?
- Evaporative cooling always require elastic collisions!
- In BEC: Worry about ratio of good to bad collisions
- Fermi gas: Collisions are suppressed in many ways!

Interactions of identical Fermions



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- Suppression of p-wave collisions:
- At ultracold temperatures: s-wave scattering cross section: $s=0$, p-wave scattering prop. to E^2 .

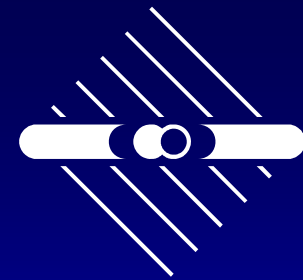


No collisions mean no thermalization, no ev. cooling!
Non-identical particles are required!

Options for evap. Cooling of fermions

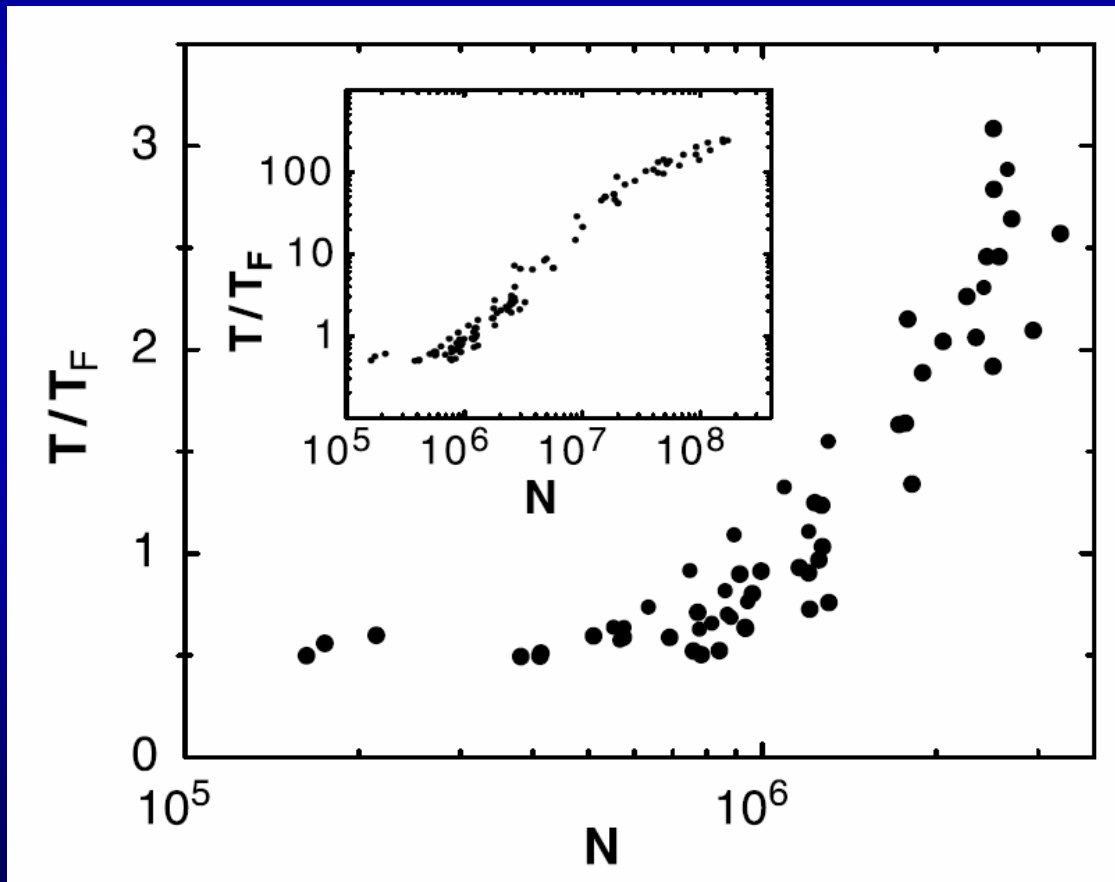
- Use different spin states of the same atoms:
 1. ^{40}K $F=9/2$, $m_F=9/2, m_F=7/2$ (magnetic trapping possible)
 2. ^6Li $F=1/2$, $m_F=\pm 1/2$ (no magnetic trapping!)
- Use bosonic species of the same element as a coolant
Mostly: ^6Li , ^7Li
- Use another (bosonic) atom for cooling
Prime choice: ^6Li , ^{23}Na \rightarrow largest Fermi seas (up to 10^7)

