Flavour-Workshop, Neckarzimmern, 6 April, 2022

Global $b \to s\ell\ell$ fits and `flavio` tutorial

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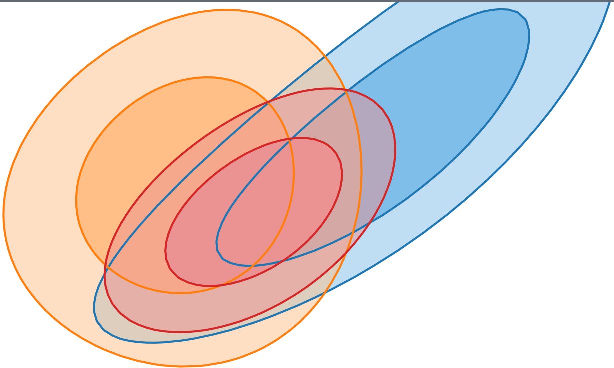

The $b \to s\ell\ell$ anomalies

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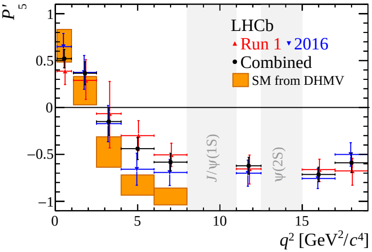
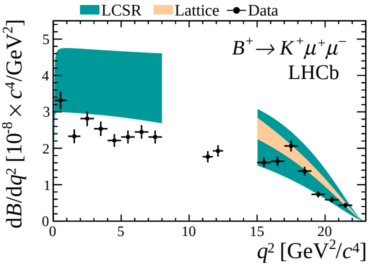
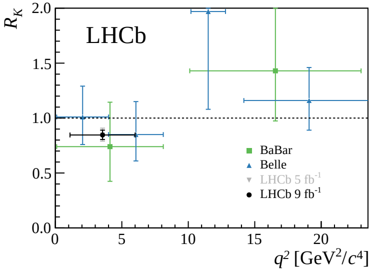
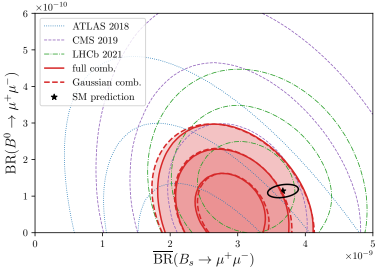








LHCb: arXiv:2003.04831, arXiv:2012.13241, arXiv:1403.8044, arXiv:1506.08777, arXiv:1606.04731, arXiv:2105.14007, arXiv:1705.05802, arXiv:2103.11769, arXiv:2108.09283, arXiv:2108.09284
ATLAS: arXiv:1812.03017, CMS: arXiv:1910.12127, Altmannshofer, PS: arXiv:2103.13370

New physics interpretation

New physics in $b \to s\ell\ell$ in the weak effective theory

- Effective Hamiltonian at scale m_b: $\mathcal{H}_{\text{eff}}^{bs\ell\ell} = \mathcal{H}_{\text{eff, SM}}^{bs\ell\ell} + \mathcal{H}_{\text{eff, NP}}^{bs\ell\ell}$

$$\mathcal{H}_{\text{eff, NP}}^{bs\ell\ell} = -\mathcal{N} \sum_{\ell=e,\mu} \sum_{i=9,10,S,P} \left(C_i^{bs\ell\ell} O_i^{bs\ell\ell} + C_i'^{bs\ell\ell} O_i'^{bs\ell\ell} \right) + \text{h.c.}$$

- Operators considered here ($\ell = e, \mu$)

$$O_9^{(\prime)bs\ell\ell} = (\bar{s}\gamma_\mu P_{L(R)} b)(\bar{\ell}\gamma^\mu \ell) ,$$
$$O_{10}^{(\prime)bs\ell\ell} = (\bar{s}\gamma_\mu P_{L(R)} b)(\bar{\ell}\gamma^\mu \gamma_5 \ell) .$$

- Not considered here
  - Scalar operators: can only reduce tension in $B_s \to \mu\mu$
  - Dipole operators: strongly constrained by radiative decays

    e.g. Paul, Straub, arXiv:1608.02556
  - Four quark operators: dominant effect from RG running above m_B

    Jäger, Leslie, Kirk, Lenz, arXiv:1701.09183

Setup

- Compare theory predictions to experimental data using likelihood function constructed with **flavio** Python package (more on this later)

- Quantify agreement between theory and experiment by likelihood L, $\Delta\chi^2$, and pull

$$\text{pull}_{\text{1D}} = 1\sigma \cdot \sqrt{\Delta\chi^2}\,, \qquad \text{where } -\frac{1}{2}\Delta\chi^2 = \ln L(\vec{0}) - \ln L(\vec{C}_{\text{best fit}})\,.$$

$$\text{pull}_{\text{2D}} = 1\sigma, 2\sigma, 3\sigma, ... \quad \text{for} \quad \Delta\chi^2 \approx 2.3, 6.2, 11.8, ...$$

- New physics scenarios in **Weak Effective Theory (WET)** at scale 4.8 GeV

Observables in global $b \to s\ell\ell$ analysis

- Inclusive decays
  - $B \to X_s \ell^+\ell^-$ ($\mathcal{B}$)
- Exclusive leptonic decays
  - $B_{s,d} \to \ell^+\ell^-$ ($\mathcal{B}$)
- Exclusive semileptonic decays
  - $B^{(0,+)} \to K^{(0,+)}\ell^+\ell^-$ ($\mathcal{B}_\mu$, R_K, angular observables)
  - $B^{(0,+)} \to K^{*(0,+)}\ell^+\ell^-$ ($\mathcal{B}_\mu$, $R_{K^{*0}}$, angular observables)
  - $B_s \to \phi\mu^+\mu^-$ ($\mathcal{B}$, angular observables)
  - $\Lambda_b \to \Lambda\mu^+\mu^-$ ($\mathcal{B}$, angular observables)
- Fits include ~ 200 observables $\Rightarrow$ **global** $b \to s\ell\ell$ analysis

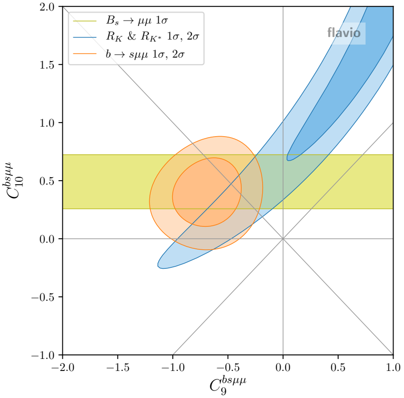
Results

based on Altmannshofer, PS, arXiv:2103.13370 (+ $B_s \to \phi\mu^+\mu^-$ angular observables, LHCb arXiv:2107.13428)
see also similar fits by other groups:
Geng et al., arXiv:2103.12738 Algueró et al., arXiv:2104.08921 Hurth et al., arXiv:2104.10058
Ciuchini et al., arXiv:2110.10126 Alok et al., arXiv:1903.09617, Datta et al., arXiv:1903.10086,
Kowalska et al., arXiv:1903.10932, D'Amico et al., arXiv:1704.05438, Hiller et al., arXiv:1704.05444, ...