First deg. Fermi gas: 40K



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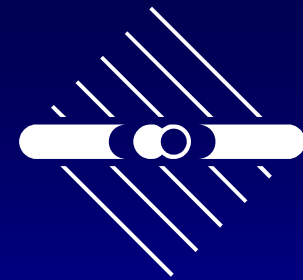
- Evaporative cooling trajectory:



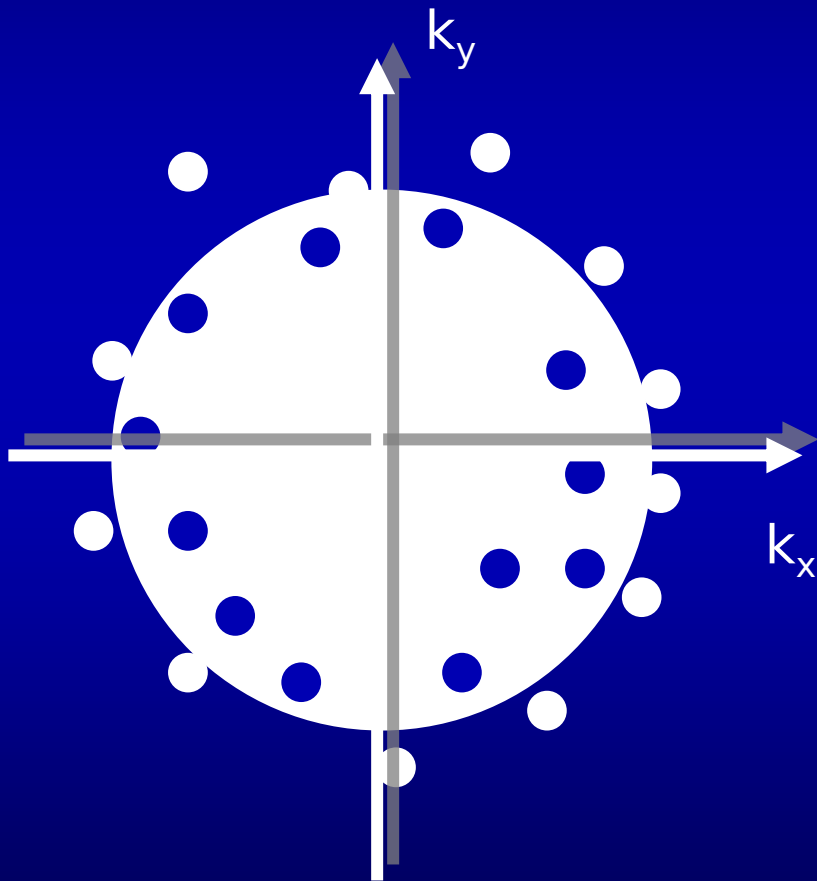
Cooling does not proceed below $T \sim 0.5T_F$ Why?

DeMarco and Jin, Science (1999)

Pauli Blocking

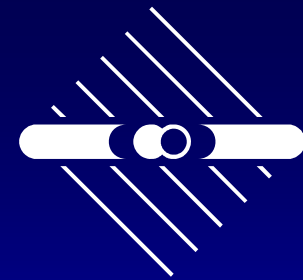


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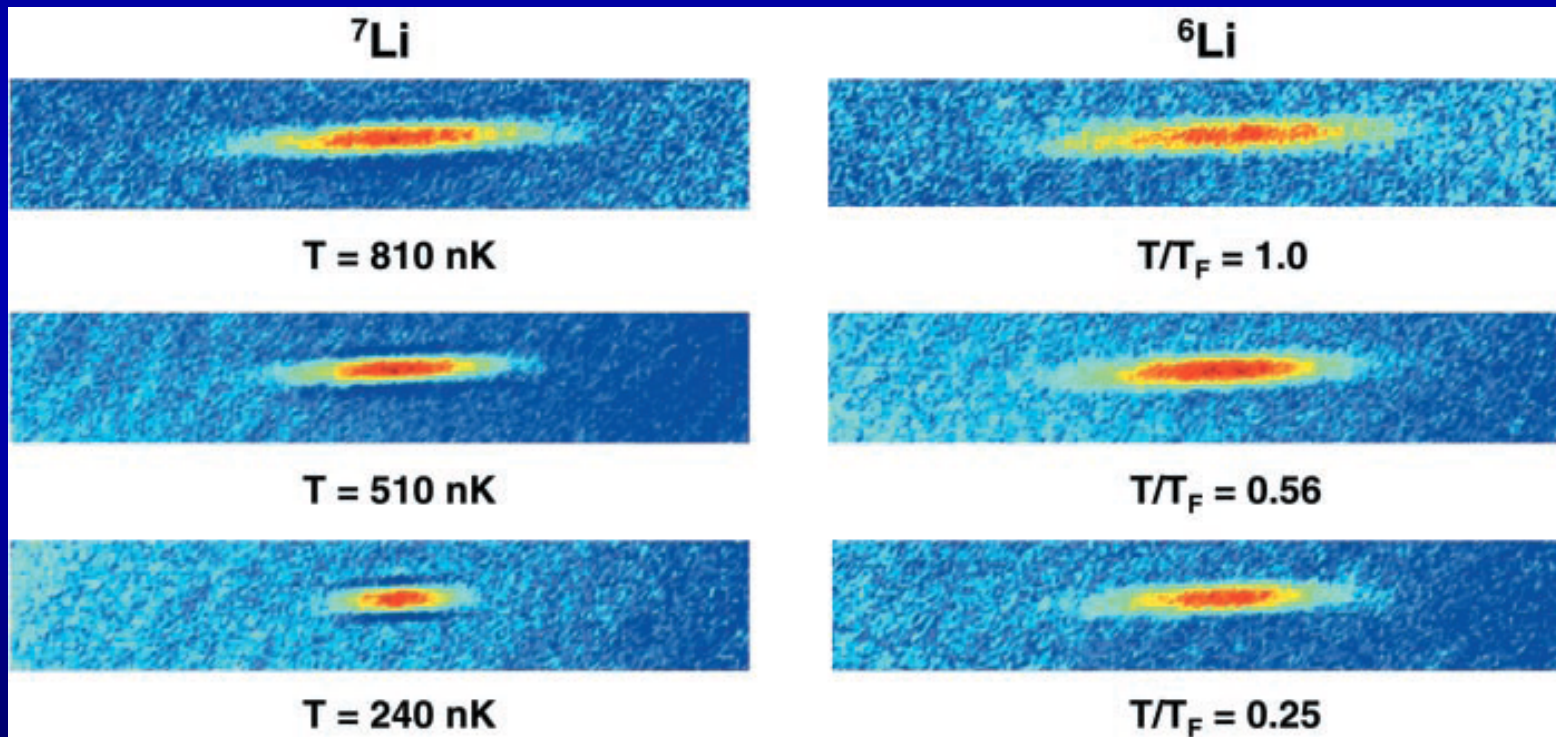
- in every collision that fills one hole, the final state of the collision partner must also be unoccupied.
- All the atoms inside the Fermi sphere cannot undergo collisions
- A Fermi gas at low temperature becomes collisionless!

How overcome Pauli-Blocking?



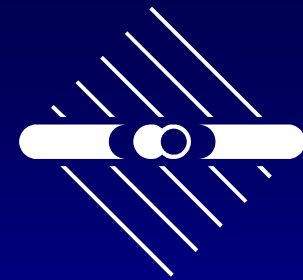
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- Using a boson as a coolant can help quite a bit!



Truscott, ..., and Hulet, *Science* (2001)

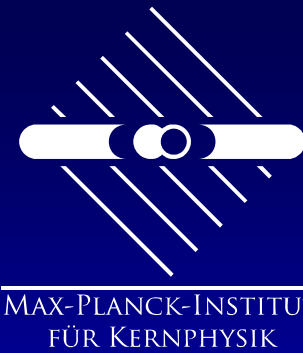
Issues with a second species



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- Need more lasers for laser cooling, plus more complicated atom source
- Often times advisable: Use a different atom instead of isotope: Such as Na
- can produce large reservoirs! (BEC Ketterle ..., NaLi here in HD)

Superfluidity?