Scenarios with a single Wilson coefficients

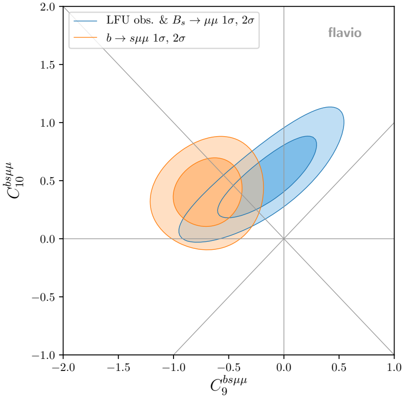
Wilson coefficient	$b \to s\mu\mu$ best fit	pull	LFU, $B_s \to \mu\mu$ best fit	pull	all rare B decays best fit	pull
$C_9^{bs\mu\mu}$	$-0.70^{+0.21}_{-0.22}$	**3.3σ**	$-0.74^{+0.20}_{-0.21}$	4.1σ	$-0.71^{+0.15}_{-0.15}$	**5.1σ**
$C_{10}^{bs\mu\mu}$	$+0.45^{+0.22}_{-0.23}$	1.9σ	$+0.60^{+0.14}_{-0.14}$	**4.7σ**	$+0.54^{+0.12}_{-0.12}$	4.8σ
$C_9^{\prime bs\mu\mu}$	$+0.15^{+0.24}_{-0.24}$	0.6σ	$-0.32^{+0.16}_{-0.17}$	2.0σ	$-0.19^{+0.13}_{-0.13}$	1.5σ
$C_{10}^{\prime bs\mu\mu}$	$-0.09^{+0.15}_{-0.15}$	0.6σ	$+0.07^{+0.11}_{-0.13}$	0.5σ	$+0.04^{+0.10}_{-0.09}$	0.4σ
$C_9^{bs\mu\mu} = C_{10}^{bs\mu\mu}$	$-0.16^{+0.14}_{-0.14}$	1.1σ	$+0.43^{+0.18}_{-0.18}$	2.4σ	$+0.05^{+0.11}_{-0.11}$	0.5σ
$C_9^{bs\mu\mu} = -C_{10}^{bs\mu\mu}$	$-0.55^{+0.13}_{-0.13}$	**3.8σ**	$-0.35^{+0.08}_{-0.08}$	**4.6σ**	$-0.39^{+0.07}_{-0.07}$	**5.6σ**
C_9^{bsee}			$+0.74^{+0.20}_{-0.19}$	4.1σ	$+0.75^{+0.20}_{-0.19}$	4.1σ
C_{10}^{bsee}			$-0.67^{+0.17}_{-0.18}$	4.2σ	$-0.66^{+0.17}_{-0.18}$	4.3σ
$C_9^{\prime bsee}$			$+0.36^{+0.18}_{-0.17}$	2.1σ	$+0.40^{+0.19}_{-0.18}$	2.3σ
$C_{10}^{\prime bsee}$			$-0.32^{+0.16}_{-0.16}$	2.1σ	$-0.31^{+0.15}_{-0.16}$	2.1σ
$C_9^{bsee} = C_{10}^{bsee}$			$-1.39^{+0.26}_{-0.26}$	4.0σ	$-1.28^{+0.24}_{-0.23}$	4.1σ
$C_9^{bsee} = -C_{10}^{bsee}$			$+0.37^{+0.10}_{-0.10}$	4.2σ	$+0.37^{+0.10}_{-0.10}$	4.3σ

Scenarios with two Wilson coefficients



WET at 4.8 GeV

Scenarios with two Wilson coefficients



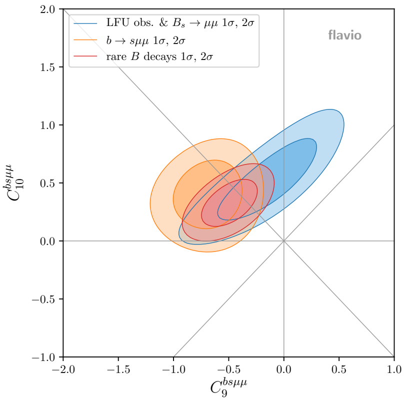
WET at 4.8 GeV

Combination of $B_s \to \mu^+\mu^-$ and LFU observables ($R_K, R_{K^*}, D_{P_{4',5'}}$)

- LFU obs. & $B_s \to \mu\mu$: very clean theory prediction, insensitive to universal $C_9^{\text{univ.}}$
- $b \to s\mu\mu$ sensitive to univ. coeff. possibly afflicted by underestimated hadr. uncert.
- Agreement between $b \to s\mu\mu$ observables and R_K & R_{K^*} could be further improved by **LFU** contribution to $\boldsymbol{C_9^{\text{univ.}}}$

possible connection to $b \to c\ell\nu$ anomalies
see backup slides

Scenarios with two Wilson coefficients



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see backup slides

Global fit in $C_9^{bs\mu\mu}$-$C_{10}^{bs\mu\mu}$ plane prefers negative $C_9^{bs\mu\mu} = -C_{10}^{bs\mu\mu}$

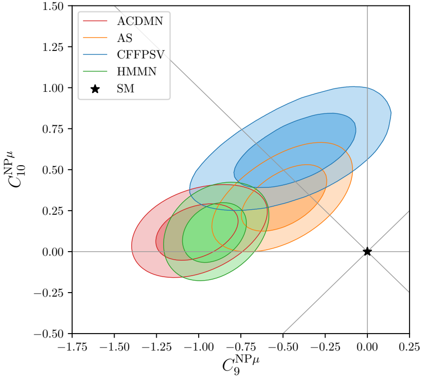
Next: How to construct your own likelihoods with `flavio`

Backup slides

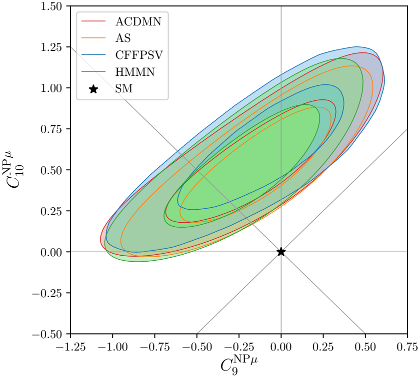
Robustness of global fits

Robustness of global fits

Capdevila, Fedele, Neshatpour, PS



global fit



fit to LFU observables + $B_s \to \mu\mu$

ACDMN (Algueró, Capdevila, Descotes-Genon, Matias, Novoa-Brunet), arXiv:2104.08921
AS (Altmannshofer, PS), arXiv:2103.13370
CFFPSV (Ciuchini, Fedele, Franco, Paul, Silvestrini, Valli), arXiv:2011.01212
HMMN (Hurth, Mahmoudi, Martínez-Santos, Neshatpour), arXiv:2104.10058

Theoretical Framework

$b \to s\ell\ell$ in the weak effective theory

- Effective Hamiltonian at scale m_b: $\mathcal{H}_{\text{eff}}^{bs\ell\ell} = \mathcal{H}_{\text{eff, sl}}^{bs\ell\ell} + \mathcal{H}_{\text{eff, had}}^{bs\ell\ell}$
- **Semileptonic operators**: ($\mathcal{N} = \frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \frac{e^2}{16\pi^2} \approx (34\text{ TeV})^{-2}$)

$$\mathcal{H}_{\text{eff, sl}}^{bs\ell\ell} = -\mathcal{N}\left(C_7^{bs} O_7^{bs} + C_7^{\prime bs} O_7^{\prime bs} + \sum_\ell \sum_{i=9,10,S,P} \left(C_i^{bs\ell\ell} O_i^{bs\ell\ell} + C_i^{\prime bs\ell\ell} O_i^{\prime bs\ell\ell} \right) \right) + \text{h.c.}$$

$$\begin{aligned}
O_9^{(\prime)bs\ell\ell} &= (\bar{s}\gamma_\mu P_{L(R)} b)(\bar{\ell}\gamma^\mu \ell)\,, & C_9^{\text{SM}} &\approx -4.1\\
O_{10}^{(\prime)bs\ell\ell} &= (\bar{s}\gamma_\mu P_{L(R)} b)(\bar{\ell}\gamma^\mu \gamma_5 \ell)\,, & C_{10}^{\text{SM}} &\approx +4.2\\
O_7^{(\prime)bs} &= \frac{m_b}{e}(\bar{s}\sigma_{\mu\nu} P_{R(L)} b)\, F^{\mu\nu}\,, & C_7^{\text{SM}} &\approx -0.3\\
O_S^{(\prime)bs\ell\ell} &= m_b(\bar{s} P_{R(L)} b)(\bar{\ell}\ell)\,, & &\\
O_P^{(\prime)bs\ell\ell} &= m_b(\bar{s} P_{R(L)} b)(\bar{\ell}\gamma_5\ell)\,. & &
\end{aligned}$$

- **Hadronic operators**:

$$\mathcal{H}_{\text{eff, had}}^{bs\ell\ell} = -\mathcal{N}\frac{16\pi^2}{e^2}\left(C_8^{bs} O_8^{bs} + C_8^{\prime bs} O_8^{\prime bs} + \sum_{i=1..6} C_i^{bs\ell\ell} O_i^{bs} \right) + \text{h.c.}$$

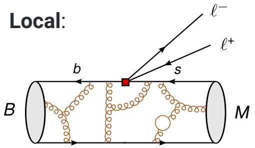
$$\text{e.g.}\quad O_1^{bs} = (\bar{s}\gamma_\mu P_L T^a c)(\bar{c}\gamma^\mu P_L T^a b)\,,\quad O_2^{bs} = (\bar{s}\gamma_\mu P_L c)(\bar{c}\gamma^\mu P_L b)\,.$$

Theory of $B \to M\ell\ell$ decays ($M = K, K^*, \phi$)

$$\mathcal{M}(B \to M\ell\ell) = \langle M\ell\ell|\mathcal{H}_{\text{eff}}^{bs\ell\ell}|B\rangle$$

$$= \mathcal{N}\Big[\left(\mathcal{A}_V^\mu + \mathcal{H}^\mu\right)\bar{u}_\ell\gamma_\mu v_\ell + \mathcal{A}_A^\mu\,\bar{u}_\ell\gamma_\mu\gamma_5 v_\ell + \mathcal{A}_S\,\bar{u}_\ell v_\ell + \mathcal{A}_P\,\bar{u}_\ell\gamma_5 v_\ell\Big]$$

Local:

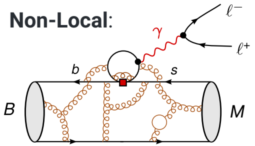


$$\mathcal{A}_V^\mu = -\frac{2im_b}{q^2}C_7\langle M|\bar{s}\,\sigma^{\mu\nu}q_\nu\,P_R\,b|B\rangle + C_9\langle M|\bar{s}\,\gamma^\mu\,P_L\,b|B\rangle$$
$$+ (P_L \leftrightarrow P_R, C_i \to C_i')$$

$$\mathcal{A}_A^\mu = C_{10}\langle M|\bar{s}\,\gamma^\mu\,P_L\,b|B\rangle + (P_L \leftrightarrow P_R, C_i \to C_i')$$

$$\mathcal{A}_{S,P} = C_{S,P}\langle M|\bar{s}\,P_R\,b|B\rangle + (P_L \leftrightarrow P_R, C_i \to C_i')$$

Non-Local:

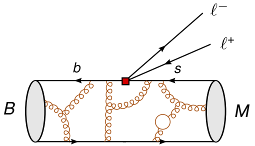


$$\mathcal{H}^\mu = \frac{-16i\pi^2}{q^2}\sum_{i=1..6,8} C_i\int dx^4 e^{iq\cdot x}\langle M|T\{j_{\text{em}}^\mu(x), O_i(0)\}|B\rangle$$

$$j_{\text{em}}^\mu = \sum_q Q_q\,\bar{q}\gamma^\mu q$$

- **Wilson coefficients $C_i = C_i^{\text{SM}} + C_i^{\text{NP}}$**:
  perturbative, short-distance UV physics, parameterize heavy new physics
- **local** and **non-local** **hadronic matrix elements**:
  non-perturbative, **main source of uncertainty**

Local matrix elements

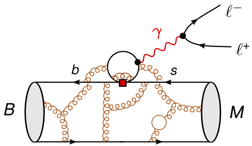


$$\mathcal{A}_V^\mu = -\frac{2im_b}{q^2} C_7 \langle M|\bar{s}\,\sigma^{\mu\nu} q_\nu\, P_R\, b|B\rangle + C_9 \langle M|\bar{s}\,\gamma^\mu\, P_L\, b|B\rangle$$
$$+ (P_L \leftrightarrow P_R, C_i \rightarrow C_i')$$
$$\mathcal{A}_A^\mu = C_{10} \langle M|\bar{s}\,\gamma^\mu\, P_L\, b|B\rangle + (P_L \leftrightarrow P_R, C_i \rightarrow C_i')$$
$$\mathcal{A}_{S,P} = C_{S,P} \langle M|\bar{s}\, P_R\, b|B\rangle + (P_L \leftrightarrow P_R, C_i \rightarrow C_i')$$

- Not all $\langle M|\bar{s}\,\Gamma_i\, b|B\rangle$ matrix elements independent:
  - **3 form factors** for each **spin zero** final state, $M = \boldsymbol{K}$
  - **7 form factors** for each **spin one** final state, $M = \boldsymbol{K^*}, \phi$