- Pairing of weakly attractive fermions leads to a gap:

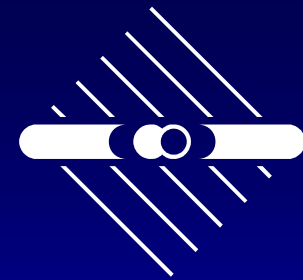
$$\Delta_0 = \frac{1}{2} \left(\frac{2}{e}\right)^{7/3} E_F \exp\left(-\frac{\pi}{2k_F|a|}\right).$$

- And a critical temperature:

$$T_{BCS} = \frac{e\gamma}{\pi} \left(\frac{2}{e}\right)^{7/3} T_F \exp\left(-\frac{\pi}{2k_F|a|}\right) \approx 0.277T_F \exp\left(-\frac{\pi}{2k_F|a|}\right)$$

- In a typical situation, T_{BCS} is extremely small!

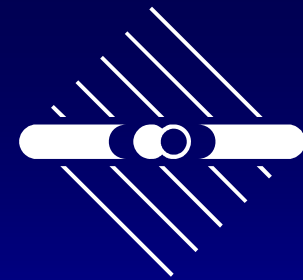
Very low temperatures!



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- Suppose a Fermi gas paired into molecules:
It can be cooled into a BEC,
- Suppose you can convert the BEC of molecules into a Fermi gas of atoms, without changing the entropy, what temperature do you get?
- $2N_{\text{atom}} \rightarrow N_{\text{mol}}$
- Ignore interactions

Very low temperatures!



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- Entropies for BEC and 2-comp. Fermi gas:

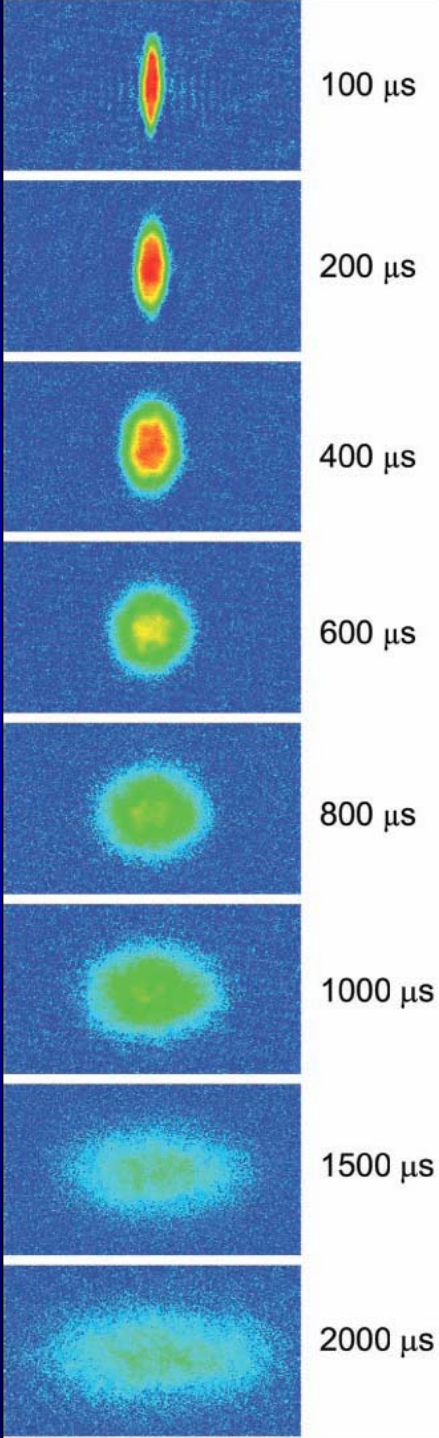
$$S_{BEC} = k_B N_{mol} \frac{2\pi^4}{45\zeta(3)} \left(\frac{T}{T_{BEC}} \right)^3,$$

$$S_{Fermi} = k_B N_{atom} \pi^2 \frac{T}{T_F}$$

$$\rightarrow \frac{T}{T_F} = \frac{\pi^2}{45\zeta(3)} \left(\frac{T}{T_{BEC}} \right)$$

For $T/T_{BEC}=1 \rightarrow T/T_F=0.18$; $T/T_{BEC}=0.25 \rightarrow T/T_F=3 \times 10^{-3}!!!$

Strongly interacting Fermi gases



Lets make a very large $\rightarrow \infty$!

Expansion of a Fermi gas with infinite scattering length

Difficult to interpret: Is the expansion due to the gas being superfluid, or because it is hydrodynamic?

\rightarrow It is both!

O'Hara, ... and Thomas, *Science* (2002)