- Determination of form factors
  - high q^2: **Lattice QCD**
    HPQCD, arXiv:1306.2384
    Fermilab, MILC, arXiv:1509.06235
    Horgan, Liu, Meinel, Wingate, arXiv:1310.3722, arXiv:1501.00367
  - low q^2: **Continuum methods** (e.g. Light-cone sum rules)
    Bharucha, Straub, Zwicky, arXiv:1503.05534
    Khodjamirian, Mannel, Pivovarov, Wang, arXiv:1006.4945
    Gubernari, Kokulu, van Dyk, arXiv:1811.00983
    Ball, Zwicky, arXiv:hep-ph/0406232
  - low + high q^2: Combined fit **continuum + lattice**
    Bharucha, Straub, Zwicky, arXiv:1503.05534
    Gubernari, Kokulu, van Dyk, arXiv:1811.00983
    Altmannshofer, Straub, arXiv:1411.3161

Non-local matrix elements



$$\mathcal{H}^\mu = \frac{-16i\pi^2}{q^2} \sum_{i=1..6,8} C_i \int dx^4 e^{iq\cdot x} \langle M | T\{j^\mu_{\rm em}(x), O_i(0)\} | B\rangle$$

$$j^\mu_{\rm em} = \sum_q Q_q\, \bar{q}\gamma^\mu q$$

- Contributions for $q^2 < 6$ GeV^2 from QCD factorization (QCDF)
  Beneke, Feldmann, Seidel, arXiv:hep-ph/0106067
- **Beyond-QCDF** contributions **the main source of uncertainty**
- Could mimic new physics in C_9 (but in general q^2 and helicity dependent)
  e.g. Ciuchini, Fedele, Franco, Mishima, Paul, Silvestrini, Valli, arXiv:1512.07157
- Several compatible approaches to treat beyond-QCDF contributions at low q^2
  - Light-Cone Sum Rules estimates — Khodjamirian, Mannel, Pivovarov, Wang, arXiv:1006.4945; Gubernari, van Dyk, Virto, arXiv:2011.09813
  - fit of sum of resonances to data — Blake, Egede, Owen, Pomery, Petridis, arXiv:1709.03921
  - analyticity + experimental data on $b \to sc\bar{c}$ — Bobeth, Chrzaszcz, van Dyk, Virto, arXiv:1707.07305
  - order of magnitude estimate parameterized as polynomial in q^2
    Descotes-Genon, Hofer, Matias, Virto, arXiv:1407.8526, arXiv:1510.04239
    Arbey, Hurth, Mahmoudi, Neshatpour, arXiv:1806.02791
    Altmannshofer, Straub, arXiv:1411.3161

“Cleanliness” of $b \to s\ell\ell$ observables in the SM

	parametric uncertainties	local hadr. matrix elements	non-local hadr. matrix elements
$\mathcal{B}(B \to M\ell\ell)$	✗	✗	✗
angular observables	✓	✗	✗
$\overline{\mathcal{B}}(B_s \to \ell\ell)$	✗	✓	✓ (N/A)
LFU observables	✓	✓	✓

p-value of the SM fit

p-value of the SM fit

p-value of goodness-of-fit from Wilks' theorem

$$p_{SM} = 1 - F(\chi^2_{SM}; n_{obs})$$

with $F(\chi^2; n_{obs})$ the χ^2 CDF and n_{obs} the number of independent observables (measurements of an observable by different experiments counted separately).

- ACDMN (Algueró, Capdevila, Descotes-Genon, Matias, Novoa-Brunet), arXiv:2104.08921

$$\begin{aligned} \textit{Global fit}: \; n_{\rm obs} &= 246 \quad \Rightarrow \quad p = 1.1\% \\ \textit{LFU fit}^*: \; n_{\rm obs} &= 22 \quad \Rightarrow \quad p = 1.4\% \end{aligned}$$

- AS (Altmannshofer, PS), arXiv:2103.13370

$$\begin{aligned} \textit{Global fit}: \; n_{\rm obs} &= 191 \quad \Rightarrow \quad p = 1.2\% \\ \textit{LFU fit}^*: \; n_{\rm obs} &= 21 \quad \Rightarrow \quad p = 0.5\% \end{aligned}$$

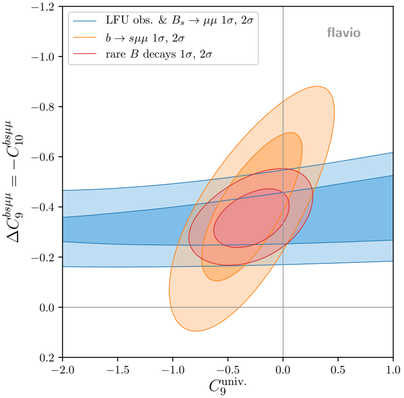
- HMMN (Hurth, Mahmoudi, Martínez-Santos, Neshatpour), arXiv:2104.10058

$$\begin{aligned} \textit{Global fit}: \; n_{\rm obs} &= 173 \quad \Rightarrow \quad p = 0.4\% \\ \textit{LFU fit}^*: \; n_{\rm obs} &= 7 \quad \Rightarrow \quad p = 0.02\% \end{aligned}$$

*LFU fit: all the measured LFU observables + $\mathcal{B}(B_s \to \mu^+\mu^-)$ (all groups)
+ effective $B_s \to \mu\mu$ lifetime + radiative decays + $\mathcal{B}(B_s \to X_s\mu^+\mu^-)$ (depending on the group)

Scenario with universal C_9

Scenarios with two Wilson coefficients



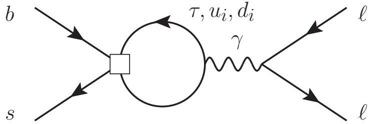
WET at 4.8 GeV

- Perform two-parameter fit in space of $\boldsymbol{C_9^{\text{univ.}}}$ and $\boldsymbol{\Delta C_9^{bs\mu\mu}} = -\boldsymbol{C_{10}^{bs\mu\mu}}$:

$$C_9^{bsee} = C_9^{bs\tau\tau} = C_9^{\text{univ.}}$$
$$C_9^{bs\mu\mu} = C_9^{\text{univ.}} + \Delta C_9^{bs\mu\mu}$$
$$C_{10}^{bsee} = C_{10}^{bs\tau\tau} = 0$$
$$C_{10}^{bs\mu\mu} = -\Delta C_9^{bs\mu\mu}$$

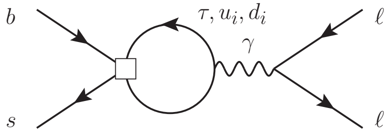
scenario first considered in
Algueró et al., arXiv:1809.08447

- Slight preference for **non-zero $\boldsymbol{C_9^{\text{univ.}}}$**
  - could be mimicked by hadronic effects
  - can arise from RG effects:



Bobeth, Haisch, arXiv:1109.1826
Crivellin, Greub, Müller, Saturnino, arXiv:1807.02068

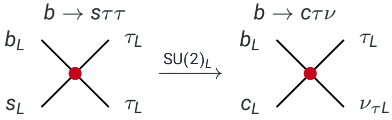
RG effect in SMEFT



RG effects require scale separation

- Consider **SMEFT**

Possible operators:



- $[O_{lq}^{(3)}]_{3323} = (\bar{l}_3 \gamma_\mu \tau^a l_3)(\bar{q}_2 \gamma^\mu \tau^a q_3)$:
  Might also **explain $R_{D^{(*)}}$ anomalies!**
- $[O_{lq}^{(1)}]_{3323} = (\bar{l}_3 \gamma_\mu l_3)(\bar{q}_2 \gamma^\mu q_3)$:
  Strong constraints from $B \to K\nu\nu$ require $[C_{lq}^{(1)}]_{3323} \approx [C_{lq}^{(3)}]_{3323}$

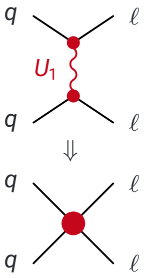
Buras et al., arXiv:1409.4557

- ***U_1* vector leptoquark** $(\mathbf{3}, \mathbf{1})_{2/3}$ couples LH fermions

$$\mathcal{L}_{U_1} \supset g_{lq}^{ji} \left(\bar{q}^i \gamma^\mu l^j \right) U_\mu + \text{h.c.}$$

- Generates **semi-leptonic operators at tree-level**

$$[C_{lq}^{(1)}]_{ijkl} = [C_{lq}^{(3)}]_{ijkl} = -\frac{g_{lq}^{jk}\, g_{lq}^{il*}}{2M_U^2}$$



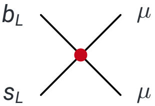
New particles to explain $b \to s\ell\ell$ anomalies

New particles to explain $b \to s\ell\ell$ anomalies

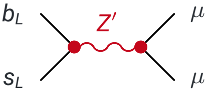
Global fits suggest

$$\boldsymbol{C_9^\mu - C_{10}^\mu \approx -0.7, \qquad 0 \gtrsim \frac{C_{10}^\mu}{C_9^\mu} \gtrsim -1}$$

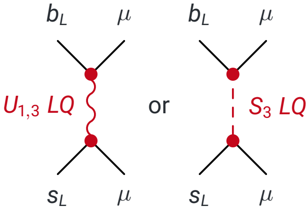
$$O_9^\mu = (\bar{s}\gamma_\mu P_L b)(\bar{\mu}\gamma^\mu \mu)\,, \quad O_{10}^\mu = (\bar{s}\gamma_\mu P_L b)(\bar{\mu}\gamma^\mu \gamma_5 \mu)$$



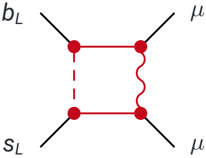
$$\sim \frac{C_9^\mu - C_{10}^\mu}{(34\,\text{TeV})^2}$$



$$\sim \frac{g_{bs}\,g_{\mu\mu}}{m_{Z'}^2}$$

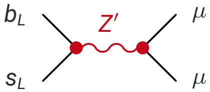


$$\sim \frac{g_{b\mu}\,g_{s\mu}}{m_{LQ}^2}$$

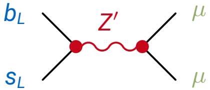


$$\sim \frac{g_b\,g_s\,g_{\mu,1}\,g_{\mu,2}}{16\,\pi^2\,m_{\text{NP}}^2}$$

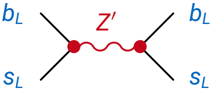
Z'



Z': Constraints from B_s-$\bar{B}_s$ mixing



$\rightarrow$



$$\sim \frac{g_{bs}\, g_{\mu\mu}}{m_{Z'}^2} \sim \frac{1}{(36\,\text{TeV})^2}$$

$$\sim \frac{g_{bs}^2}{m_{Z'}^2} \lesssim \frac{\left|\frac{M_{12}}{M_{12}^{\text{SM}}} - 1\right| \Big/ 10\%}{(244\,\text{TeV})^2}$$

$$\left|\frac{M_{12}}{M_{12}^{\text{SM}}} - 1\right| \approx 10\%$$

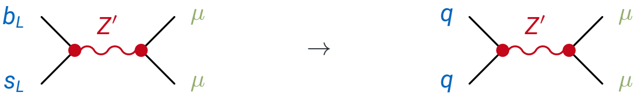
$$\Downarrow$$

$$\frac{g_{\mu\mu}}{m_{Z'}} \gtrsim \frac{1}{5.3\,\text{TeV}}$$

Ways around:

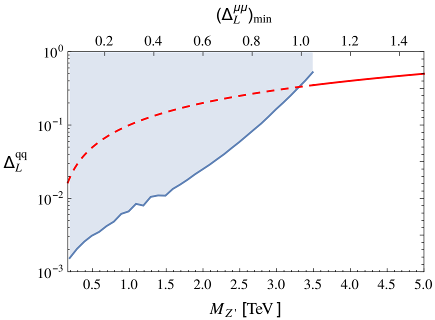
- imaginary part of g_{bs} $\rightarrow$ constraints from *CP* violating observables
- Z' coupling to $(\bar{s}\gamma_\mu P_R b)$ $\rightarrow$ constraint from $R_K \approx R_{K^*}$
- ...

Z': Constraints from $pp \to \mu\mu$

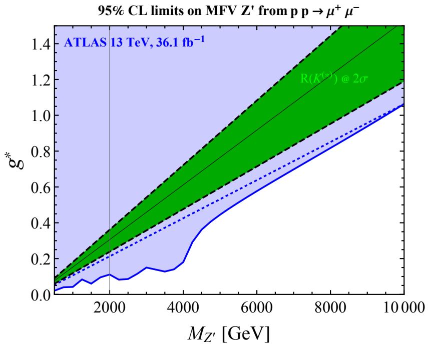


- Direct searches for a Z' resonance
- Searches for quark-lepton contact interactions

Z': Constraints from $pp \to \mu\mu$



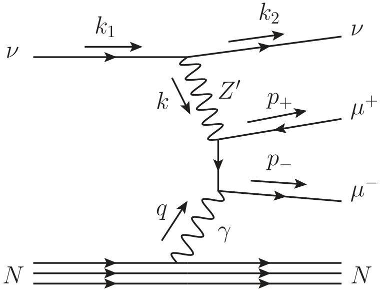
Altmannshofer, Straub, arXiv:1411.3161



Greljo, Marzocca, arXiv:1704.09015

- Couplings to light quarks must be suppressed for $m_{Z'} < 4.5\,\text{TeV}$
- MFV-like Z'-quark couplings already excluded

Z': Constraints from neutrino trident production

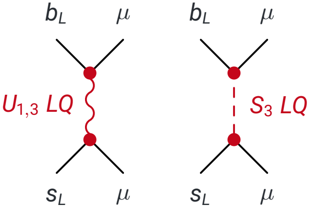


Altmannshofer, Gori, Pospelov, Yavin, arXiv:1406.2332

- $\mu^+\mu^-$ production induced by neutrino in Coulomb field of heavy nucleus
- Cross section with Z' contribution

$$\frac{\sigma}{\sigma_{SM}} \simeq \frac{1 + \left(1 + 4\, s_W^2 + 2\, v^2 \frac{g_{Z'}^2}{m_{Z'}^2}\right)^2}{1 + \left(1 + 4\, s_W^2\right)^2}$$

Leptoquarks



Overview of Leptoquarks

Scenario	Spin	$G_{\rm SM}$	$\mathcal{L}_{\rm int}$
S_1	0	$(\overline{\mathbf{3}},\mathbf{1})_{\frac{1}{3}}$	$\hat\lambda_{\rm L}\,(\overline{q}^{\sf c}_{\rm L}\cdot\epsilon\cdot l_{\rm L})\,\phi\;+\;\hat\lambda_{\rm R}\,\overline{u}^{\sf c}_{\rm R}\ell_{\rm R}\phi\;+\;\hat\lambda^1_{qq}\,(\overline{q}_{\rm L}\cdot\epsilon\cdot q^{\sf c}_{\rm L})\,\phi\;+\;\hat\lambda^2_{qq}\,\overline{d}_{\rm R}u^{\sf c}_{\rm R}\phi$
$\widetilde{S}_1$	0	$(\overline{\mathbf{3}},\mathbf{1})_{\frac{4}{3}}$	$\hat\lambda_{\rm R}\,\overline{d}^{\sf c}_{\rm R}\ell_{\rm R}\phi\;+\;\hat\lambda_{qq}\,\overline{u}_{\rm R}u^{\sf c}_{\rm R}\phi$
R_2	0	$(\mathbf{3},\mathbf{2})_{\frac{7}{6}}$	$\hat\lambda_{\rm L}\,(\overline{q}_{\rm L}\cdot\phi)\,\ell_{\rm R}\;+\;\hat\lambda_{\rm R}\,\overline{u}_{\rm R}\,(l_{\rm L}\cdot\epsilon\cdot\phi)$
$\widetilde{R}_2$	0	$(\mathbf{3},\mathbf{2})_{\frac{1}{6}}$	$\hat\lambda_{\rm R}\,\overline{d}_{\rm R}\,(l_{\rm L}\cdot\epsilon\cdot\phi)$
S_3	0	$(\overline{\mathbf{3}},\mathbf{3})_{\frac{1}{3}}$	$\hat\lambda_{\rm L}\,(\overline{q}^{\sf c}_{\rm L}\cdot\epsilon\cdot\tau^a\cdot l_{\rm L})\,\phi^a\;+\;\hat\lambda_{qq}\,(\overline{q}_{\rm L}\cdot\epsilon\cdot\tau^a\cdot q^{\sf c}_{\rm L})\,\phi^a$
U_1	1	$(\mathbf{3},\mathbf{1})_{\frac{2}{3}}$	$\hat\lambda_{\rm L}\,(\overline{q}_{\rm L}\gamma^\mu l_{\rm L})\,\phi_\mu\;+\;\hat\lambda_{\rm R}\,\overline{d}_{\rm R}\gamma^\mu\ell_{\rm R}\phi_\mu$
$\widetilde{U}_1$	1	$(\mathbf{3},\mathbf{1})_{\frac{5}{3}}$	$\hat\lambda_{\rm R}\,\overline{u}_{\rm R}\gamma^\mu\ell_{\rm R}\phi_\mu$
V_2	1	$(\overline{\mathbf{3}},\mathbf{2})_{\frac{5}{6}}$	$\hat\lambda_{\rm L}\,(\overline{q}^{\sf c}_{\rm L}\cdot\epsilon\cdot\phi_\mu)\,\gamma^\mu\ell_{\rm R}\;+\;\hat\lambda_{\rm R}\,\overline{d}^{\sf c}_{\rm R}\gamma^\mu\,(l_{\rm L}\cdot\epsilon\cdot\phi_\mu)\;+\;\hat\lambda_{qq}\,\overline{u}_{\rm R}\gamma^\mu\,(q^{\sf c}_{\rm L}\cdot\phi_\mu)$
$\widetilde{V}_2$	1	$(\overline{\mathbf{3}},\mathbf{2})_{-\frac{1}{6}}$	$\hat\lambda_{\rm R}\,\overline{u}^{\sf c}_{\rm R}\gamma^\mu\,(l_{\rm L}\cdot\epsilon\cdot\phi_\mu)\;+\;\hat\lambda_{qq}\,(\overline{q}_{\rm L}\cdot\phi_\mu)\,\gamma^\mu d^{\sf c}_{\rm R}$
U_3	1	$(\mathbf{3},\mathbf{3})_{\frac{2}{3}}$	$\hat\lambda_{\rm L}\,(\overline{q}_{\rm L}\cdot\tau^a\cdot\gamma^\mu l_{\rm L})\,\phi^a_\mu$

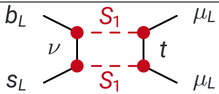
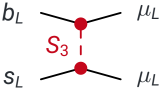
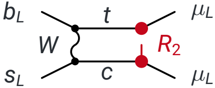
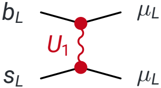
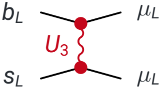
Table by Christoph Niehoff

Leptoquark contributions to WET Wilson coefficients

	$C_9^{\rm NP}$	$C_{10}^{\rm NP}$	C_9'	C_{10}'	C_S	C_P	C_S'	C_P'	$C_L^{\rm NP}$	C_R
S_1	—	—	—	—	—	—	—	—	$-\frac{1}{4}\lambda_{\rm L}^{b\ell}\lambda_{\rm L}^{s\ell\,*}$	—
$\widetilde{S}_1$	—	—	$-\frac{1}{2}\lambda_{\rm R}^{b\ell}\lambda_{\rm R}^{s\ell\,*}$	$+C_9'$	—	—	—	—	—	—
R_2	$\frac{1}{2}\lambda_{\rm L}^{s\ell}\lambda_{\rm L}^{b\ell\,*}$	$+C_9^{\rm NP}$	—	—	—	—	—	—	—	—
$\widetilde{R}_2$	—	—	$-\frac{1}{2}\lambda_{\rm R}^{s\ell}\lambda_{\rm R}^{b\ell\,*}$	$-C_9'$	—	—	—	—	—	$+C_9'$
S_3	$\frac{3}{4}\lambda_{\rm L}^{b\ell}\lambda_{\rm L}^{s\ell\,*}$	$-C_9^{\rm NP}$	—	—	—	—	—	—	$+\frac{1}{2}C_9^{\rm NP}$	—
U_1	$-\frac{1}{2}\lambda_{\rm L}^{s\ell}\lambda_{\rm L}^{b\ell\,*}$	$-C_9^{\rm NP}$	$-\frac{1}{2}\lambda_{\rm R}^{s\ell}\lambda_{\rm R}^{b\ell\,*}$	$+C_9'$	$\lambda_{\rm L}^{s\ell}\lambda_{\rm R}^{b\ell\,*}m_b^{-1}$	$-C_S$	$-\lambda_{\rm R}^{s\ell}\lambda_{\rm L}^{b\ell\,*}m_b^{-1}$	$+C_S'$	—	—
$\widetilde{U}_1$	—	—	—	—	—	—	—	—	—	—
V_2	$-\frac{1}{2}\lambda_{\rm L}^{b\ell}\lambda_{\rm L}^{s\ell\,*}$	$+C_9^{\rm NP}$	$\frac{1}{2}\lambda_{\rm R}^{b\ell}\lambda_{\rm R}^{s\ell\,*}$	$-C_9'$	$\lambda_{\rm L}^{b\ell}\lambda_{\rm R}^{s\ell\,*}m_b^{-1}$	$-C_S$	$-\lambda_{\rm R}^{b\ell}\lambda_{\rm L}^{s\ell\,*}m_b^{-1}$	$+C_S'$	—	$+C_9'$
$\widetilde{V}_2$	—	—	—	—	—	—	—	—	—	—
U_3	$-\frac{3}{2}\lambda_{\rm L}^{b\ell}\lambda_{\rm L}^{s\ell\,*}$	$-C_9^{\rm NP}$	—	—	—	—	—	—	$+2C_9^{\rm NP}$	

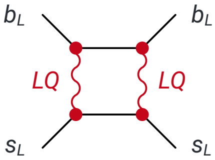
Table by Christoph Niehoff

Leptoquarks: possible solutions for $b \to s\mu\mu$

<table>
<tr><th>Spin</th><th>G_{SM}</th><th>Name</th><th>Characteristic process</th><th></th></tr>
<tr><td>0</td><td>$(\bar{3},1)_{1/3}$</td><td>S_1</td><td>
</td><td>Bauer, Neubert, arXiv:1511.01900</td></tr>
<tr><td>0</td><td>$(\bar{3},3)_{1/3}$</td><td>S_3</td><td>
</td><td>Hiller, Schmaltz, arXiv:1408.1627</td></tr>
<tr><td>0</td><td>$(3,2)_{7/6}$</td><td>R_2</td><td>
</td><td>Bečirević, Sumensari, arXiv:1704.05835</td></tr>
<tr><td>1</td><td>$(3,1)_{2/3}$</td><td>U_1</td><td>
</td><td>Barbieri et al., arXiv:1512.01560</td></tr>
<tr><td>1</td><td>$(3,3)_{2/3}$</td><td>U_3</td><td>
</td><td>Fajfer, Košnik, arXiv:1511.06024</td></tr>
</table>

Leptoquarks: B_s-$\bar{B}_s$ mixing loop-suppressed

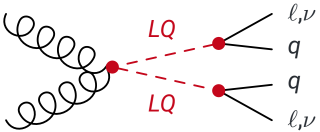
- Generic strong constraint on Z' models is loop-suppressed for leptoquark models



- Big advantage compared to Z'

Leptoquarks: direct constraints

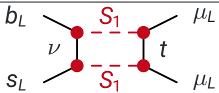
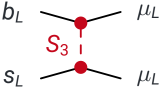
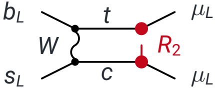
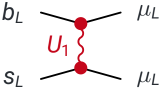
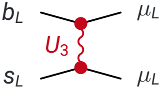
- QCD pair production
- Direct searches with $jj\ell\ell$ or $jj\nu\nu$ final states



Decays	Scalar LQ limits	Vector LQ limits	$\mathcal{L}_{\text{int}}$ / Ref.
$jj\,\tau\bar{\tau}$	–	–	–
$b\bar{b}\,\tau\bar{\tau}$	1.0 (0.8) TeV	1.5 (1.3) TeV	36 fb^{-1} [39]
$t\bar{t}\,\tau\bar{\tau}$	1.4 (1.2) TeV	2.0 (1.8) TeV	140 fb^{-1} [40]
$jj\,\mu\bar{\mu}$	1.7 (1.4) TeV	2.3 (2.1) TeV	140 fb^{-1} [41]
$b\bar{b}\,\mu\bar{\mu}$	1.7 (1.5) TeV	2.3 (2.1) TeV	140 fb^{-1} [41]
$t\bar{t}\,\mu\bar{\mu}$	1.5 (1.3) TeV	2.0 (1.8) TeV	140 fb^{-1} [42]
$jj\,\nu\bar{\nu}$	1.0 (0.6) TeV	1.8 (1.5) TeV	36 fb^{-1} [43]
$b\bar{b}\,\nu\bar{\nu}$	1.1 (0.8) TeV	1.8 (1.5) TeV	36 fb^{-1} [43]
$t\bar{t}\,\nu\bar{\nu}$	1.2 (0.9) TeV	1.8 (1.6) TeV	140 fb^{-1} [44]

Angelescu, Bečirević, Faroughy, Jaffredo, Sumensari, arXiv:2103.12504

Leptoquarks: still viable solutions for $b \to s\mu\mu$

Spin	G_{SM}	Name	Characteristic process	$R_{K^{(*)}}$	
0	$(\bar{3}, 1)_{1/3}$	S_1		X	requires too large couplings
0	$(\bar{3}, 3)_{1/3}$	S_3		✓	
0	$(3, 2)_{7/6}$	R_2		X	tension with LHC limits
1	$(3, 1)_{2/3}$	U_1		✓	
1	$(3, 3)_{2/3}$	U_3		✓	

cf. Angelescu, Bečirević, Faroughy, Jaffredo, Sumensari, arXiv:2103.12504

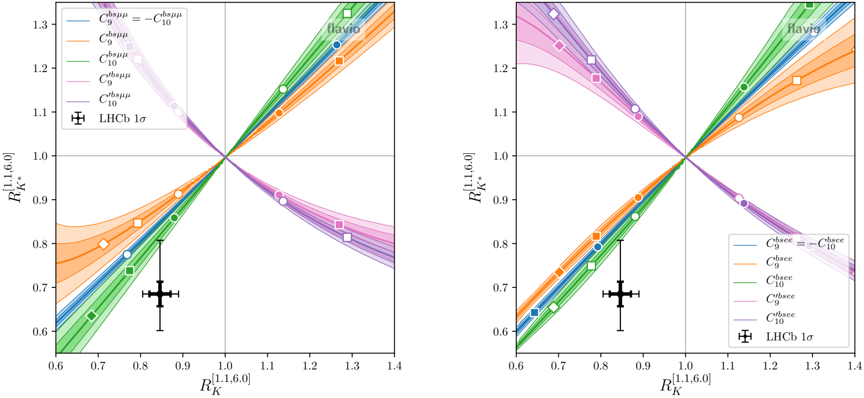
Theory uncertainties in presence of NP

Scenarios with a single Wilson coefficients

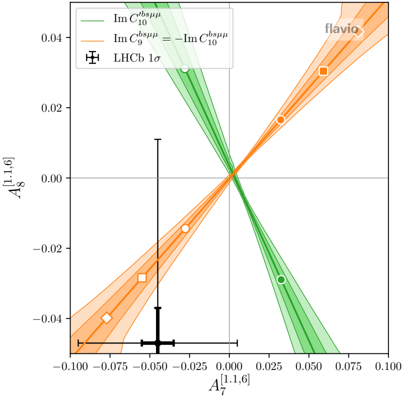
	Wilson coefficient	$b \to s\mu\mu$ best fit	$b \to s\mu\mu$ pull	LFU, $B_s \to \mu\mu$ best fit	LFU, $B_s \to \mu\mu$ pull	all rare B decays best fit	all rare B decays pull
NP err.	$C_9^{bs\mu\mu}$	$-0.70^{+0.21}_{-0.22}$	$\mathbf{3.3\sigma}$	$-0.74^{+0.20}_{-0.21}$	4.1σ	$-0.71^{+0.15}_{-0.15}$	$\mathbf{5.1\sigma}$
	$C_{10}^{bs\mu\mu}$	$+0.45^{+0.22}_{-0.23}$	1.9σ	$+0.60^{+0.14}_{-0.14}$	$\mathbf{4.7\sigma}$	$+0.54^{+0.12}_{-0.12}$	4.8σ
	$C_9^{bs\mu\mu} = -C_{10}^{bs\mu\mu}$	$-0.55^{+0.13}_{-0.13}$	$\mathbf{3.8\sigma}$	$-0.35^{+0.08}_{-0.08}$	$\mathbf{4.6\sigma}$	$-0.39^{+0.07}_{-0.07}$	$\mathbf{5.6\sigma}$
SM err.	$C_9^{bs\mu\mu}$	$-0.83^{+0.22}_{-0.20}$	$\mathbf{3.6\sigma}$	$-0.74^{+0.20}_{-0.21}$	4.1σ	$-0.77^{+0.15}_{-0.15}$	$\mathbf{5.3\sigma}$
	$C_{10}^{bs\mu\mu}$	$+0.45^{+0.21}_{-0.20}$	2.3σ	$+0.60^{+0.14}_{-0.14}$	$\mathbf{4.7\sigma}$	$+0.54^{+0.12}_{-0.12}$	4.9σ
	$C_9^{bs\mu\mu} = -C_{10}^{bs\mu\mu}$	$-0.60^{+0.17}_{-0.18}$	$\mathbf{3.8\sigma}$	$-0.35^{+0.08}_{-0.08}$	$\mathbf{4.6\sigma}$	$-0.39^{+0.07}_{-0.07}$	$\mathbf{5.6\sigma}$

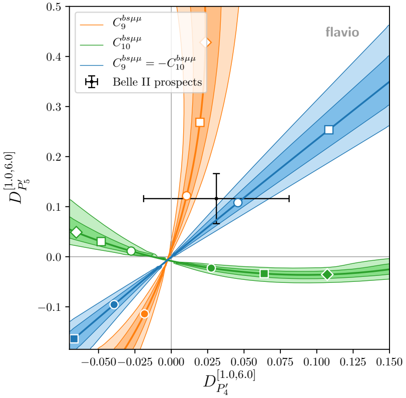
Visible effect of theory errors depending on new physics, in particular for $C_9^{bs\mu\mu}$

Theory uncertainties in presence of NP



Theory uncertainties in presence of NP





Parameterisation of beyond-QCDF contributions

Parameterisation of beyond-QCDF contributions for $B \to K$

$$C_9^{\text{eff}}(q^2) \to C_9^{\text{eff}}(q^2) + a_K + b_K(q^2/\,\text{GeV}^2) \quad \text{at low } q^2\,,$$

$$C_9^{\text{eff}}(q^2) \to C_9^{\text{eff}}(q^2) + c_K \quad \text{at high } q^2\,,$$

$$\text{Re}(a_K) = 0.0 \pm 0.08\,, \qquad \text{Re}(b_K) = 0.0 \pm 0.03\,, \qquad \text{Re}(c_K) = 0.0 \pm 0.2\,,$$
$$\text{Im}(a_K) = 0.0 \pm 0.08\,, \qquad \text{Im}(b_K) = 0.0 \pm 0.03\,, \qquad \text{Im}(c_K) = 0.0 \pm 0.2\,.$$

1σ uncertainties enclose the effects considered in Khodjamirian et al. arXiv:1006.4945, Beylich et al. arXiv:1101.5118, Khodjamirian et al. arXiv:1211.0234

Parameterisation of beyond-QCDF contributions for $B \to K^*$ and $B_s \to \phi$

$$
\begin{aligned}
C_7^{\text{eff}}(q^2) &\to C_7^{\text{eff}}(q^2) + a_{0,-} + b_{0,-}(q^2/\,\text{GeV}^2) \\
C_7' &\to C_7' + a_+ + b_+(q^2/\,\text{GeV}^2)
\end{aligned}
\qquad \text{at low } q^2 \,,
$$

$$
C_9^{\text{eff}}(q^2) \to C_9^{\text{eff}}(q^2) + c_\lambda \qquad \text{at high } q^2 \,,
$$

$$
\begin{aligned}
\text{Re}(a_+) &= 0.0 \pm 0.004 \,, & \text{Re}(b_+) &= 0.0 \pm 0.005 \,, & \text{Re}(c_+) &= 0.0 \pm 0.3 \,, \\
\text{Im}(a_+) &= 0.0 \pm 0.004 \,, & \text{Im}(b_+) &= 0.0 \pm 0.005 \,, & \text{Im}(c_+) &= 0.0 \pm 0.3 \,, \\
\text{Re}(a_-) &= 0.0 \pm 0.015 \,, & \text{Re}(b_-) &= 0.0 \pm 0.01 \,, & \text{Re}(c_-) &= 0.0 \pm 0.3 \,, \\
\text{Im}(a_-) &= 0.0 \pm 0.015 \,, & \text{Im}(b_-) &= 0.0 \pm 0.01 \,, & \text{Im}(c_-) &= 0.0 \pm 0.3 \,, \\
\text{Re}(a_0) &= 0.0 \pm 0.12 \,, & \text{Re}(b_0) &= 0.0 \pm 0.05 \,, & \text{Re}(c_0) &= 0.0 \pm 0.3 \,, \\
\text{Im}(a_0) &= 0.0 \pm 0.12 \,, & \text{Im}(b_0) &= 0.0 \pm 0.05 \,, & \text{Im}(c_0) &= 0.0 \pm 0.3 \,.
\end{aligned}
$$

1σ uncertainties enclose the effects considered in Khodjamirian et al. arXiv:1006.4945, Beylich et al. arXiv:1101.5118